

Potsdam  
THE STATE UNIVERSITY OF NEW YORK

# SOAR: The Sky in Motion Life on the Tilted Teacup Ride

## The Year

Aileen A. O'Donoghue  
Priest Associate Professor of Physics

ST. LAWRENCE UNIVERSITY

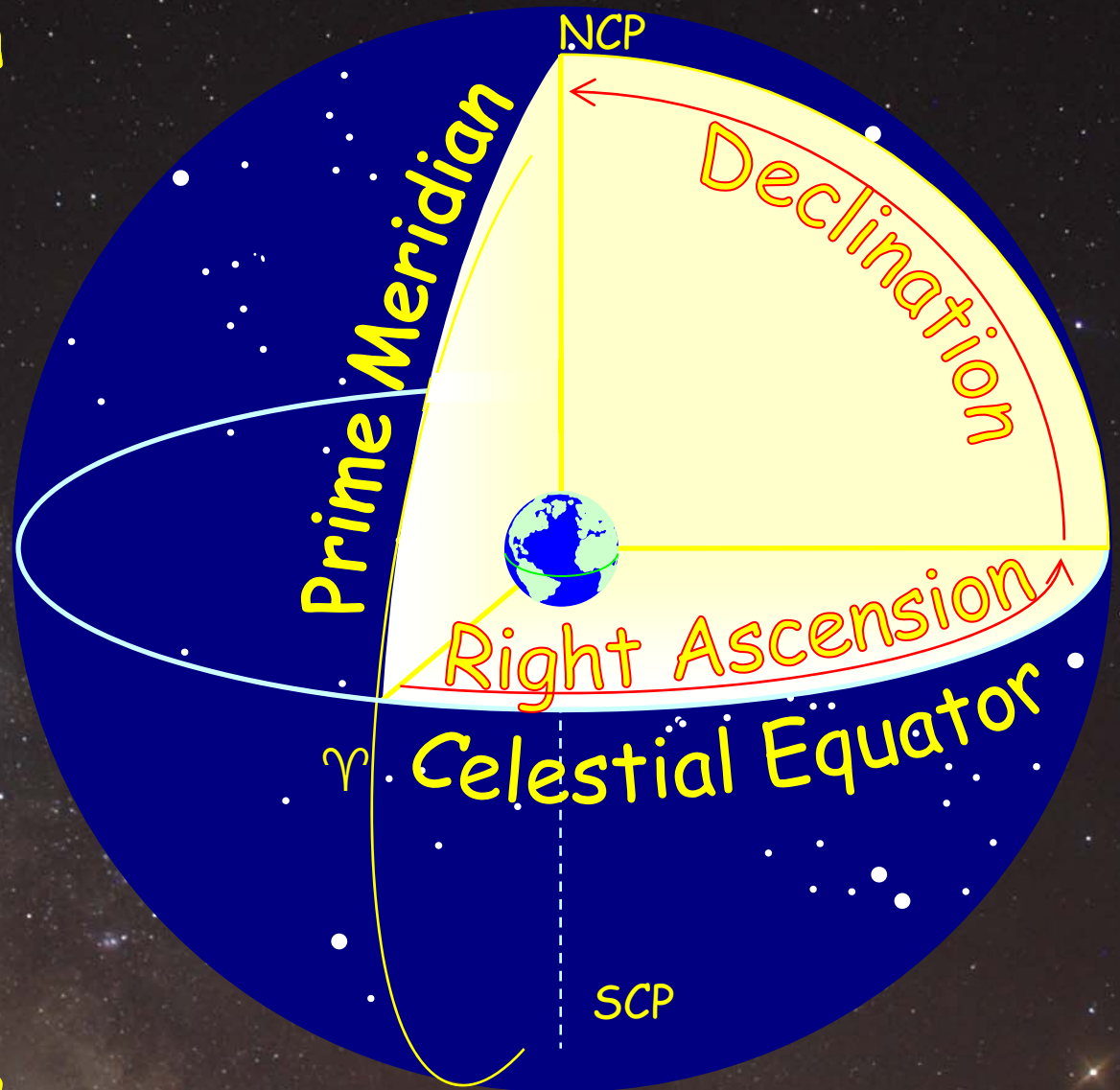
# Celestial Coordinates

## ☆ Right Ascension

- 🌐 RA or  $\alpha$
- 🌐 From prime meridian ( $0^h$ ) to  $23^h59^m59^s$  Eastward

## ☆ Declination

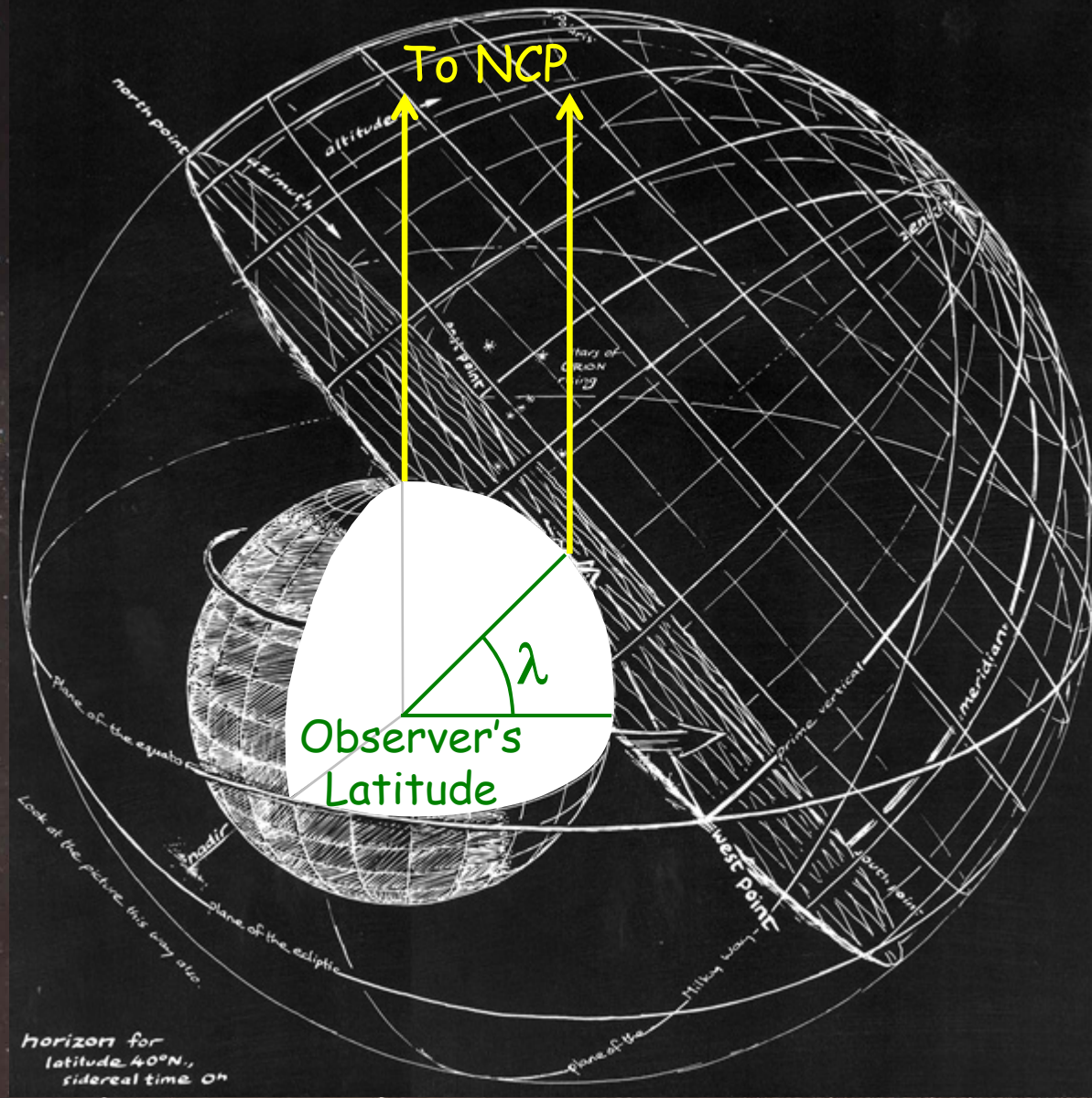
- 🌐 Dec or  $\delta$
- 🌐 From celestial equator ( $0^\circ$ ) to poles N & S  $90^\circ$



# Tilted Sky

☆ Observers see sky "tilted" due to latitude

Our view is tilted with respect to Earth's due to our latitude.

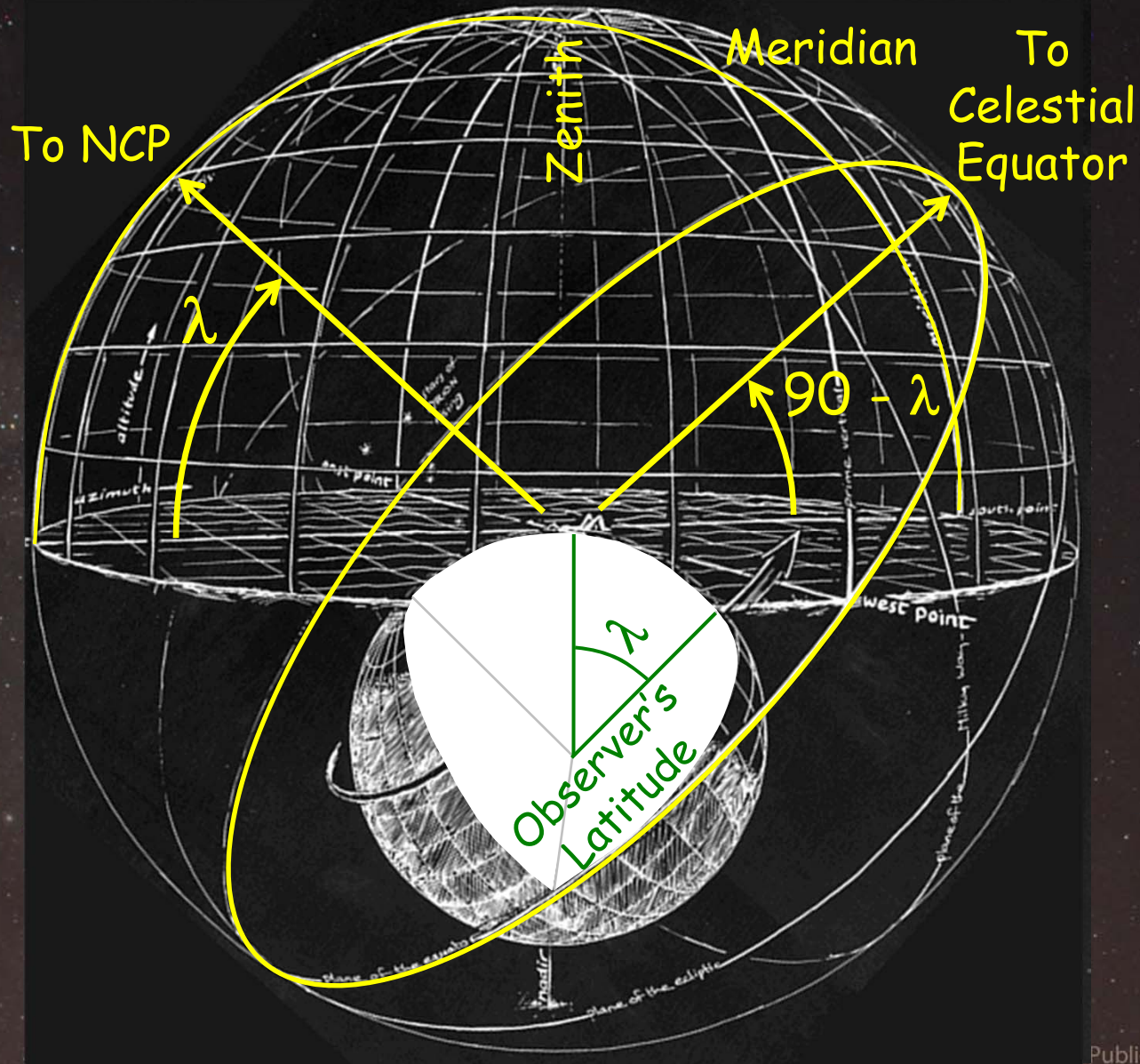


# Tilted Sky

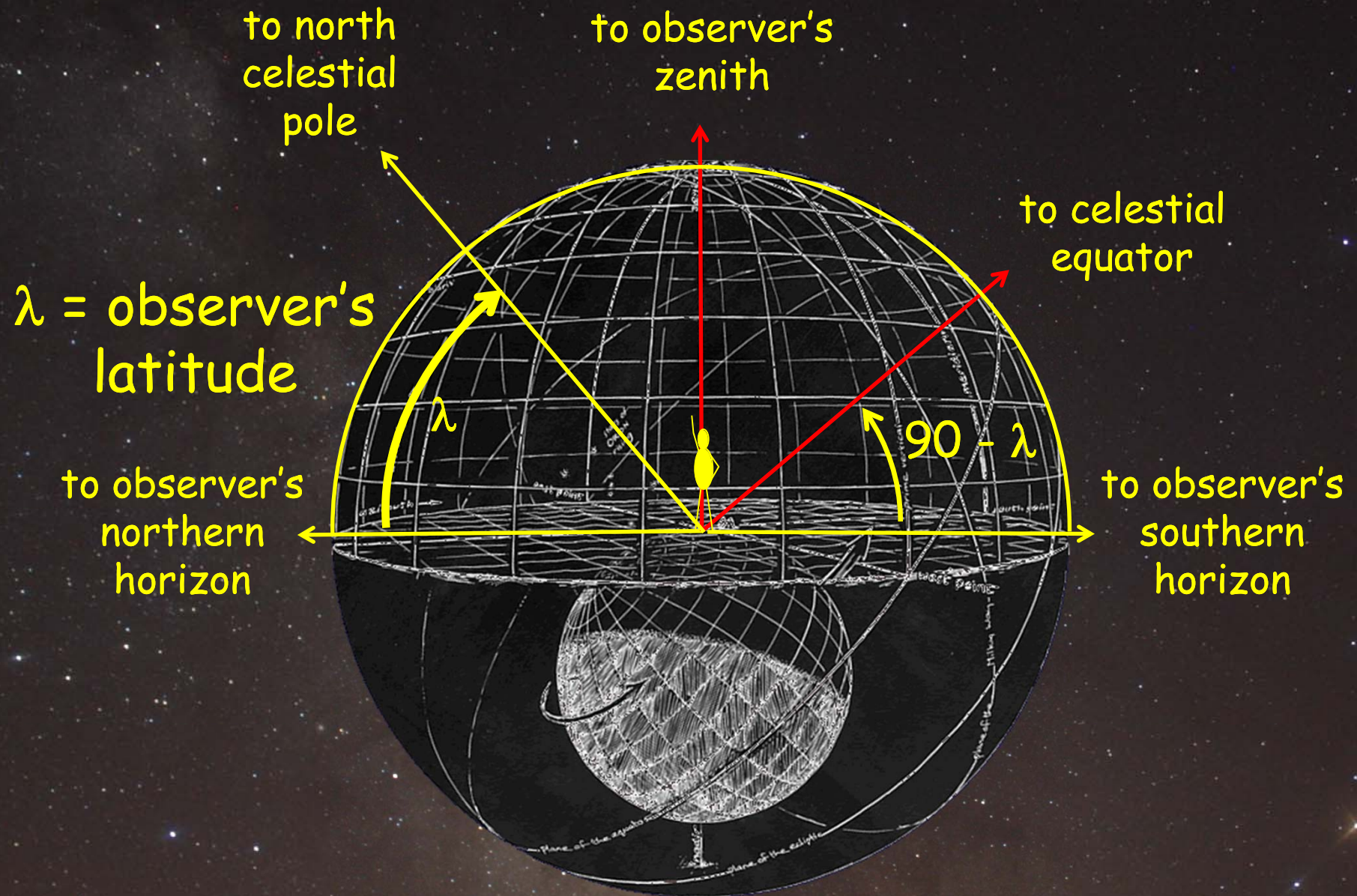
☆ Observers see sky "tilted" due to latitude

We see ourselves "on top" of the Earth, beneath the sky.

So we see sky motions tilted

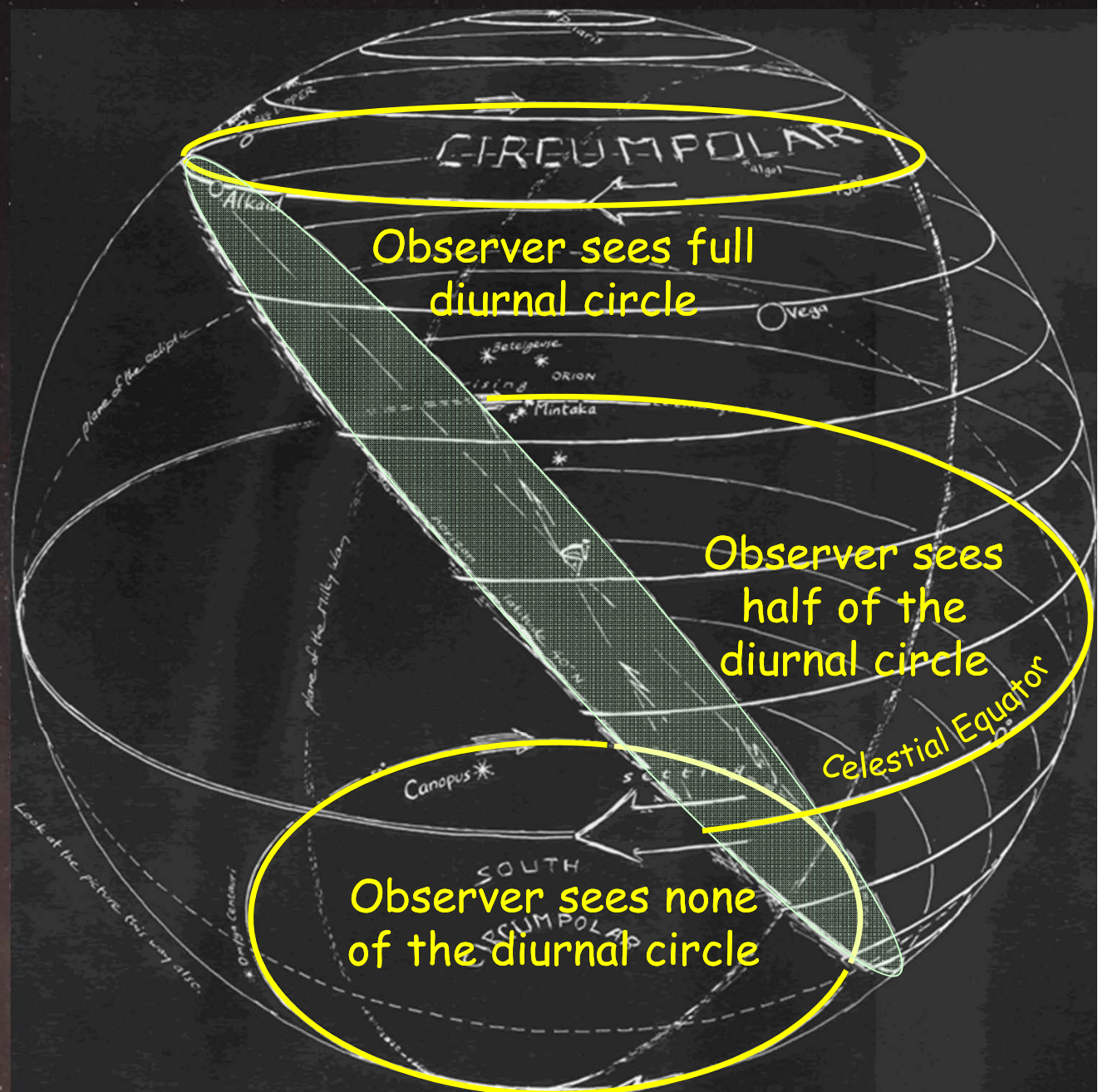


# Horizon Coordinate System



# Diurnal Circles

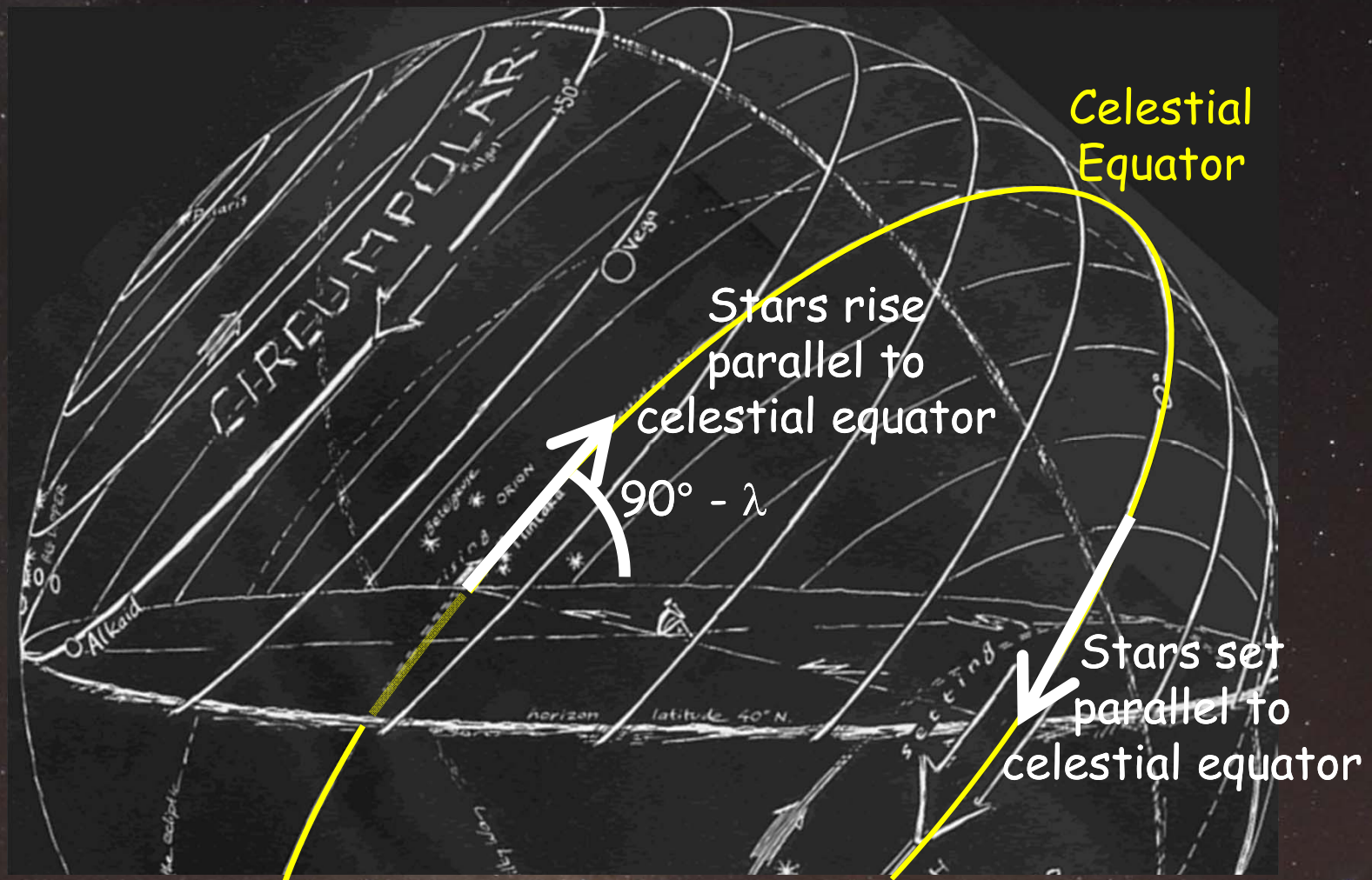
- ☆ Each celestial object circles the observer each day
- ☆ Observer sees part of each circle



# View of Observers

☆ Diurnal circles are parallel to CE

🌐 Stars rise and set at CE's angle from horizon

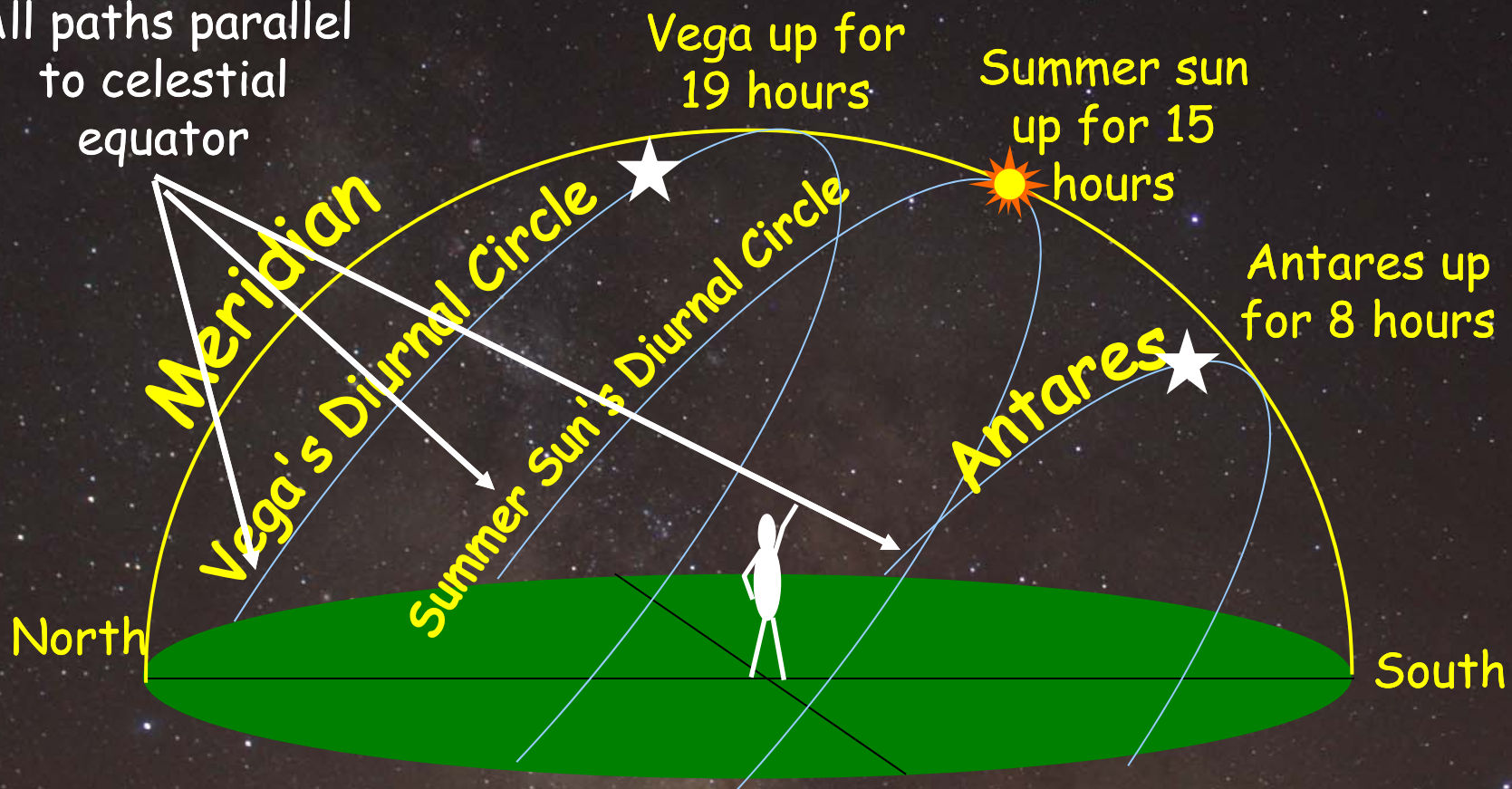


# Star Paths

☆ Each travels a diurnal circle

🌍 Portion of diurnal circle above horizon determines time object is "up"

All paths parallel to celestial equator



# Sunrise, Sunset ...

☆ Everything in the sky (sun, moon, stars, etc.)

🌍 Rises in the east

🌍 Sets in the west

each day

Measuring Circles:

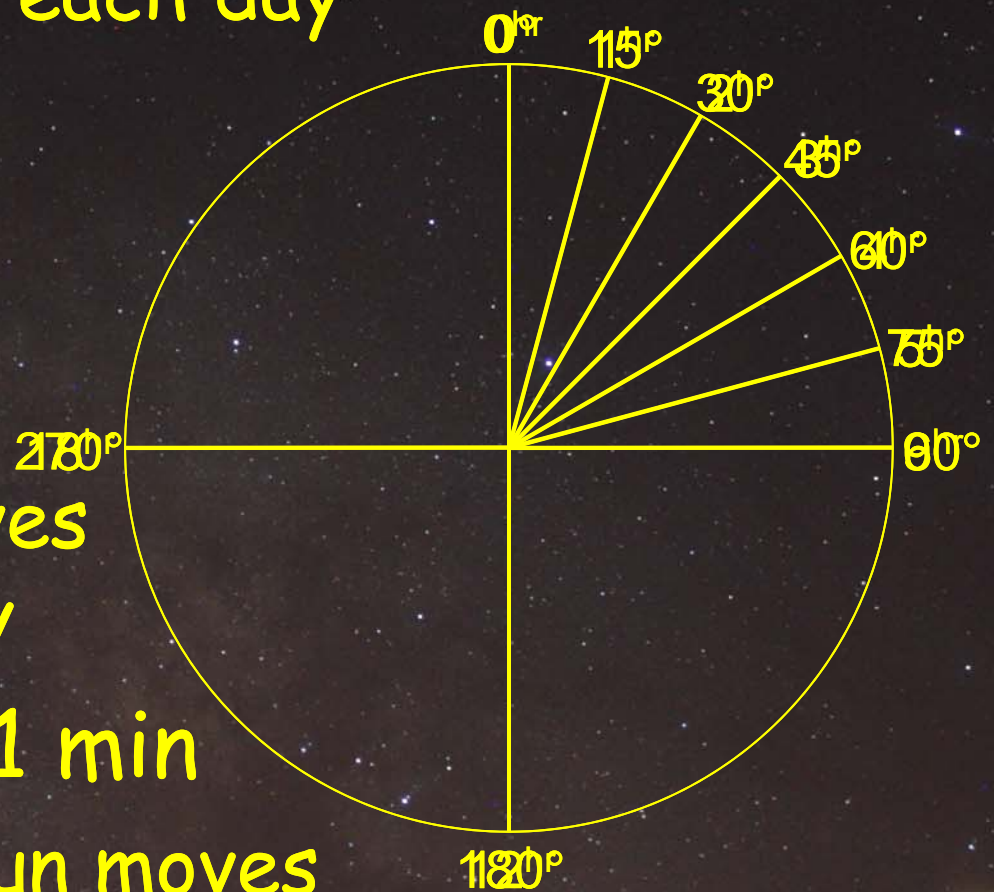
$360^\circ = 24 \text{ hr}$

$15^\circ = 1 \text{ hr}$

Each hour, the sun moves  
15 degrees in the sky

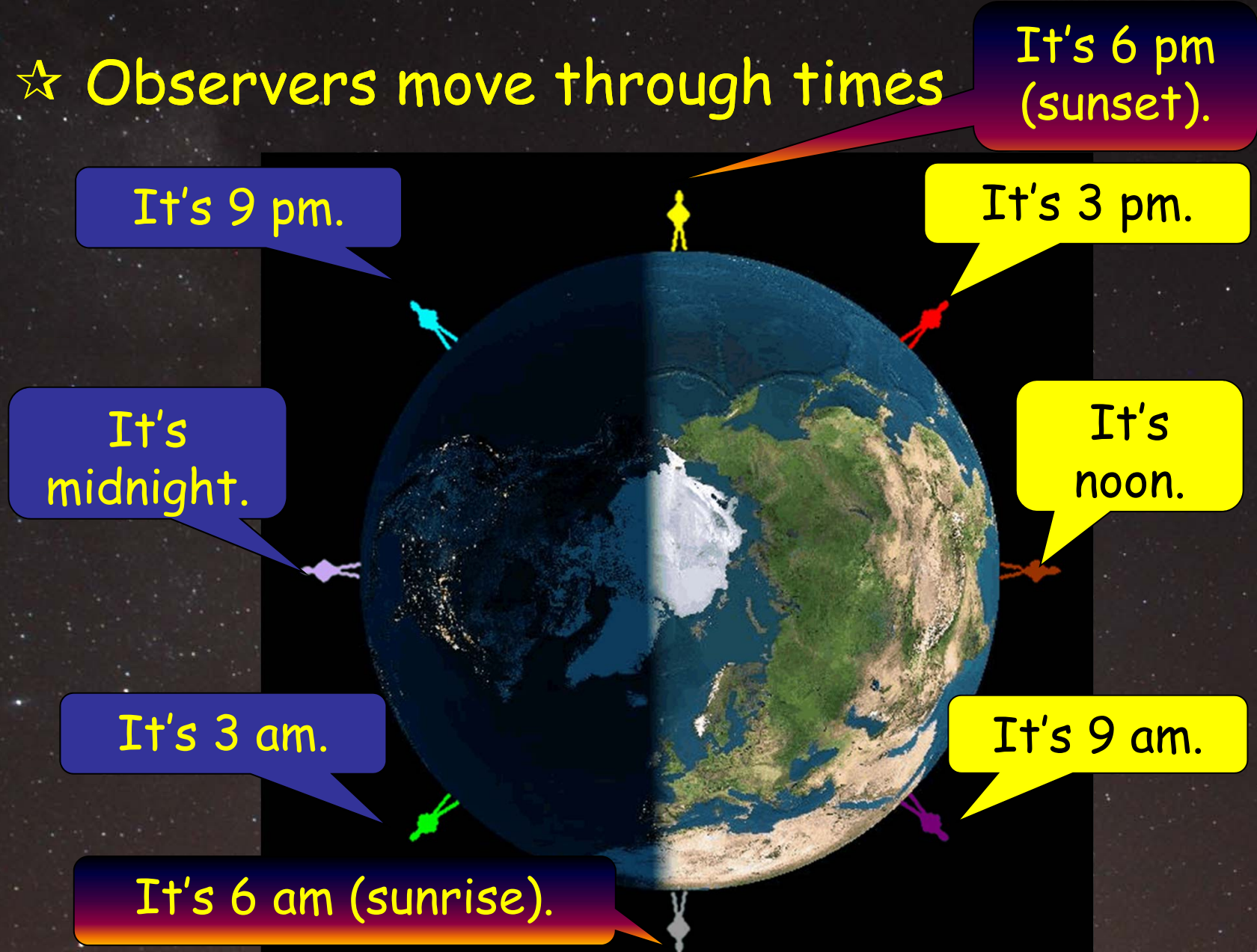
$1^\circ = 4 \text{ min}$  or  $15' = 1 \text{ min}$

Every 4 minutes, the sun moves  
1 degree = 60' in the sky



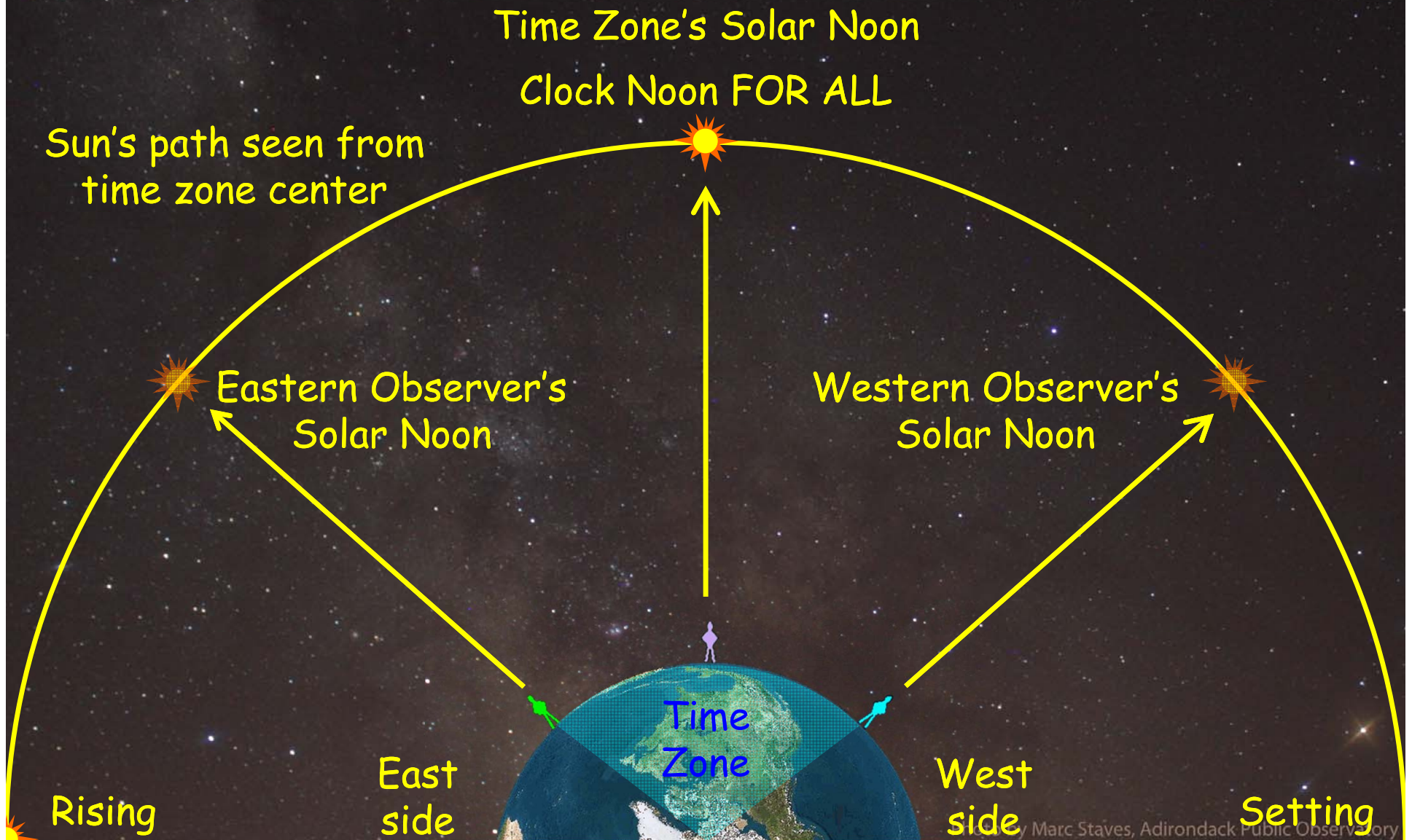
# Clock Time = Position of Sol

☆ Observers move through times



# Solar Time vs. Clock Time

☆ Solar time varies across time zones

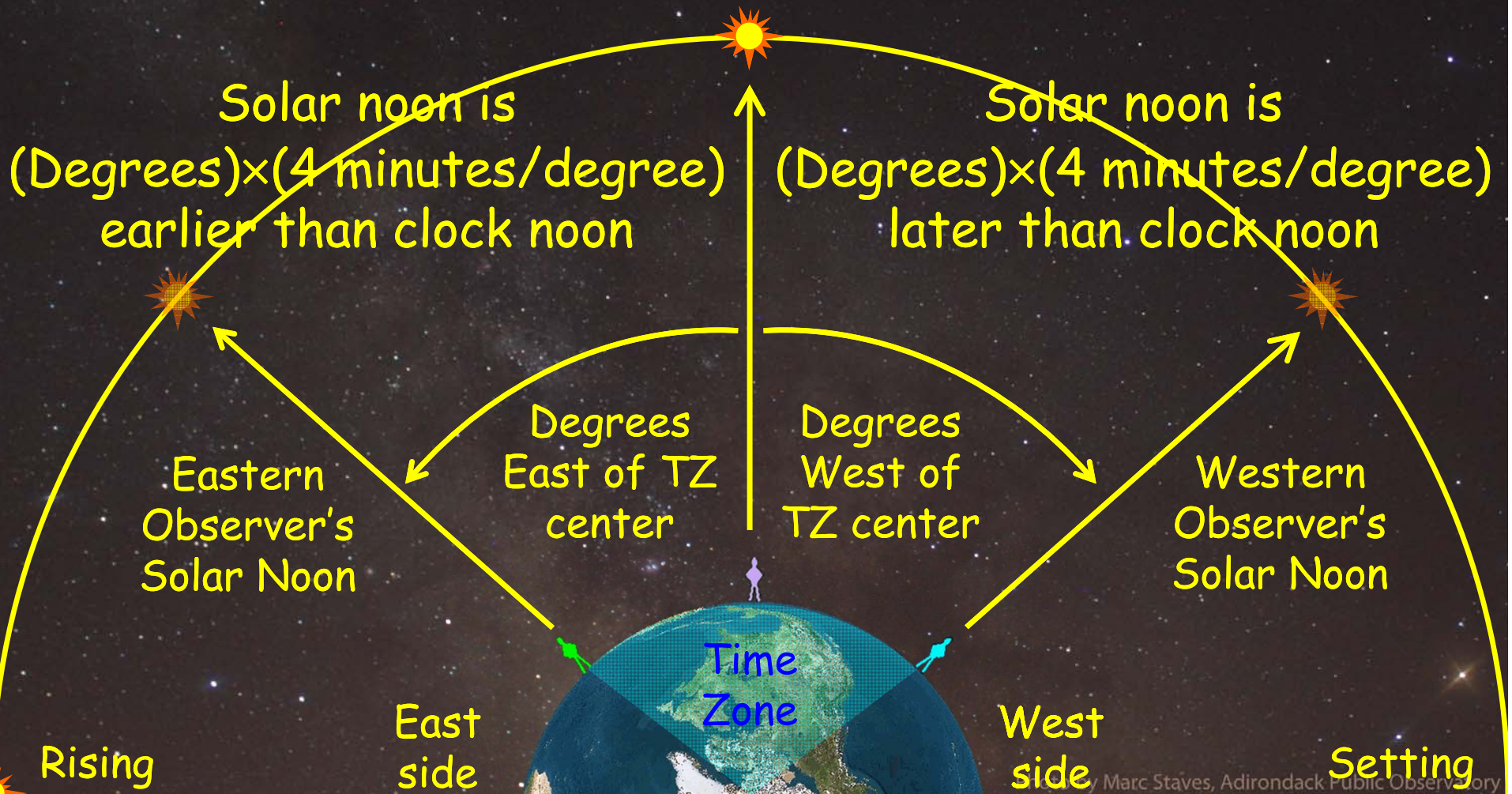


# Solar Time vs. Clock Time

☆ Solar time varies across time zones

Time Zone's Solar Noon

Clock Noon FOR ALL



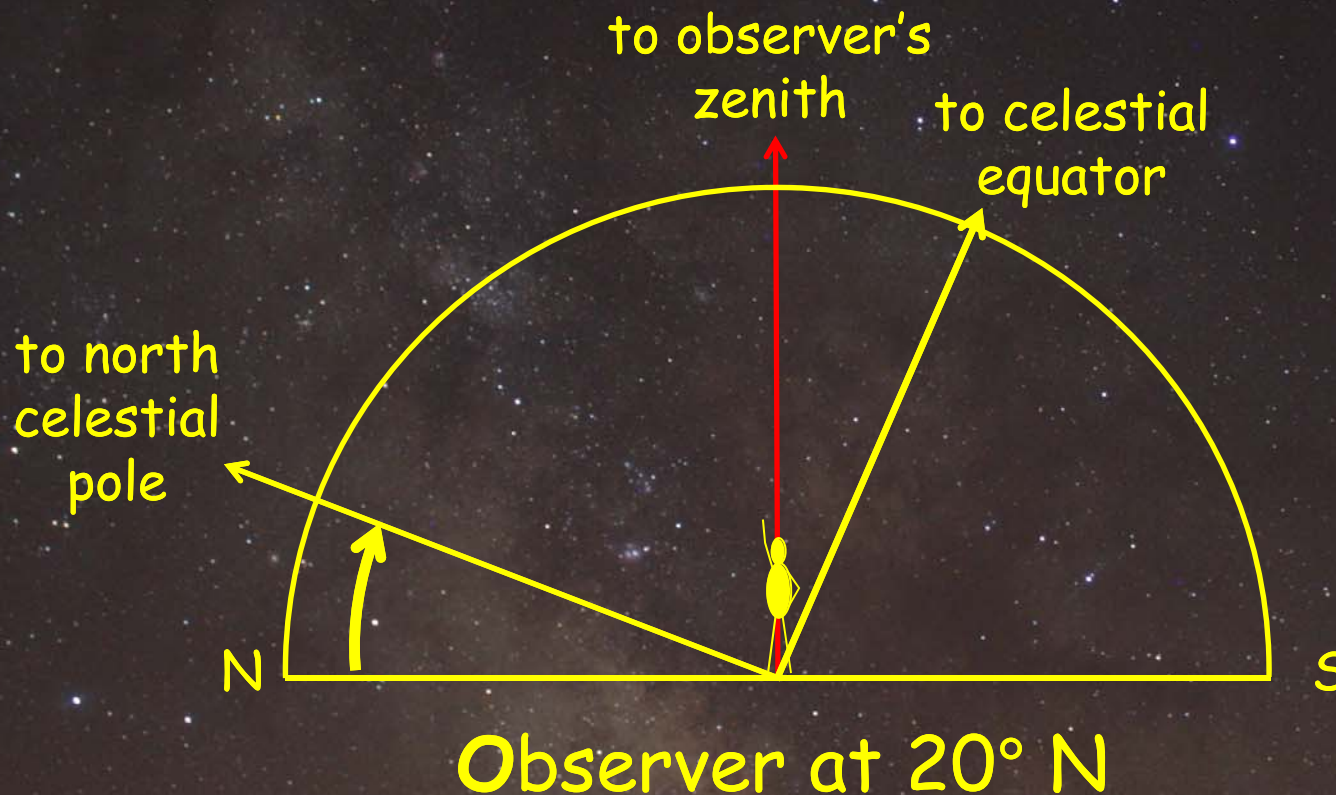
# Celestial Navigation

## ☆ Finding Latitude & Longitude from

🌍 Altitude of Polaris (NCP)

🌍 Transit time of star

› Looked up in an ephemeris (eg. Field Guide)

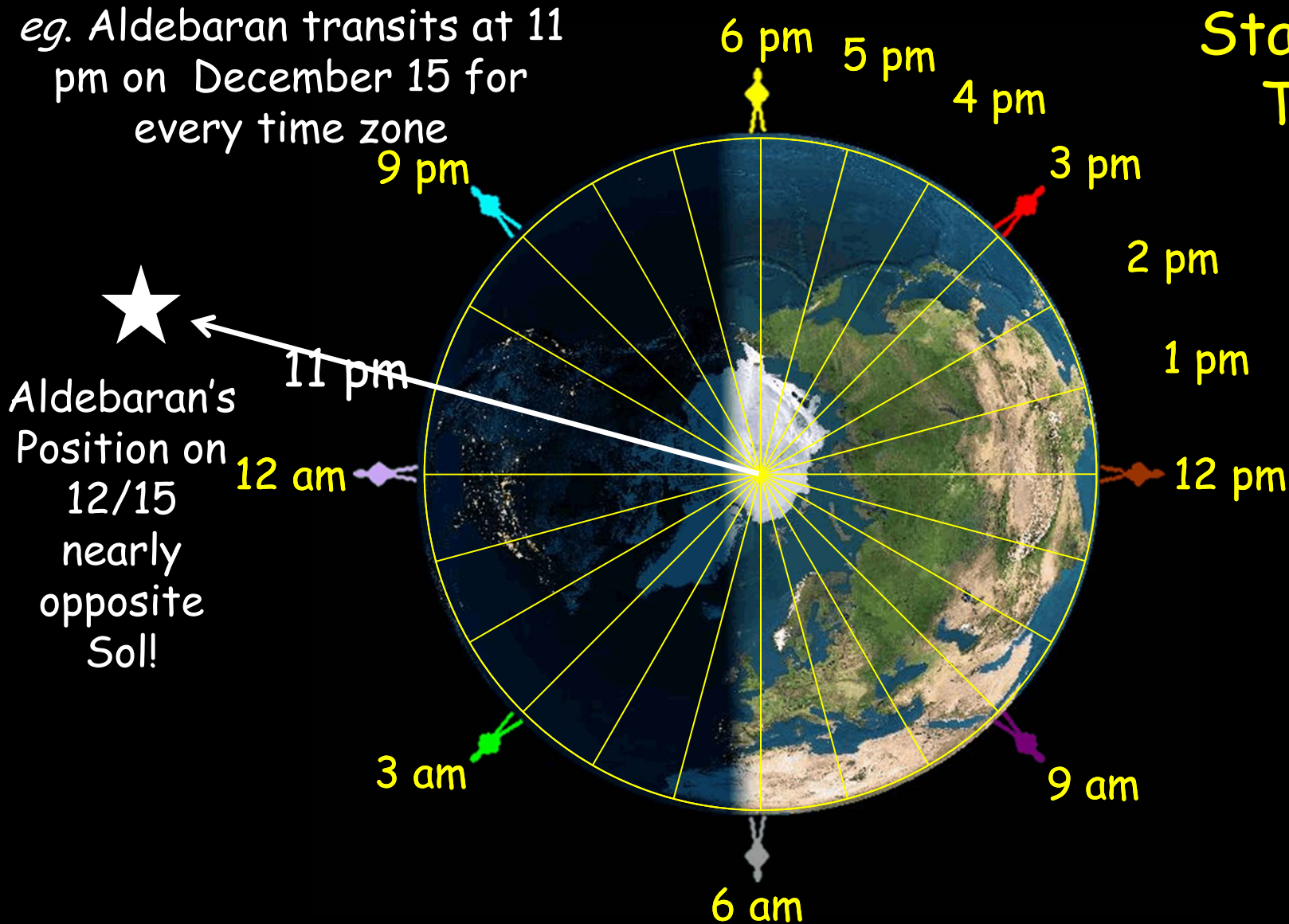


# Star Transit Time

Gives position of star with respect to the sun

eg. Aldebaran transits at 11 pm on December 15 for every time zone

Standard Time



# Clicker Question

☆ What's your longitude if you see Altair transit at 1 am on September first and your watch is set for Pacific time?

On 9/1 Altair transits at 10 pm PDT

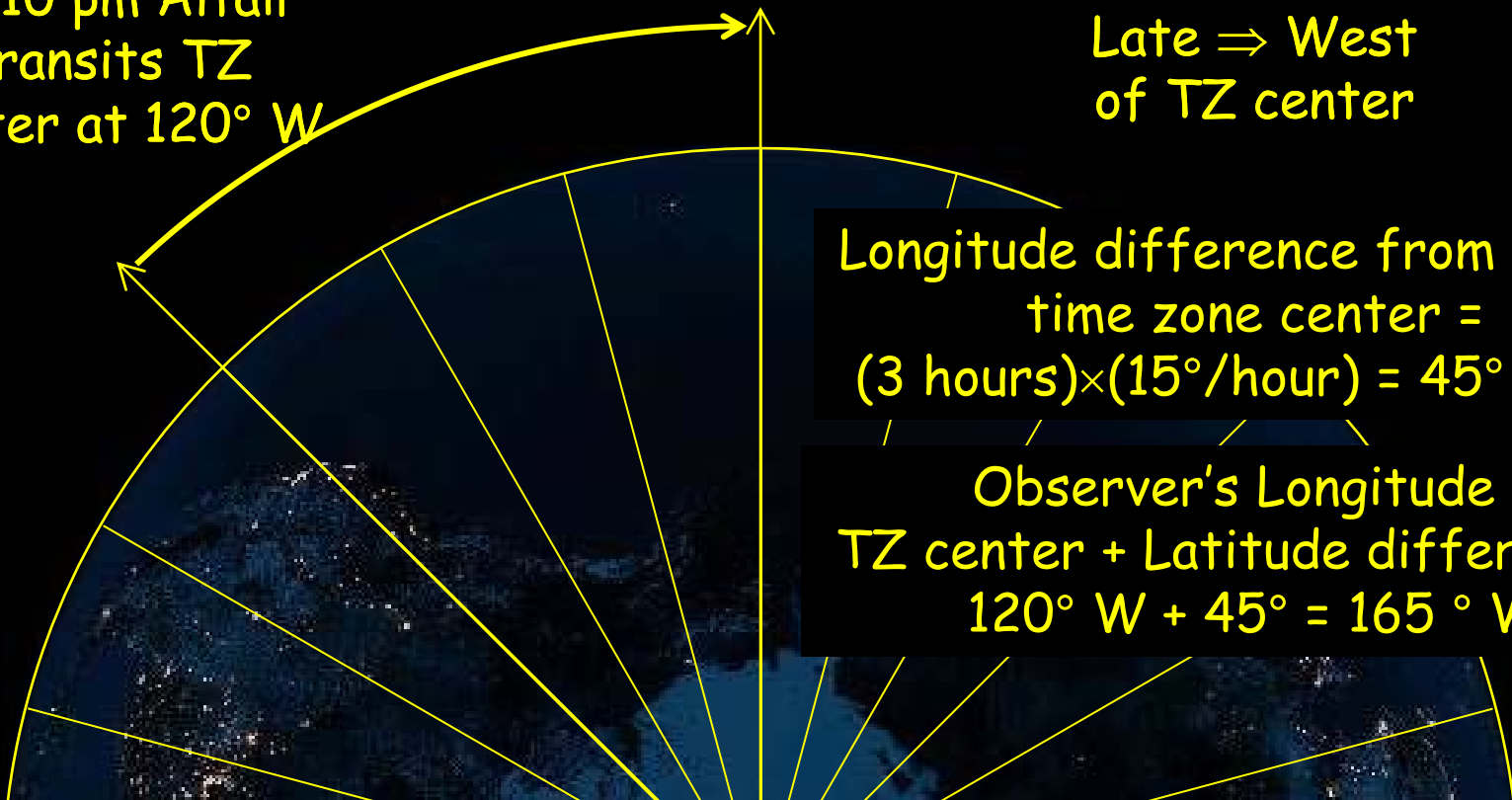
At 10 pm Altair transits TZ center at  $120^\circ$  W

Observer sees Altair transit at 1 am PDT

Late  $\Rightarrow$  West of TZ center

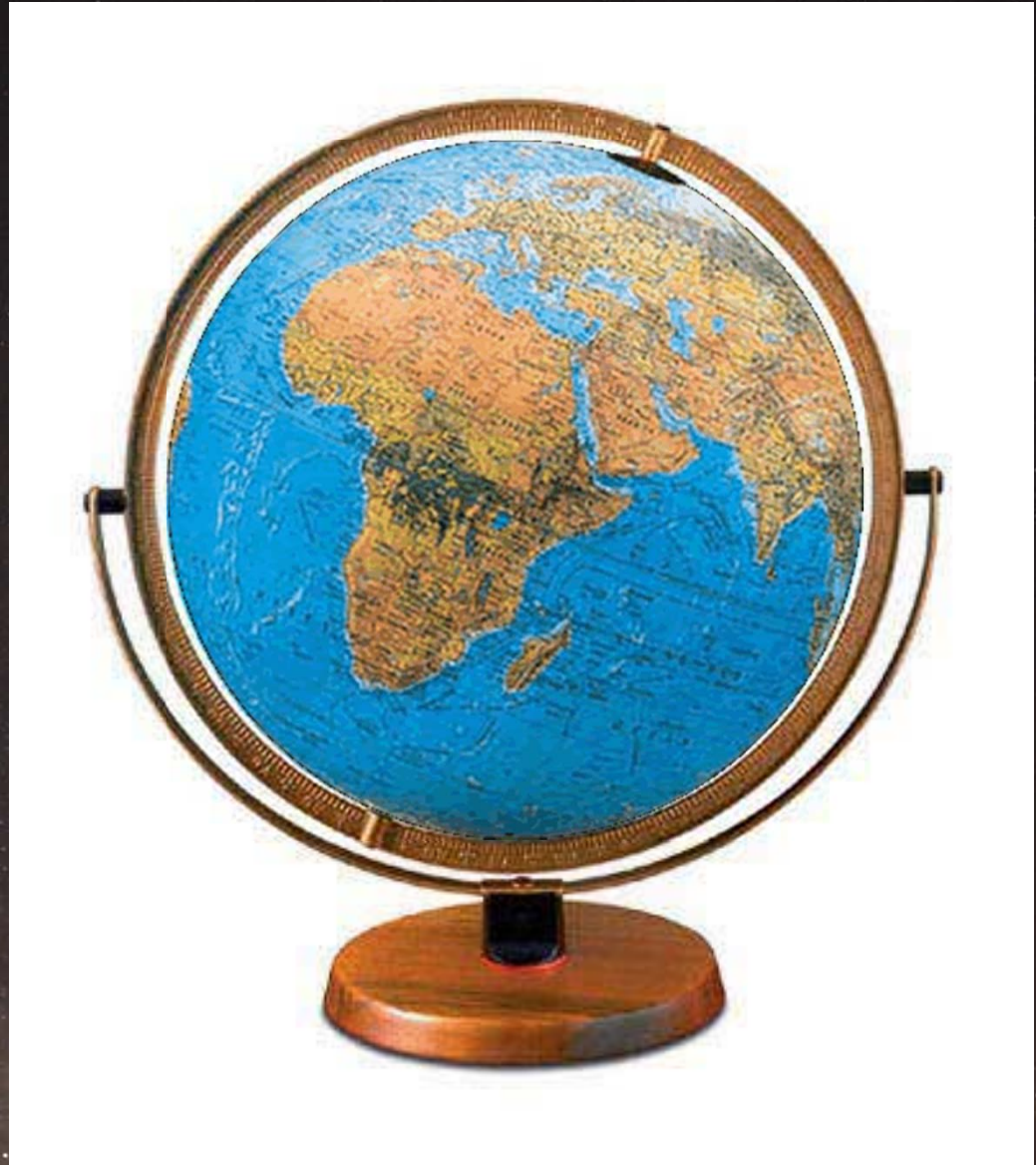
Longitude difference from clock's time zone center =  $(3 \text{ hours}) \times (15^\circ/\text{hour}) = 45^\circ$  West

Observer's Longitude = TZ center + Longitude difference =  $120^\circ$  W +  $45^\circ$  =  $165^\circ$  W

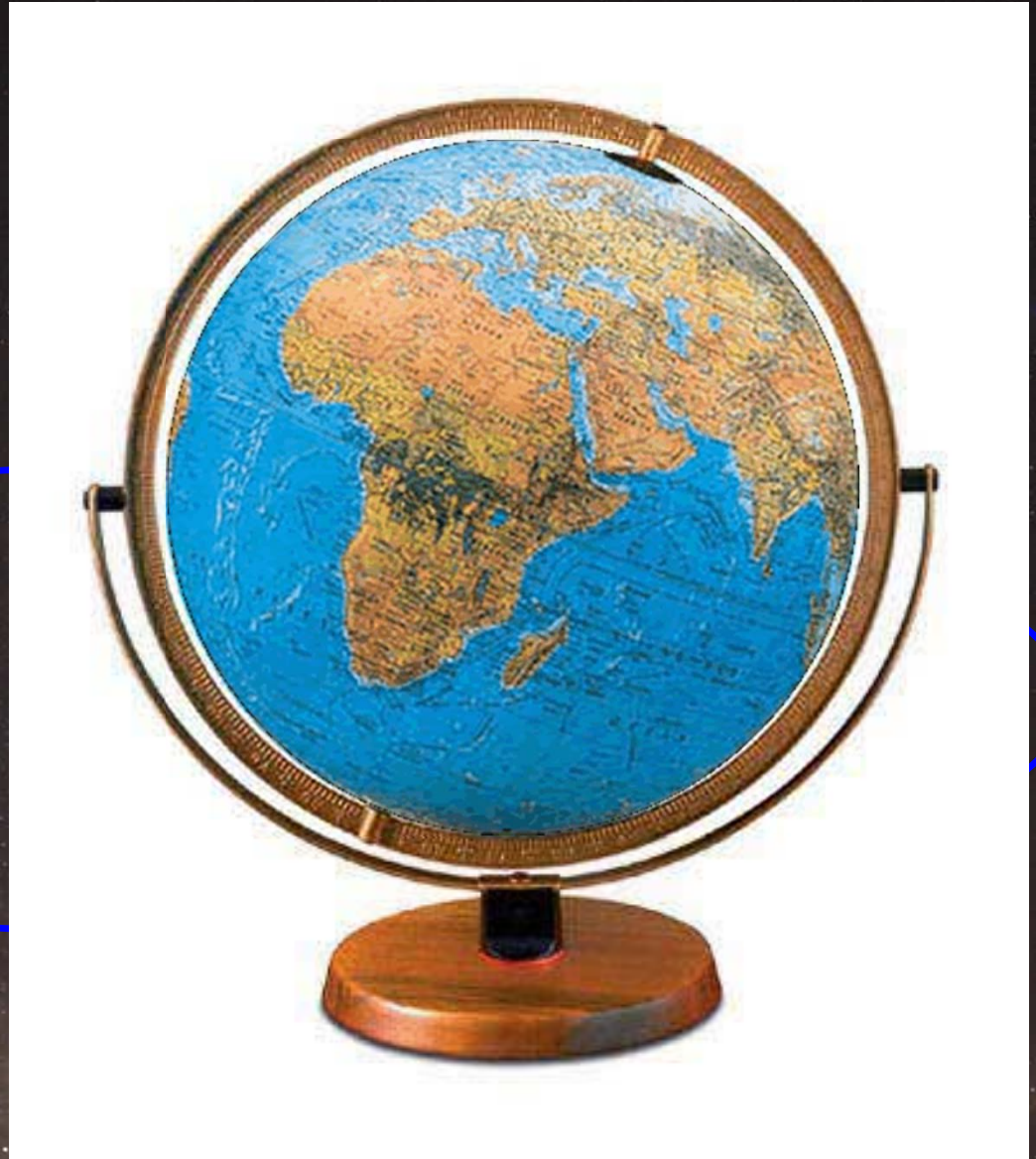


# Models of Earth

Why are  
globes  
tilted?



# Earth's Orbit



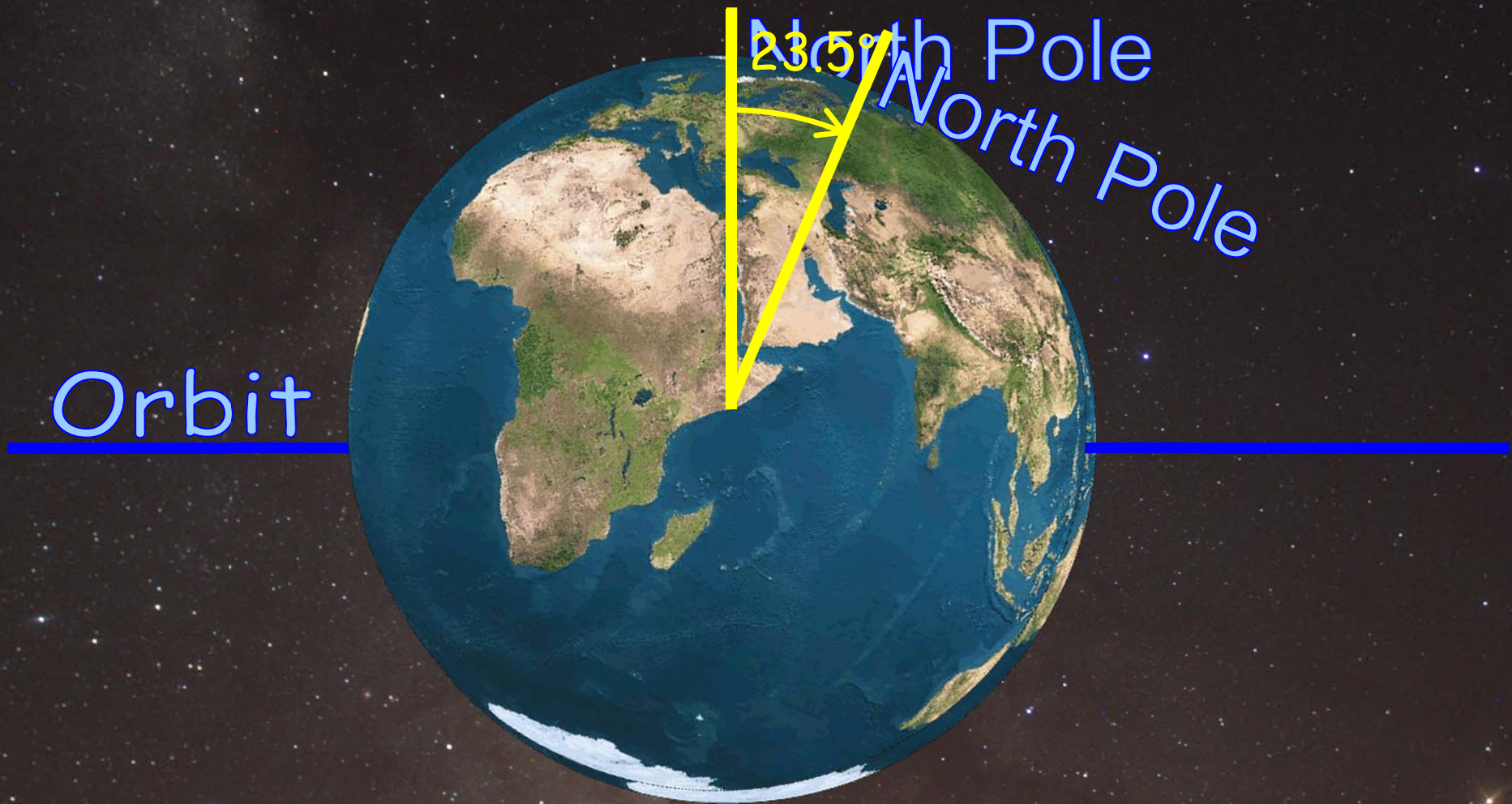
# Earth's Orbit

- ☆ Ellipse with sun at one focus
  - 🌍 perihelion - closest to sun
  - 🌍 aphelion - farthest from sun
- ☆ N Pole toward Polaris



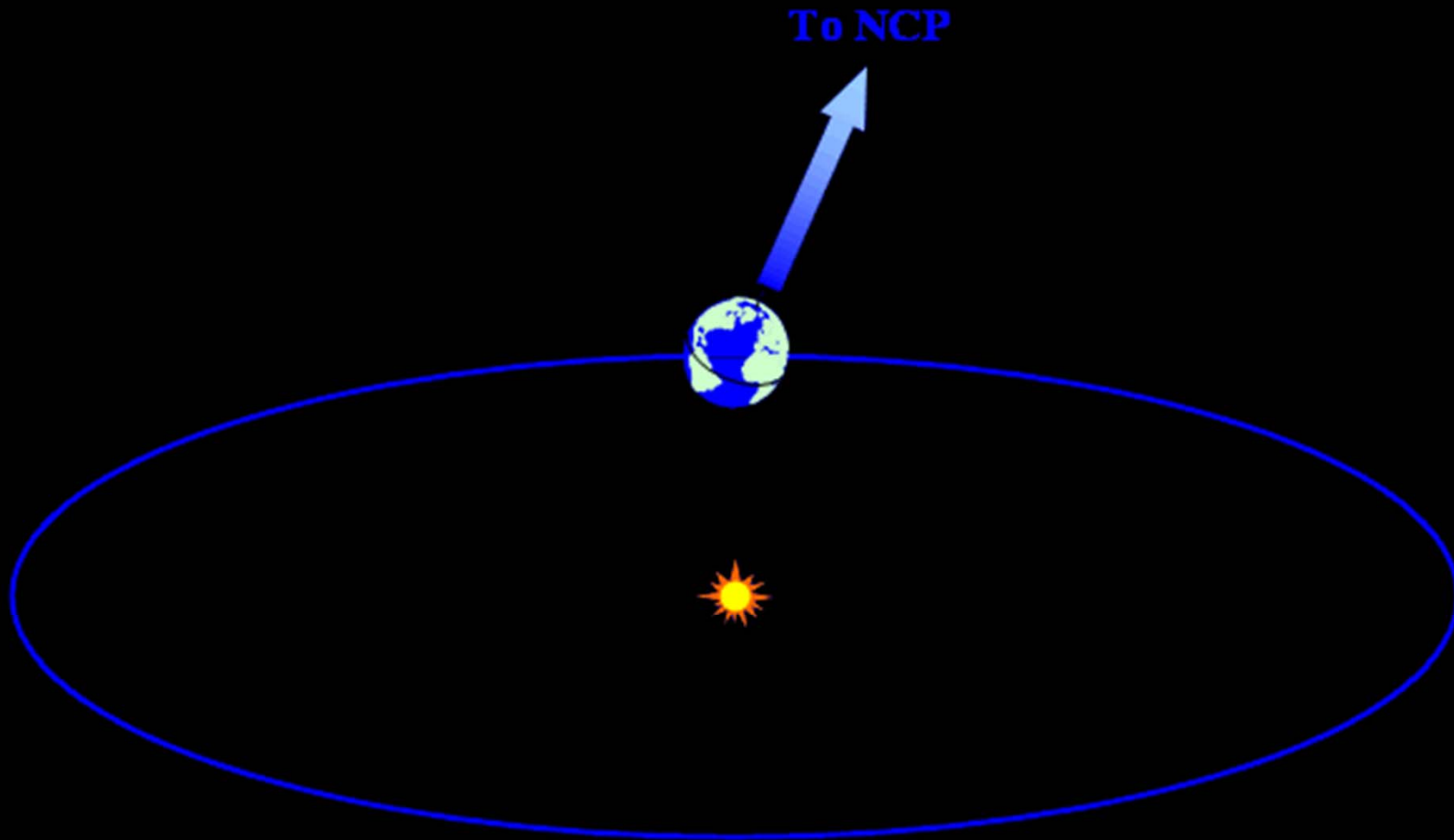
# Earth's Orbit

☆ Rotation Axis tilted  $23.5^\circ$  from  $\perp$



# Earth's Orbit

☆ Axis always points at Polaris



# The Home World

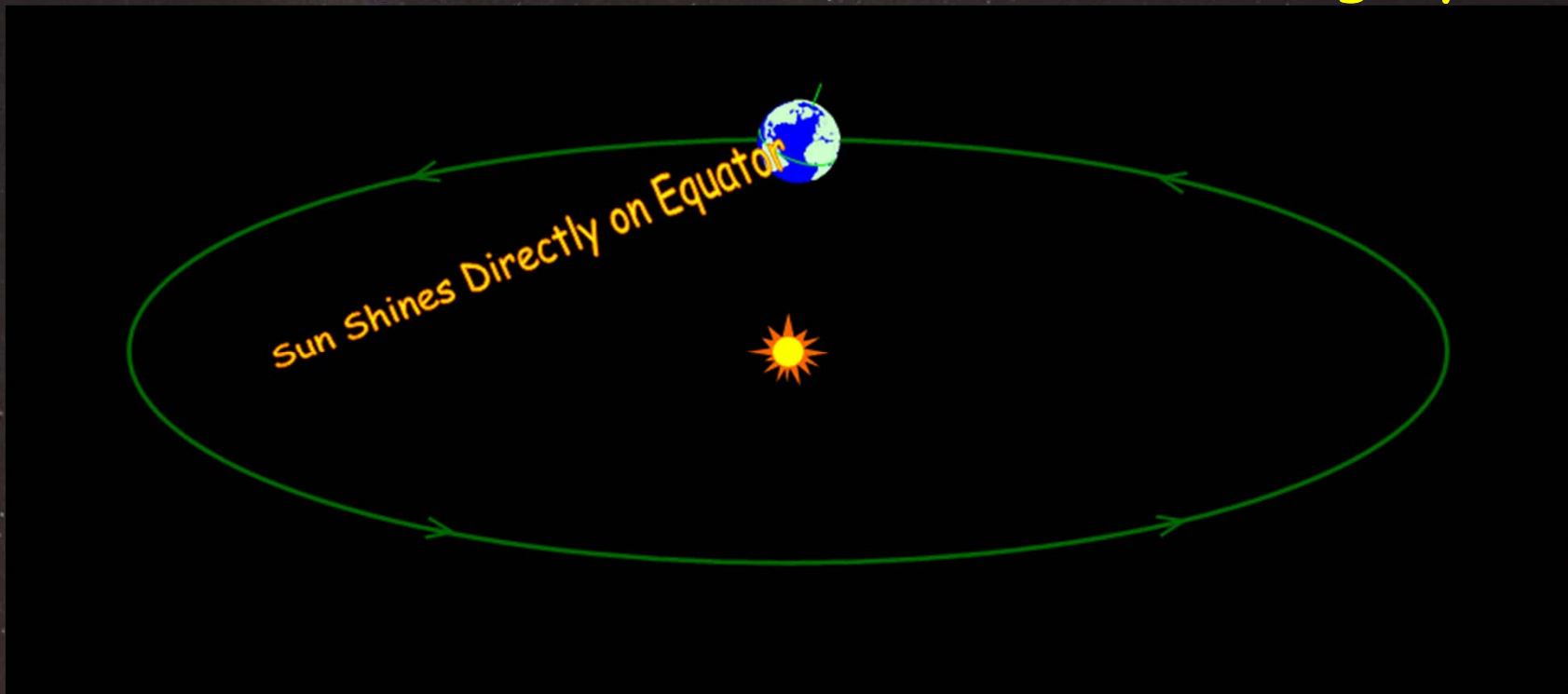
## ☆ The Earth in space

🌍  $360^\circ$  in 365 days  $\Rightarrow \sim 1^\circ/\text{day}$

🌍 Rotation axis tilted  $23.5^\circ$  from orbit axis

$\Rightarrow$  Declination of sun varies through year

$\Rightarrow$  subsolar latitude varies through year



# Solstices & Equinoxes

## ☆ Declination ( $\delta$ ) of the sun

🌍 Equinox: Sun crossing celestial equator  $\delta_{\text{Sol}} = 0^\circ$

› Vernal Equinox: sun moving north

› Autumnal Equinox: sun moving south

🌍 Solstice: Sun at N/S extreme  $\delta_{\text{Sol}} = \pm 23.5^\circ$

› (N) Summer solstice: sun at northernmost point

› (N) Winter solstice: sun at southernmost point

## ☆ Right Ascension ( $\alpha$ ) of the sun

🌍  $0^{\text{h}}$  = Vernal Equinox ( $\Upsilon$ )

🌍  $6^{\text{h}}$  = Summer Solstice ( $\text{II}$ )

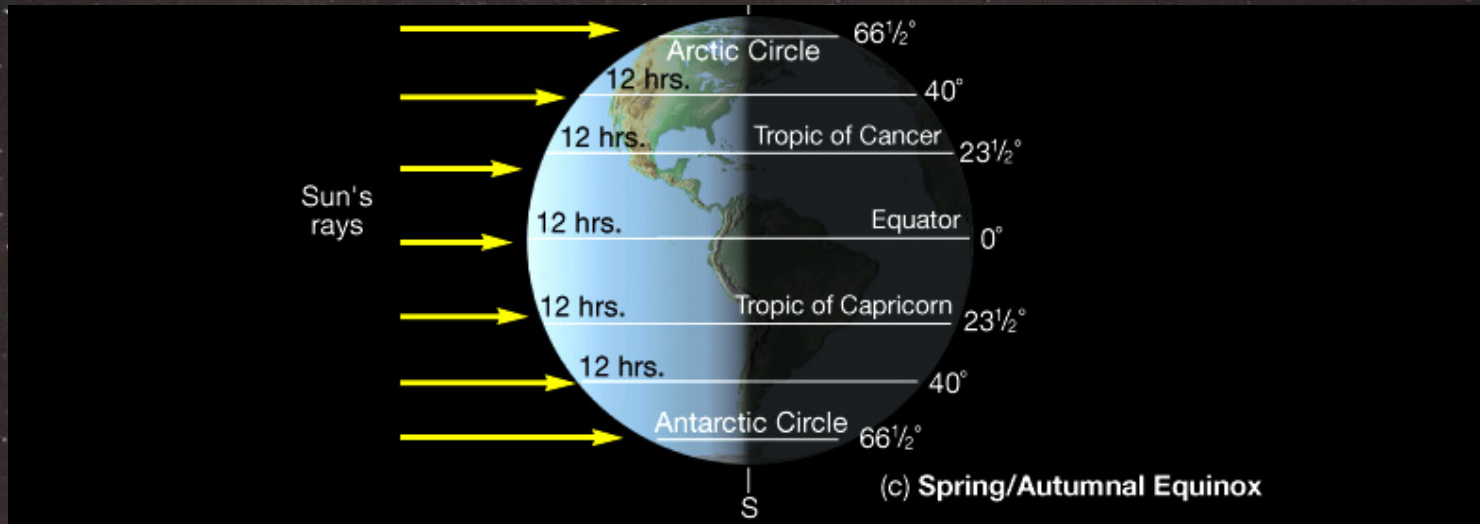
🌍  $12^{\text{h}}$  = Autumnal Equinox ( $\text{M}$ )

🌍  $18^{\text{h}}$  = Winter Solstice ( $\text{X}$ )

# Seasons

## ☆ Equinox - sun on Celestial Equator

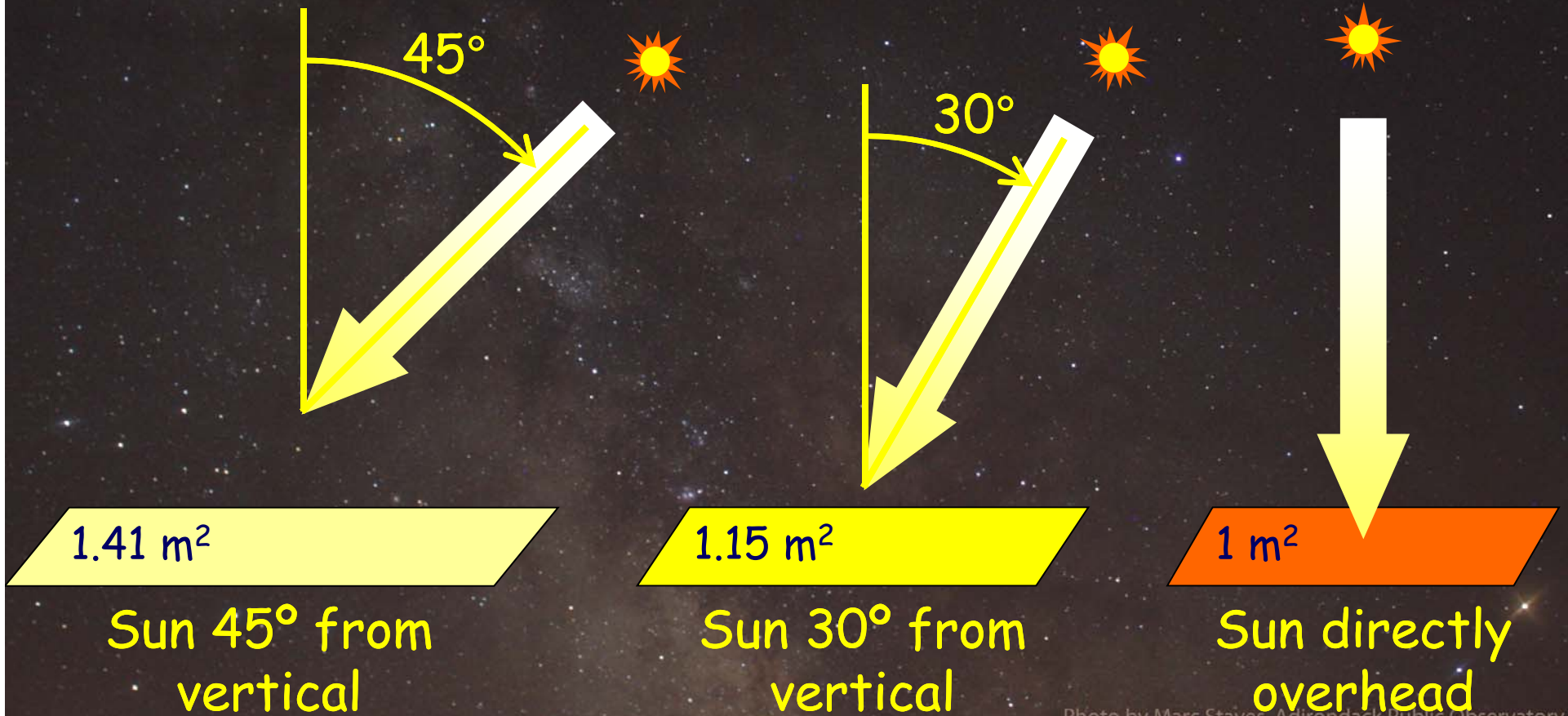
- ☉ Vernal (spring):  $\delta = 0^\circ$ ,  $\alpha = 0^h$ 
  - › Sun crossing equator moving north
- ☉ Autumnal (fall):  $\delta = 0^\circ$ ,  $\alpha = 12^h$ 
  - › Sun crossing equator moving south

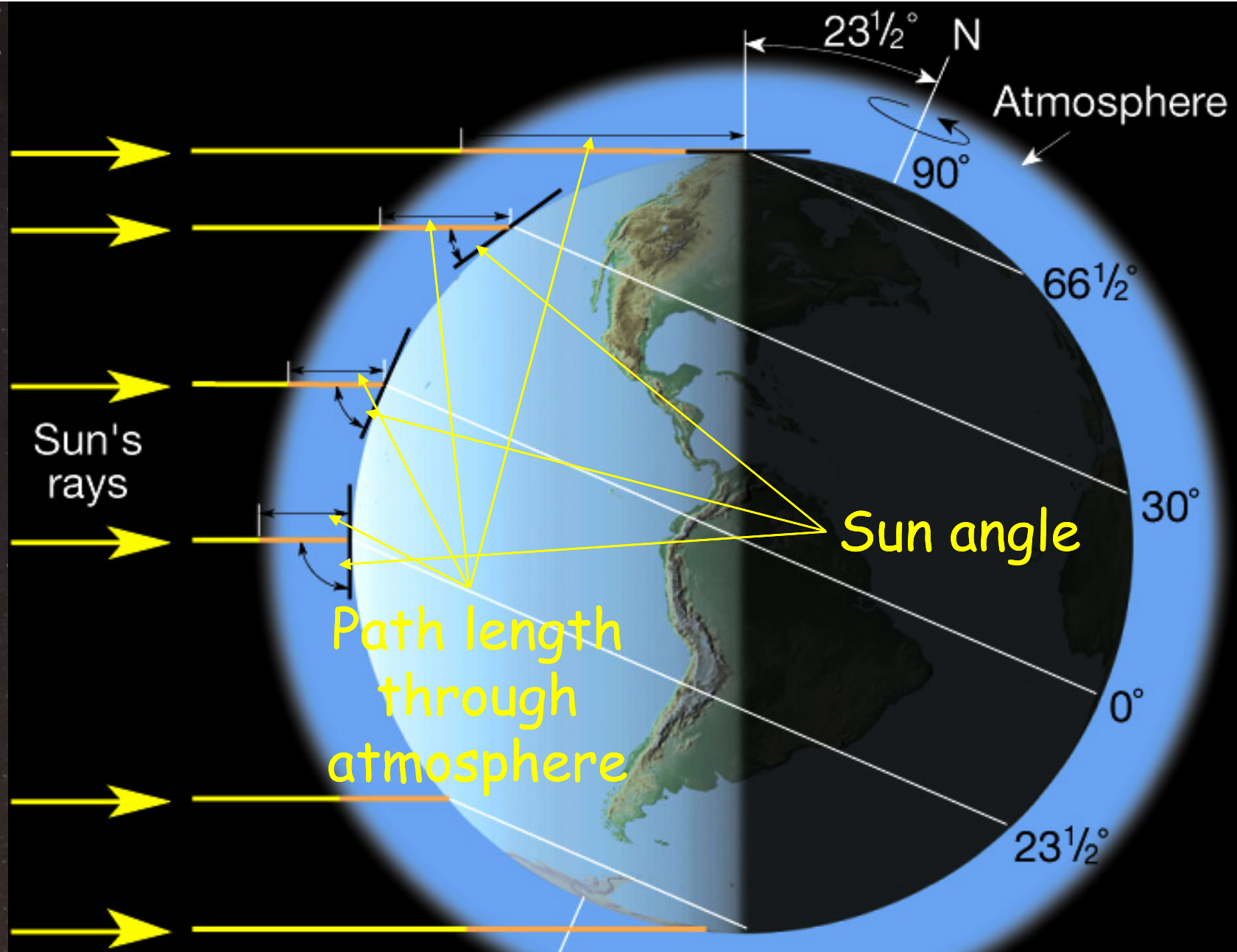




# Seasons

- ☆ Due to changing angle of sunlight
  - 🌍 At low angles, sunlight spreads out
    - › less energy falls on any piece of ground

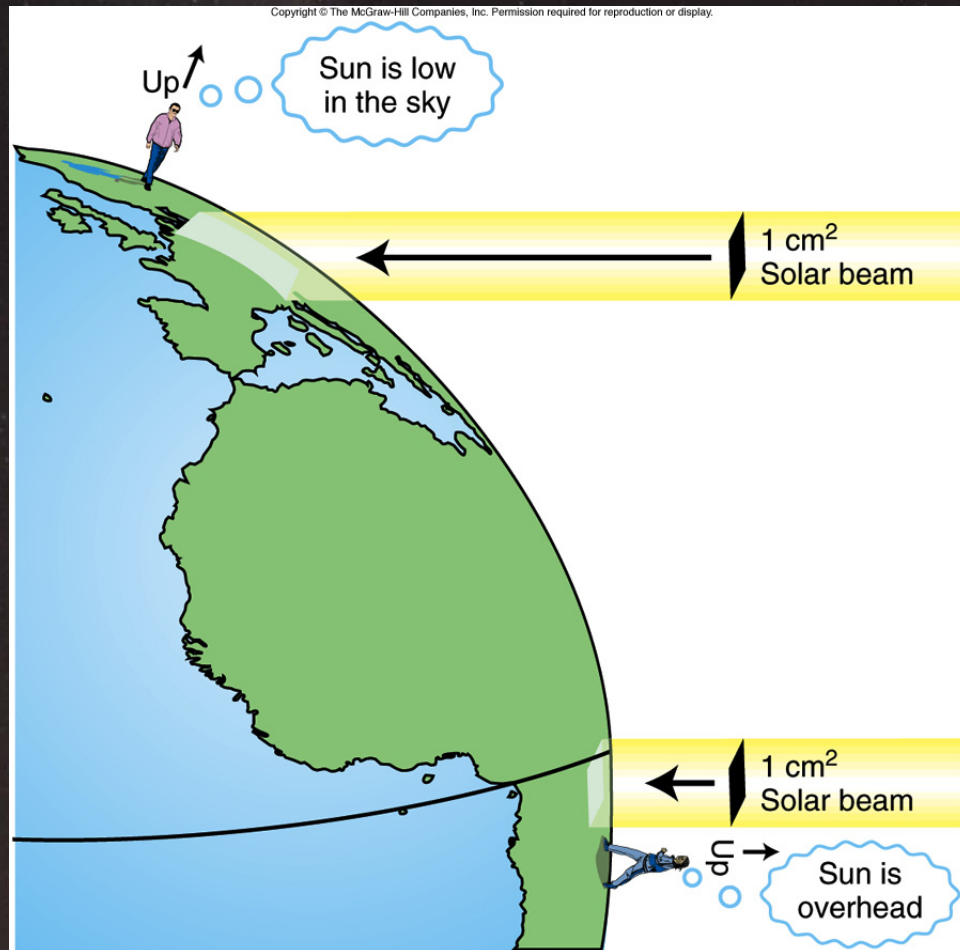




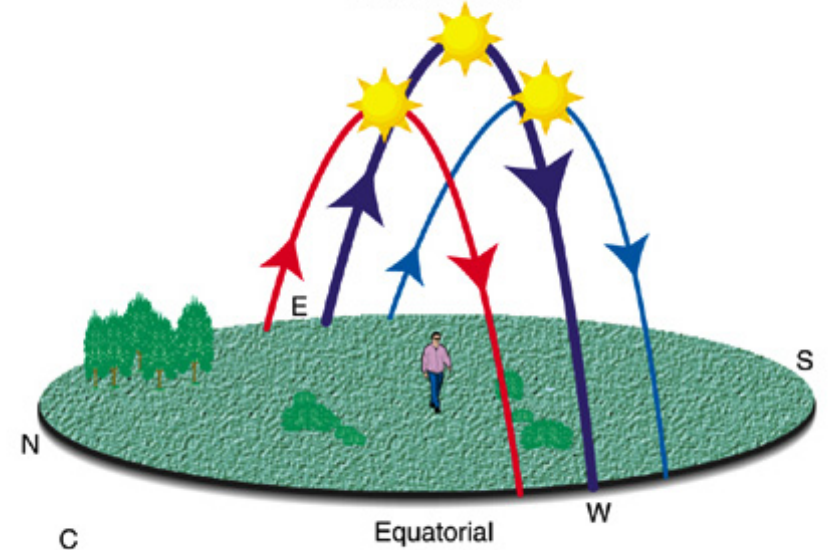
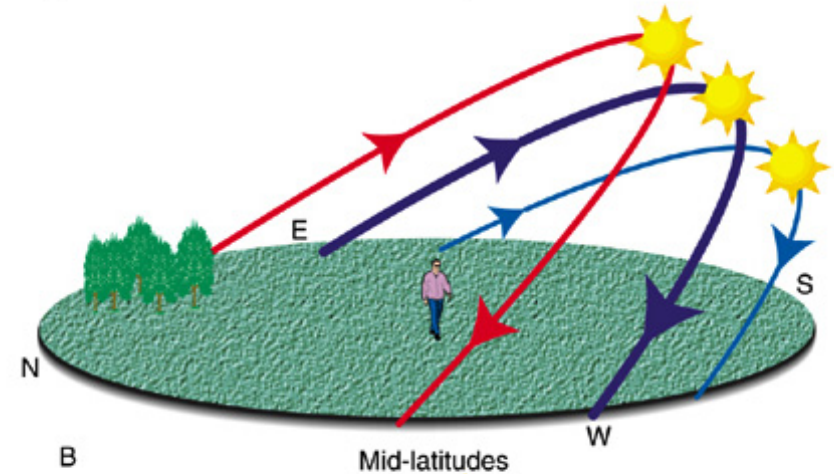
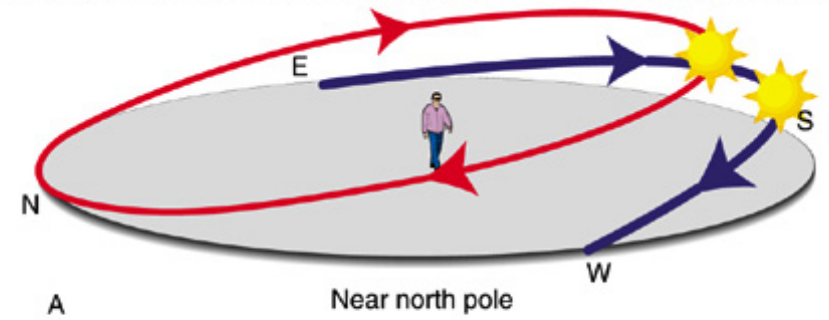
Seasons: Due to changing insolation.

# Seasons

☆ Vary with latitude



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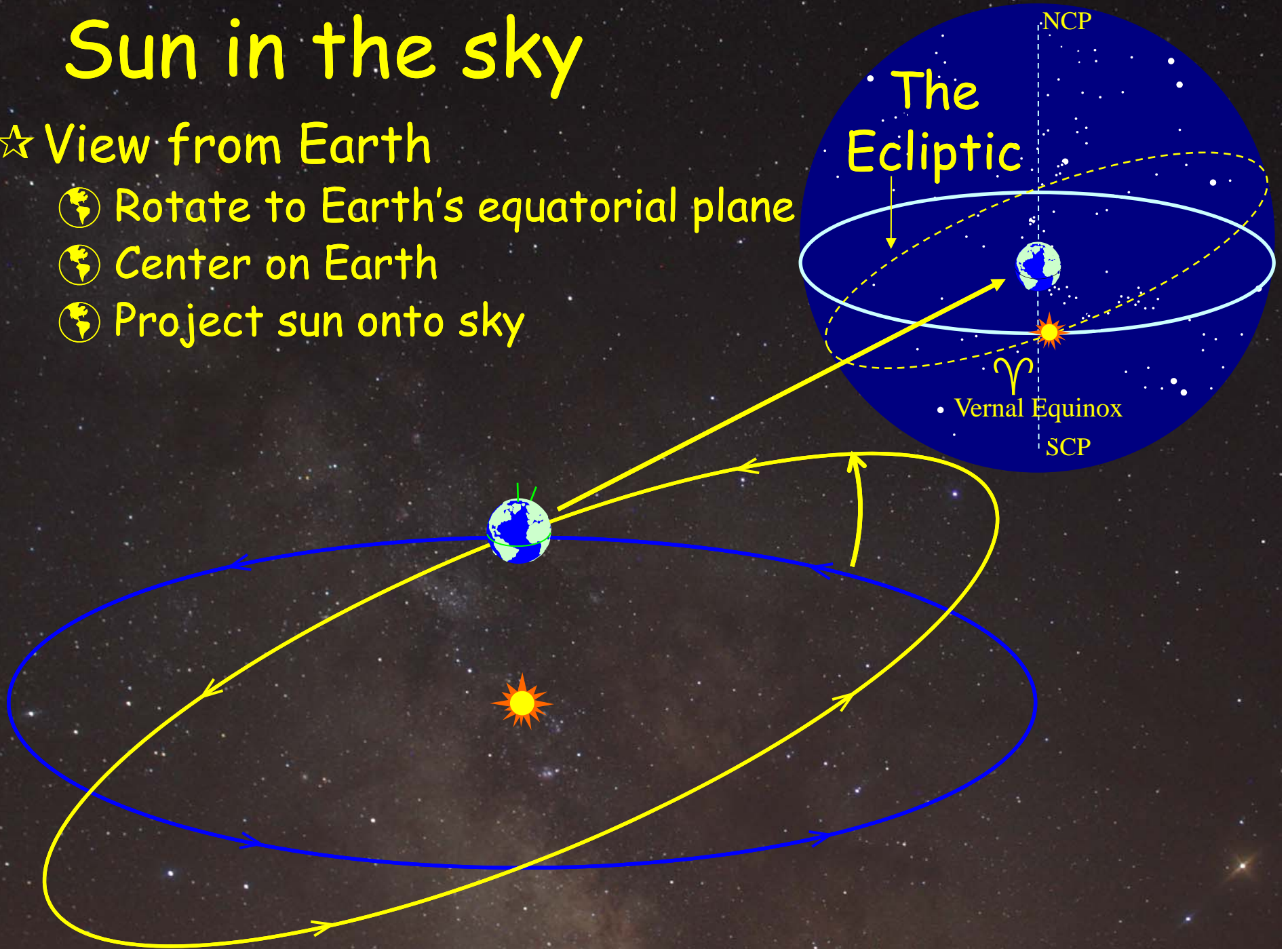


— June    — September, March    — December

# Sun in the sky

## ☆ View from Earth

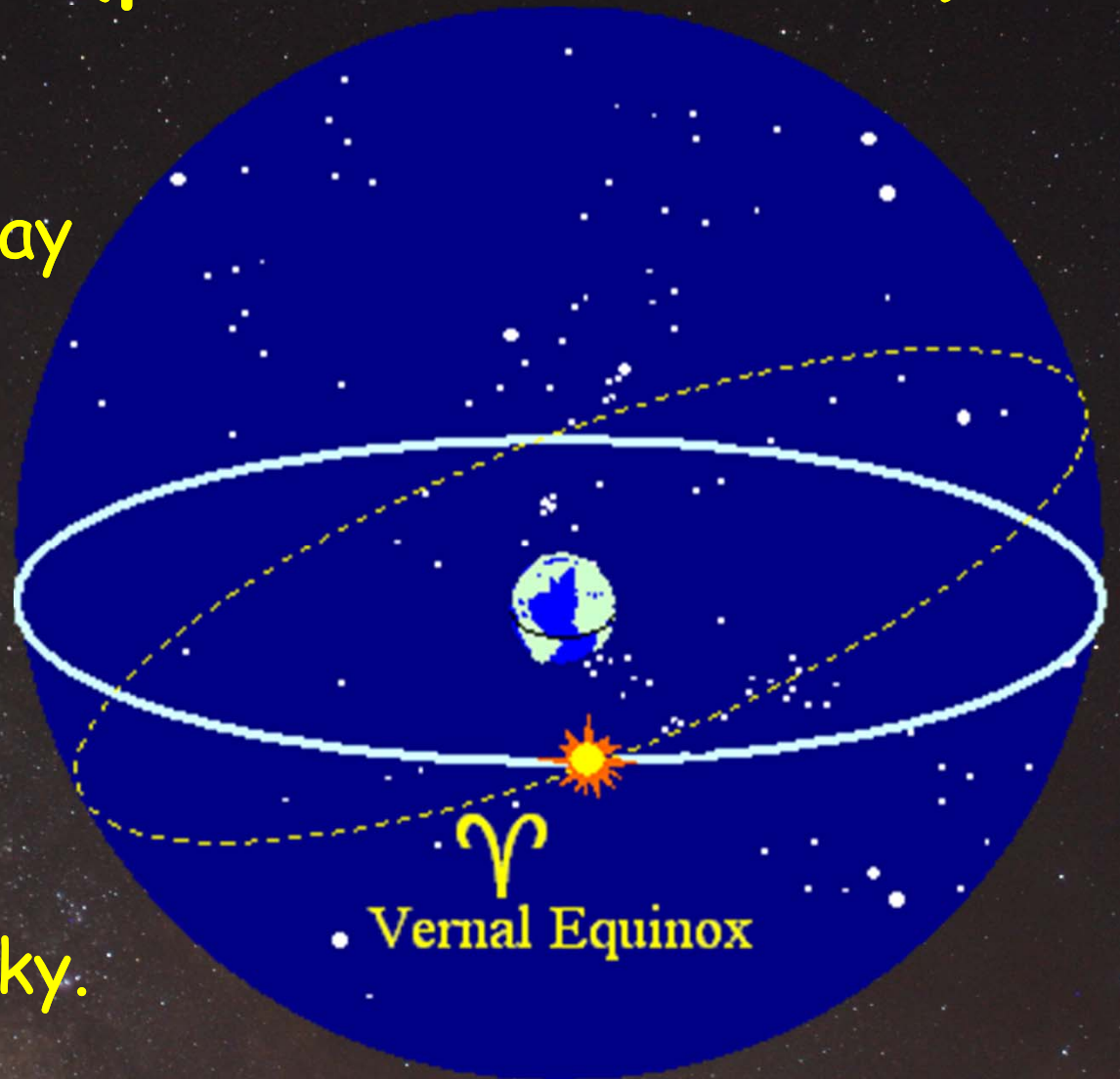
- 🌍 Rotate to Earth's equatorial plane
- 🌍 Center on Earth
- 🌍 Project sun onto sky



# The Ecliptic (path of the sun)

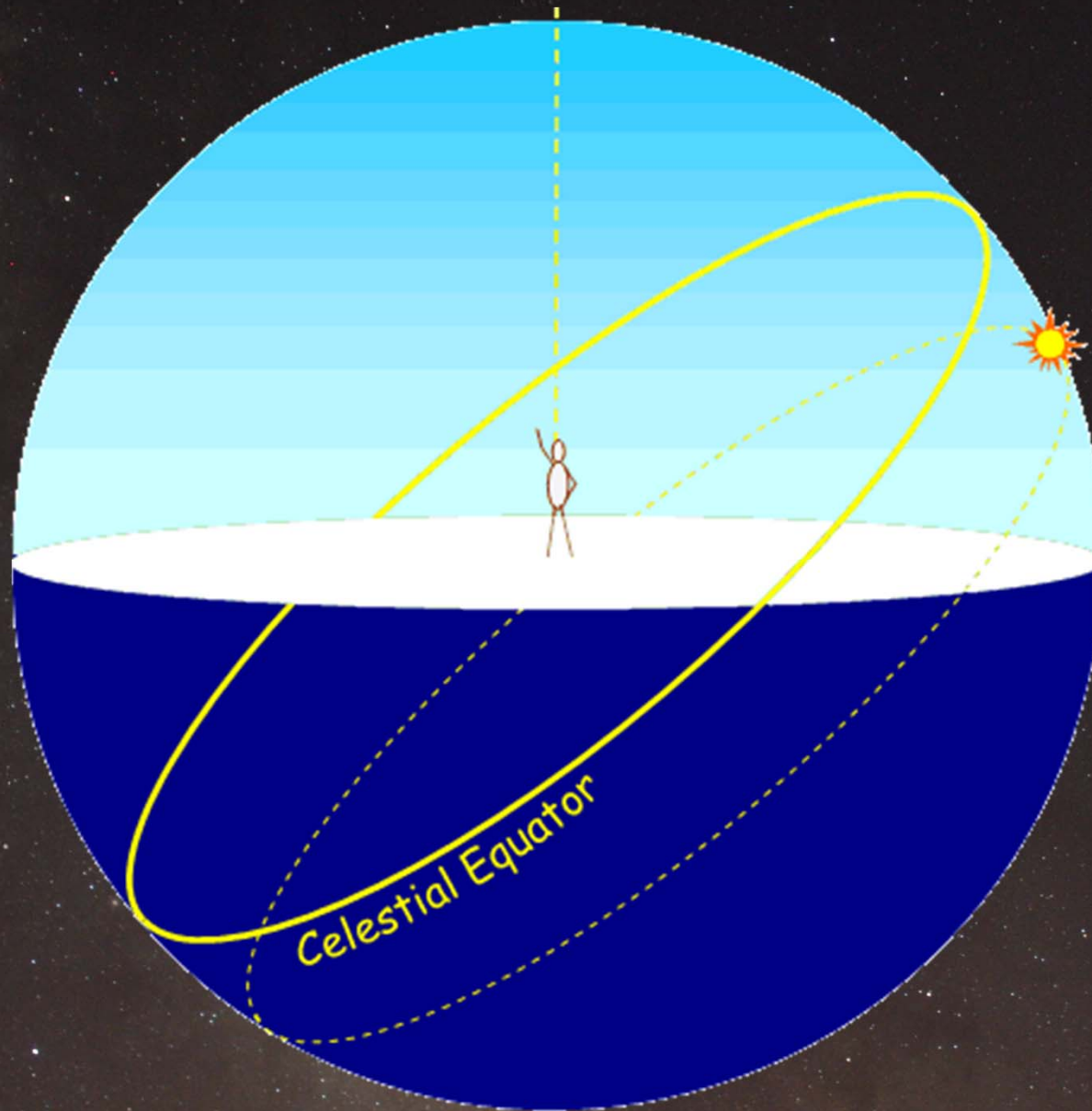
## ☆ View from Earth

- ☉ Sun moves  $\sim 1^\circ$ /day eastward across stars
- ☉ Sun moves north and south in declination
- ☉ Solstices & Equinoxes are positions in the sky.

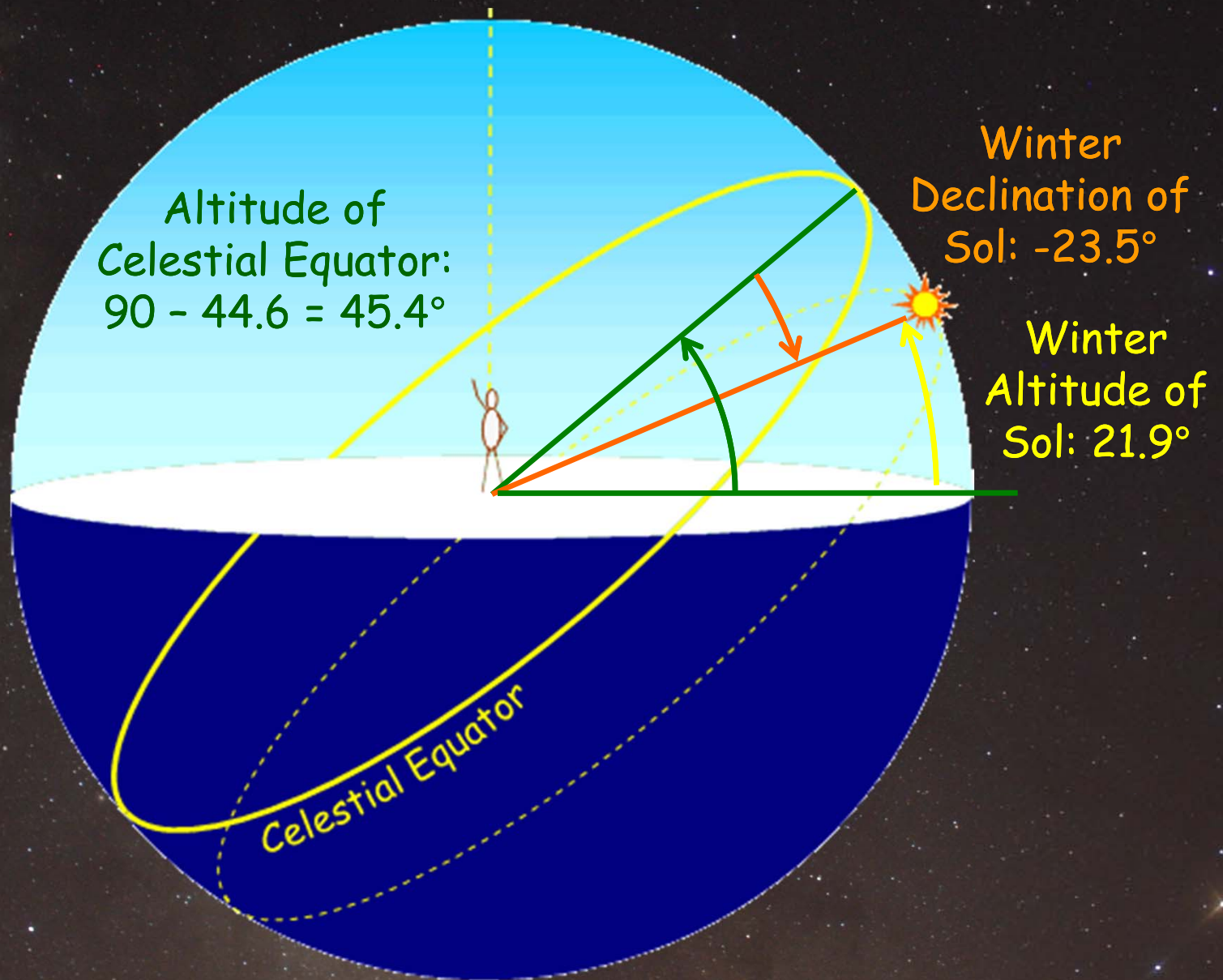


This motion is  
through the YEAR!

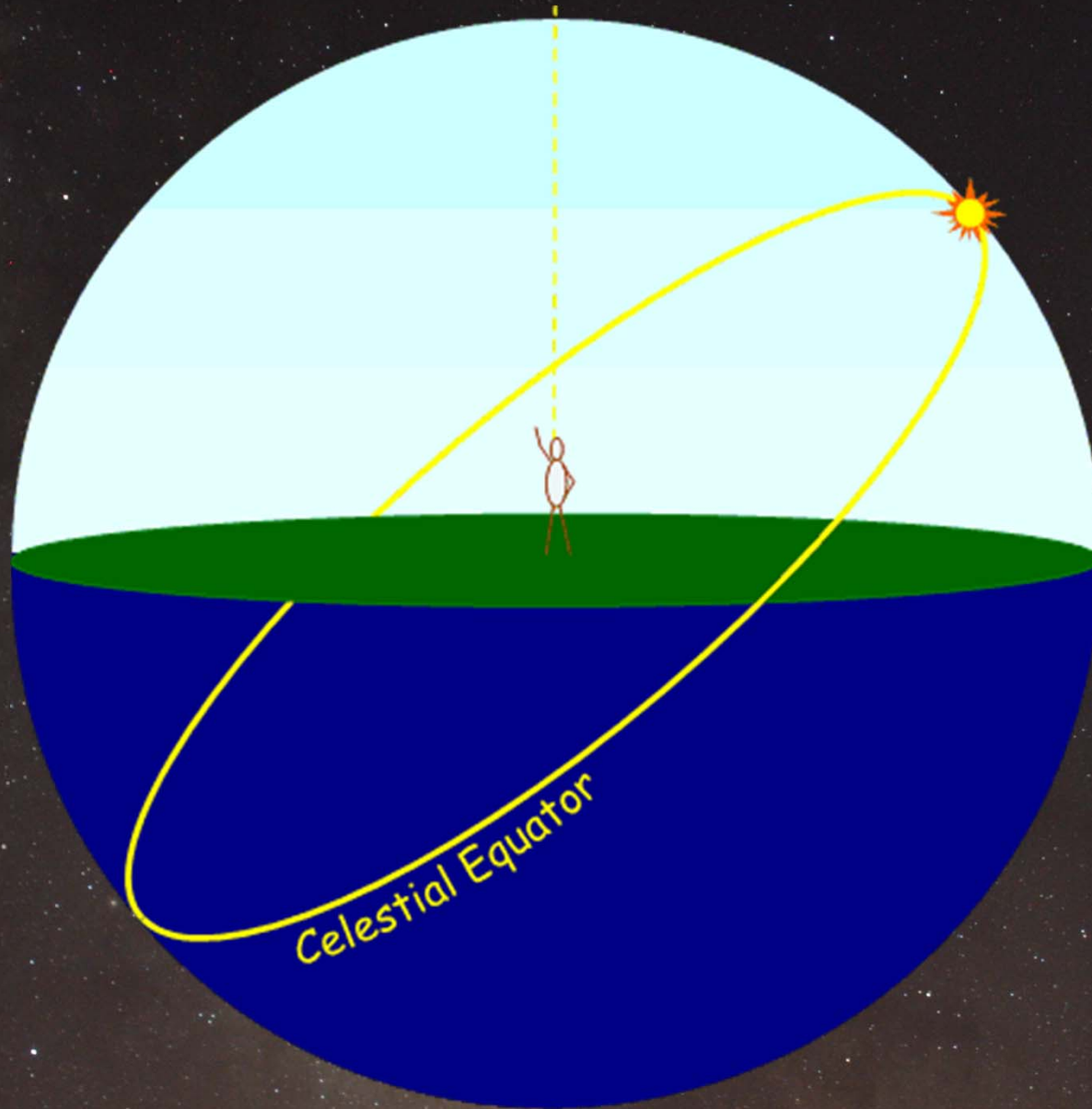
# Sun's path on a winter day



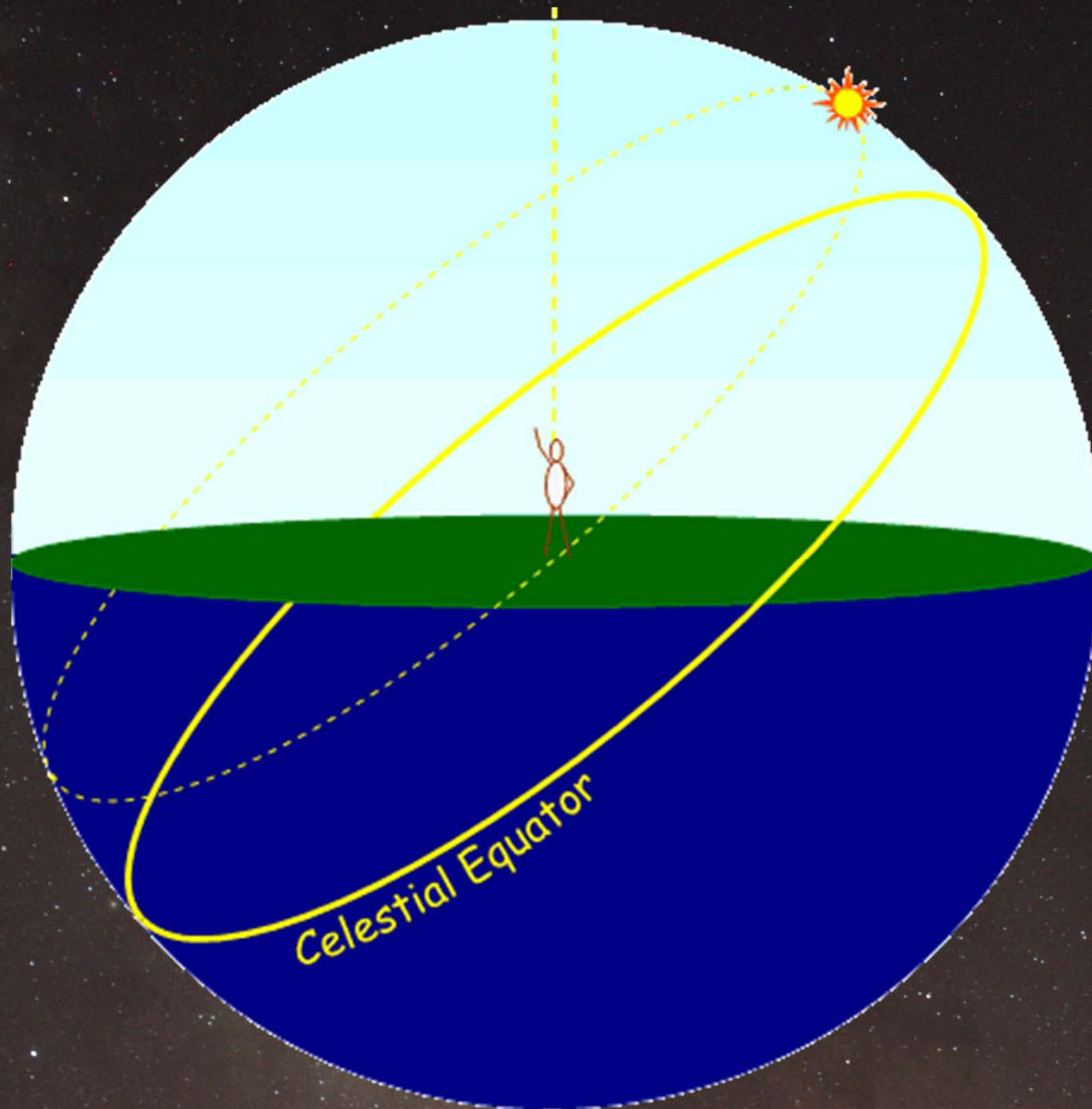
# Sun's path on a winter day



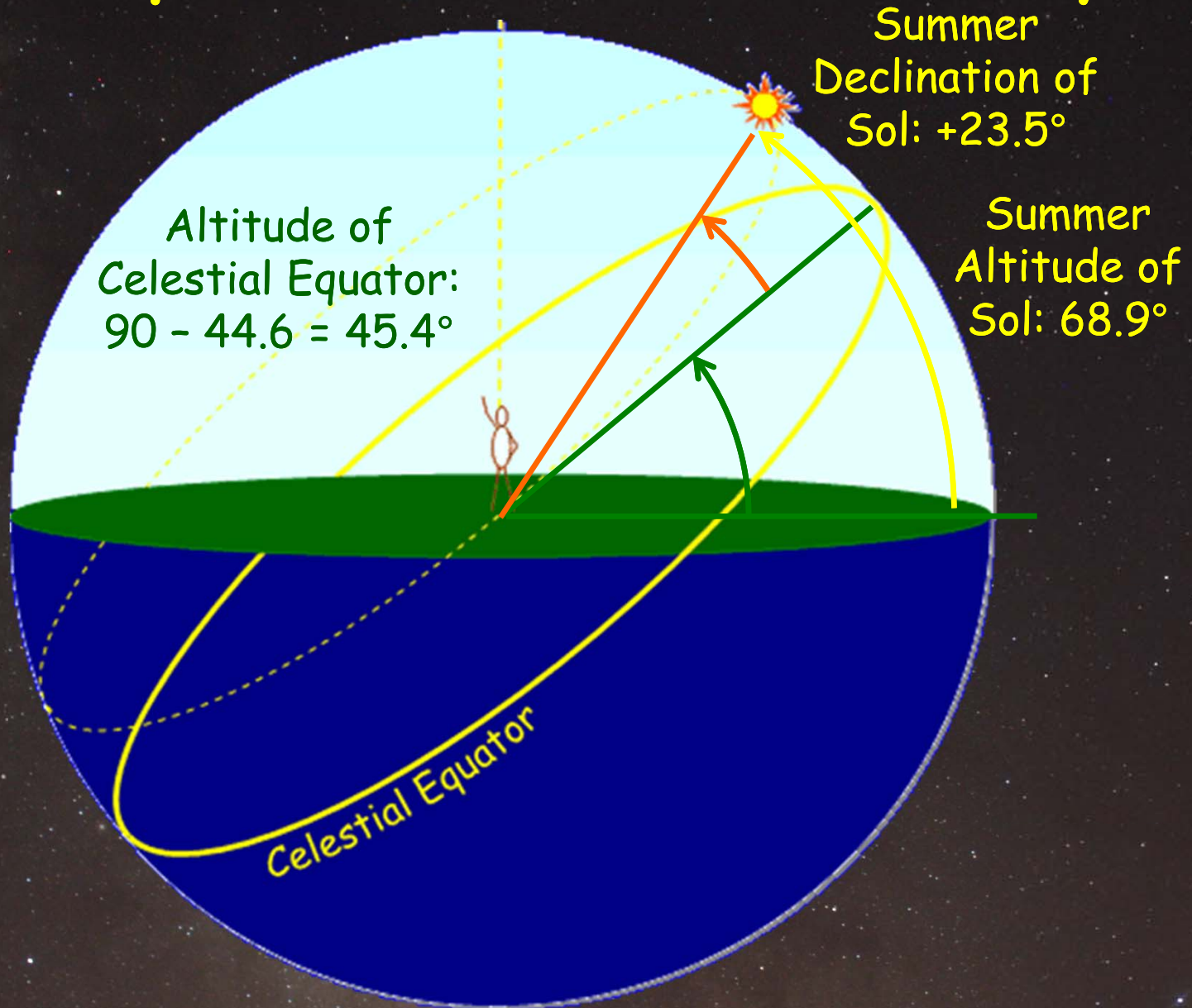
# Sun's path on a fall/spring day



# Sun's path on a summer day



# Sun's path on a summer day



# Clicker Question

At noon on the summer solstice, the sun's maximum altitude in Key West ( $24.6^{\circ}\text{N}$ ) is

A.  $41.9^{\circ}$

B.  $65.4^{\circ}$

C.  $88.9^{\circ}$

Hint:

$$90^{\circ} - 24.6^{\circ} = 65.4^{\circ}$$

Hint: What is  
 $65.4^{\circ} + 23.5^{\circ}$ ?





# Stars in the sky

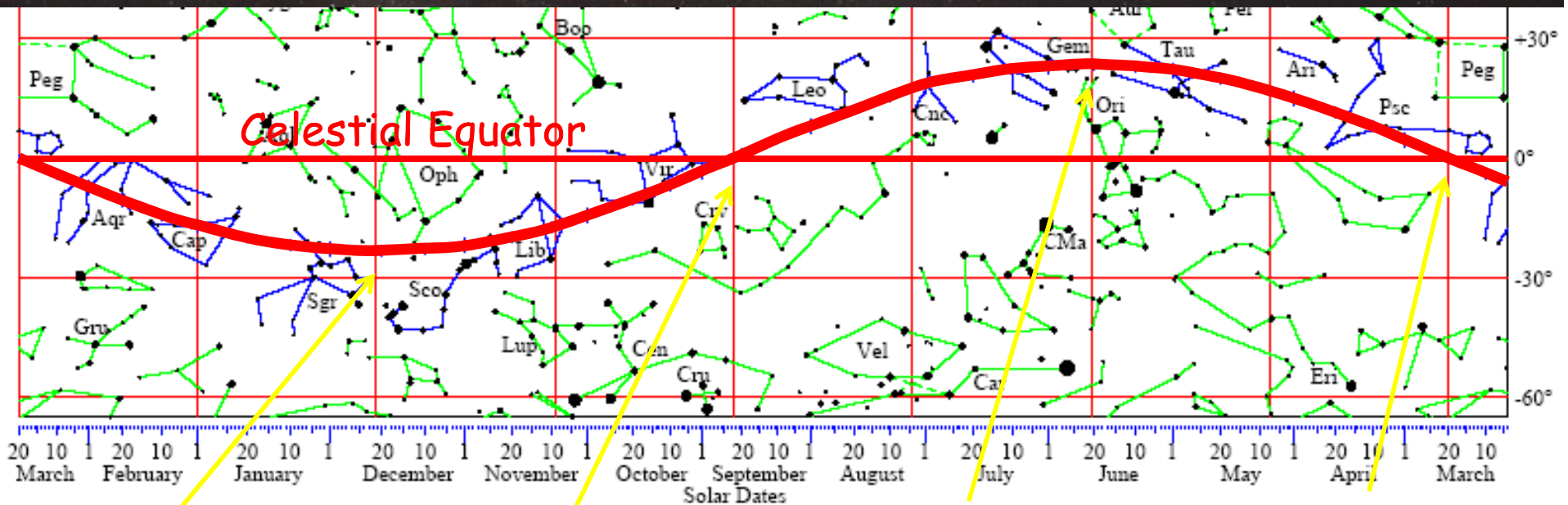
☆ Midnight view from Earth

🌍 Stars opposite sun's position

☾ see opposite season's constellations,

↷ eg. Gemini is a winter sky constellation, Scorpius summer

🌍 Midnight "window" shifts 1° eastward/day



Winter Solstice  
in Sagittarius

Autumnal  
Equinox in Virgo

Summer Solstice  
in Taurus

Vernal Equinox  
in Pisces

# Time

## ☆ Clock Time

- 🌍 the position of the mean sun at TZ center
  - › eg. 12 pm = transit of mean sun (avg. of analemma)
- 🌍 Mean Solar Day = 24:00:00 (hours:min:sec of time)

## ☆ Solar Time

- 🌍 the position of the sun wrt the observer
  - eg. Noon = sun transits
- 🌍 Solar Day varies as shown by analemma

## ☆ Sidereal Time

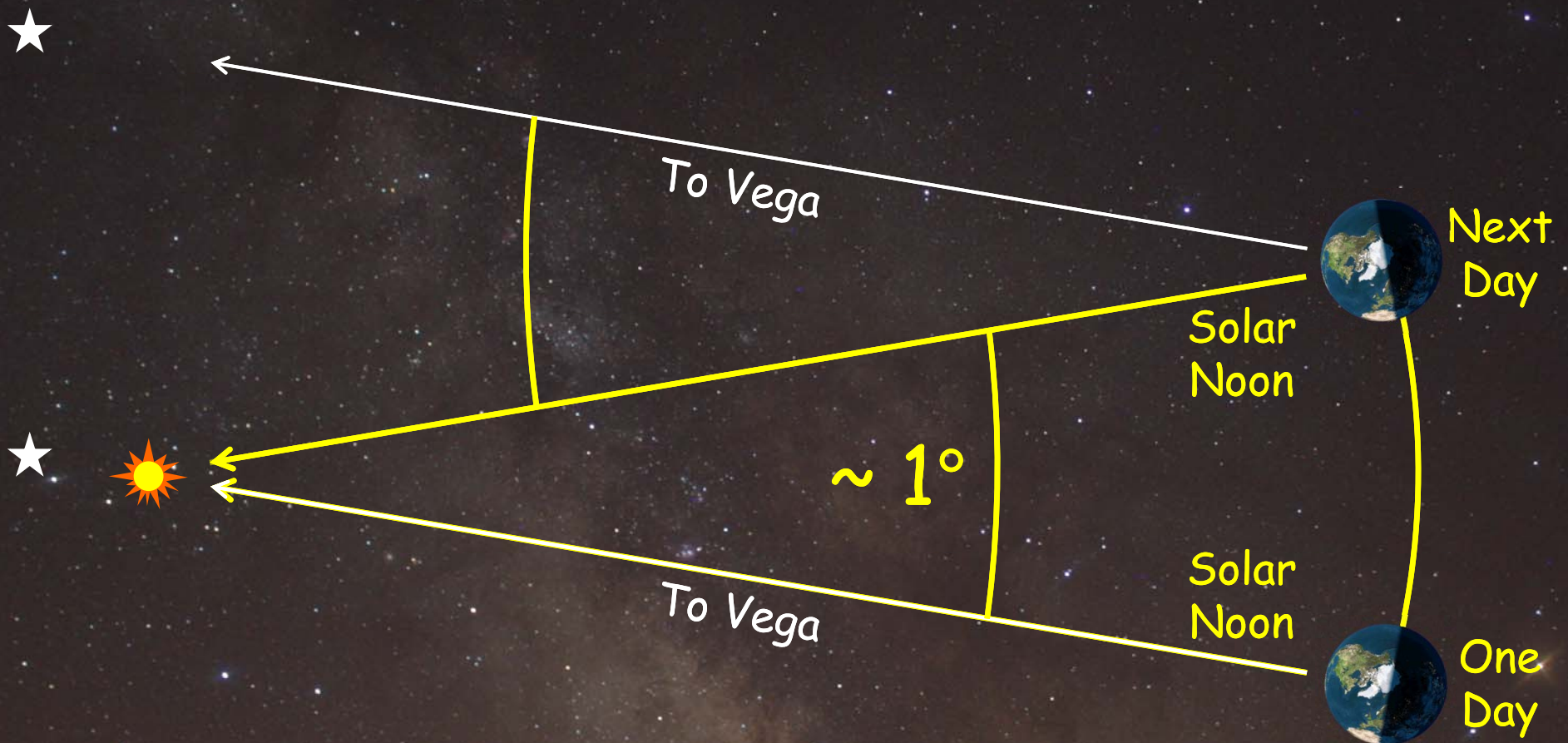
- 🌍 the position of  $\Upsilon$  wrt the observer
  - › eg. 0<sup>h</sup> Local Sidereal Time (LST) =  $\Upsilon$  transits
  - › Sidereal time = R.A. on the meridian
- 🌍 Sidereal Day = 23:56:00

# The Sidereal Day

🌍 Earth turns  $360^\circ$  with respect to stars

    ) eg. Vega transit to Vega Transit

🌍 23:56:00



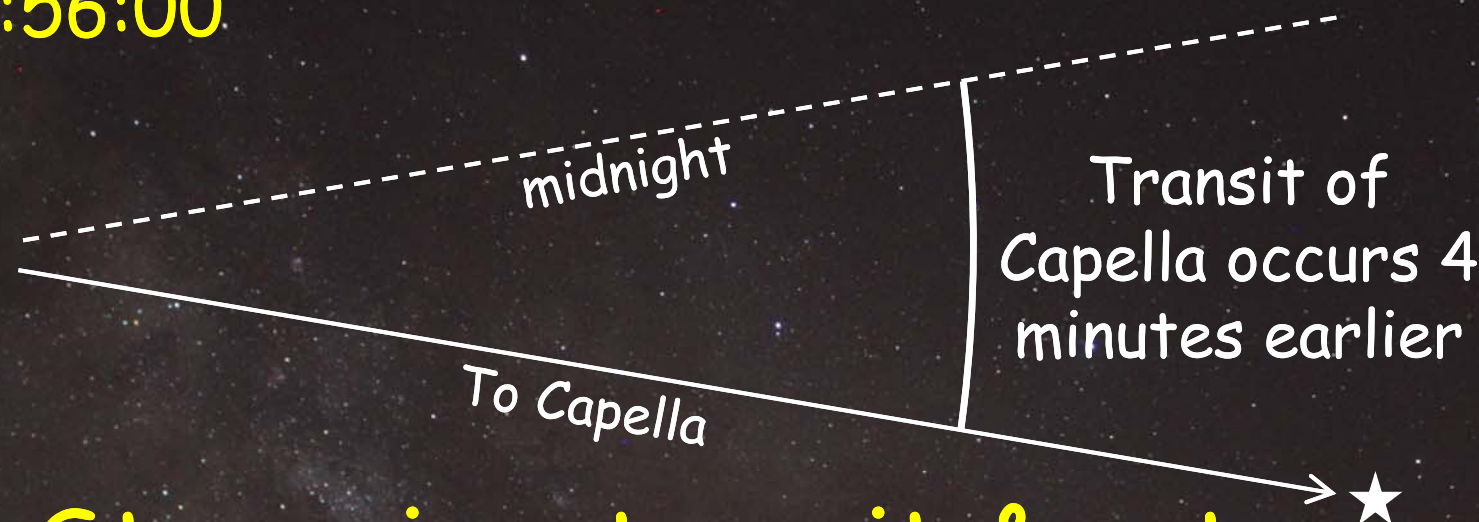


# The Sidereal Day

🌍 Earth turns  $360^\circ$  with respect to stars

    ) eg. Capella transit to Capella Transit

🌍 23:56:00

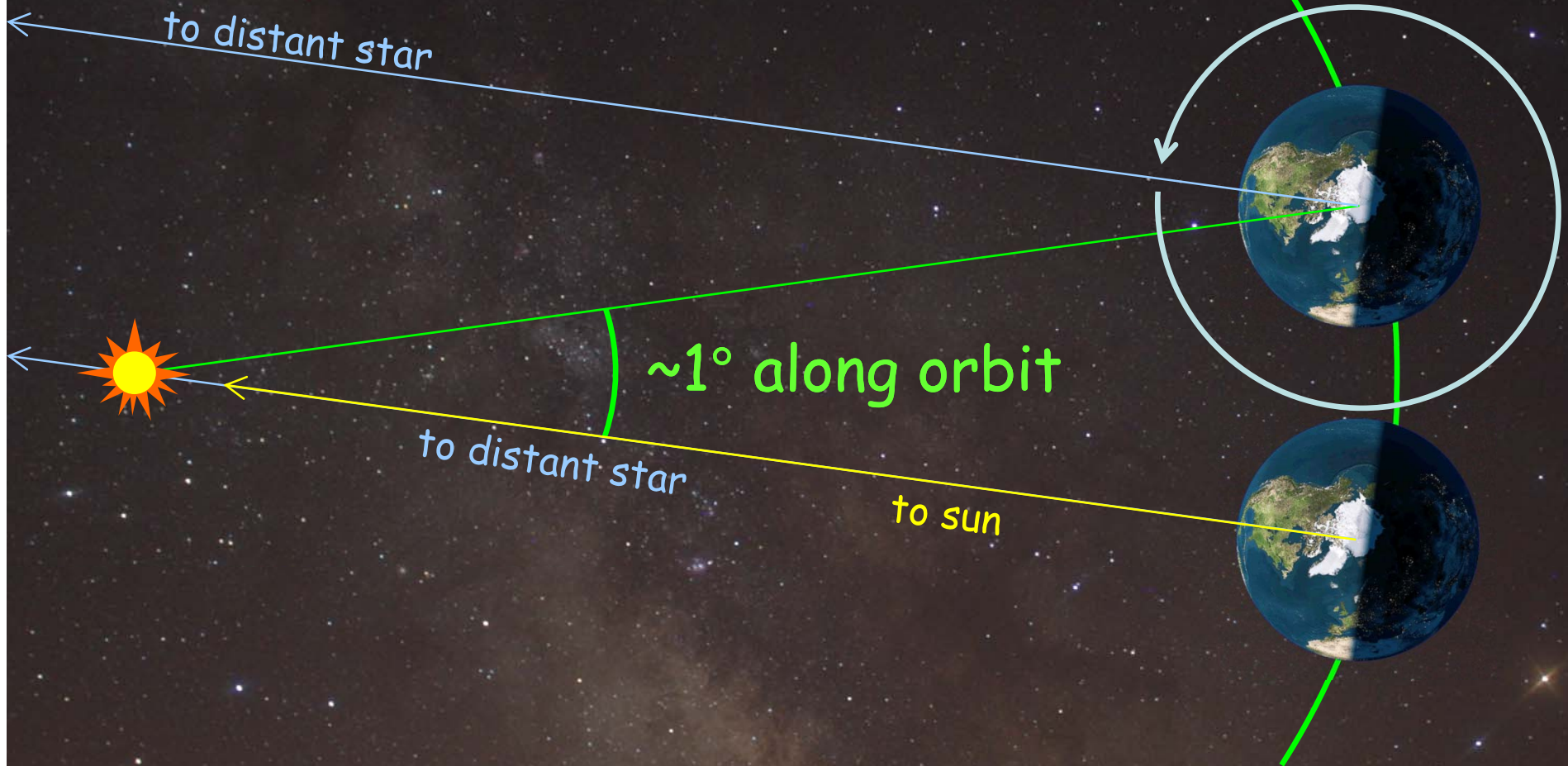


Stars rise, transit & set  
four minutes earlier each  
day!



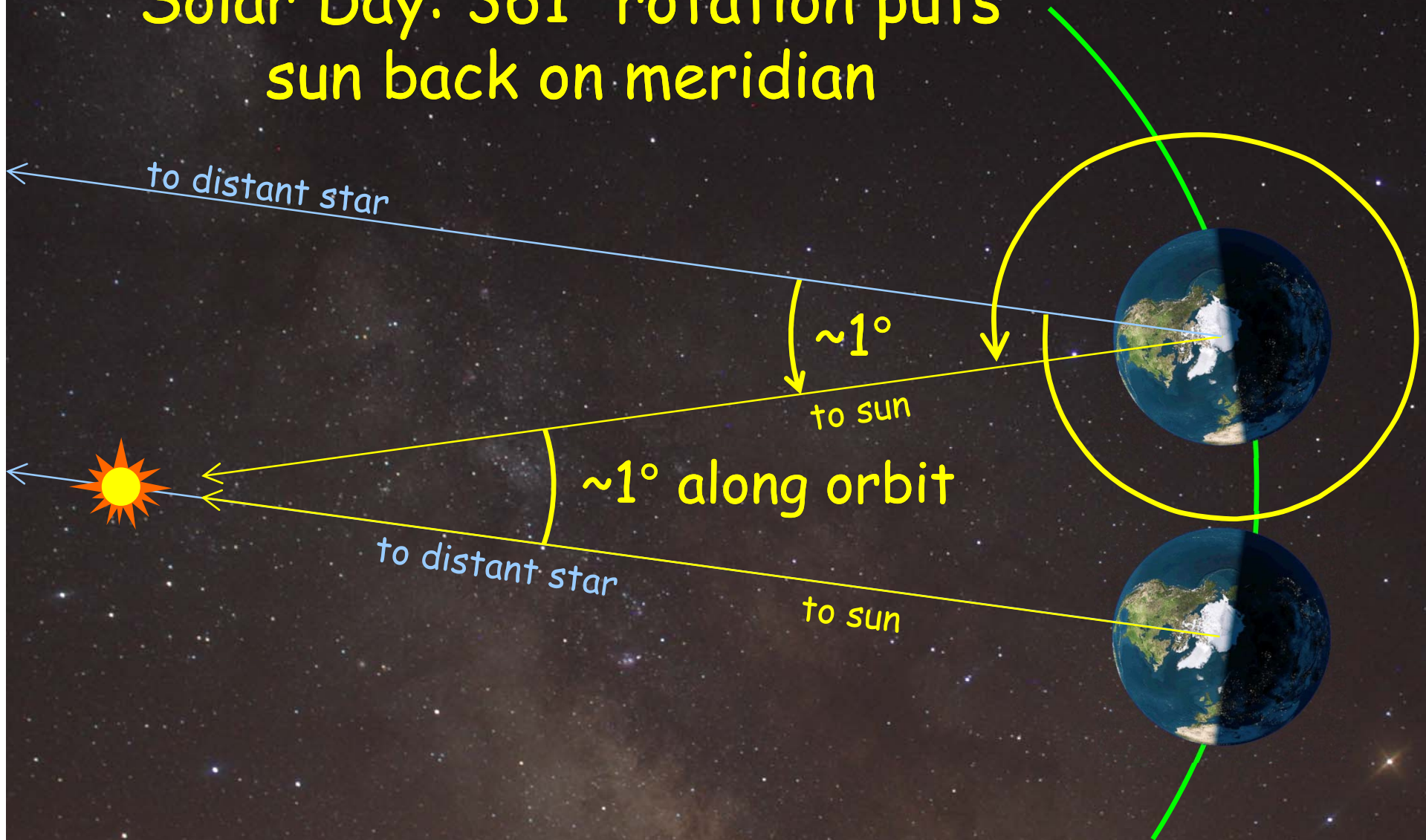
# The Sidereal Day

Sidereal Day: 360° rotation puts star back on meridian



# The Solar Day

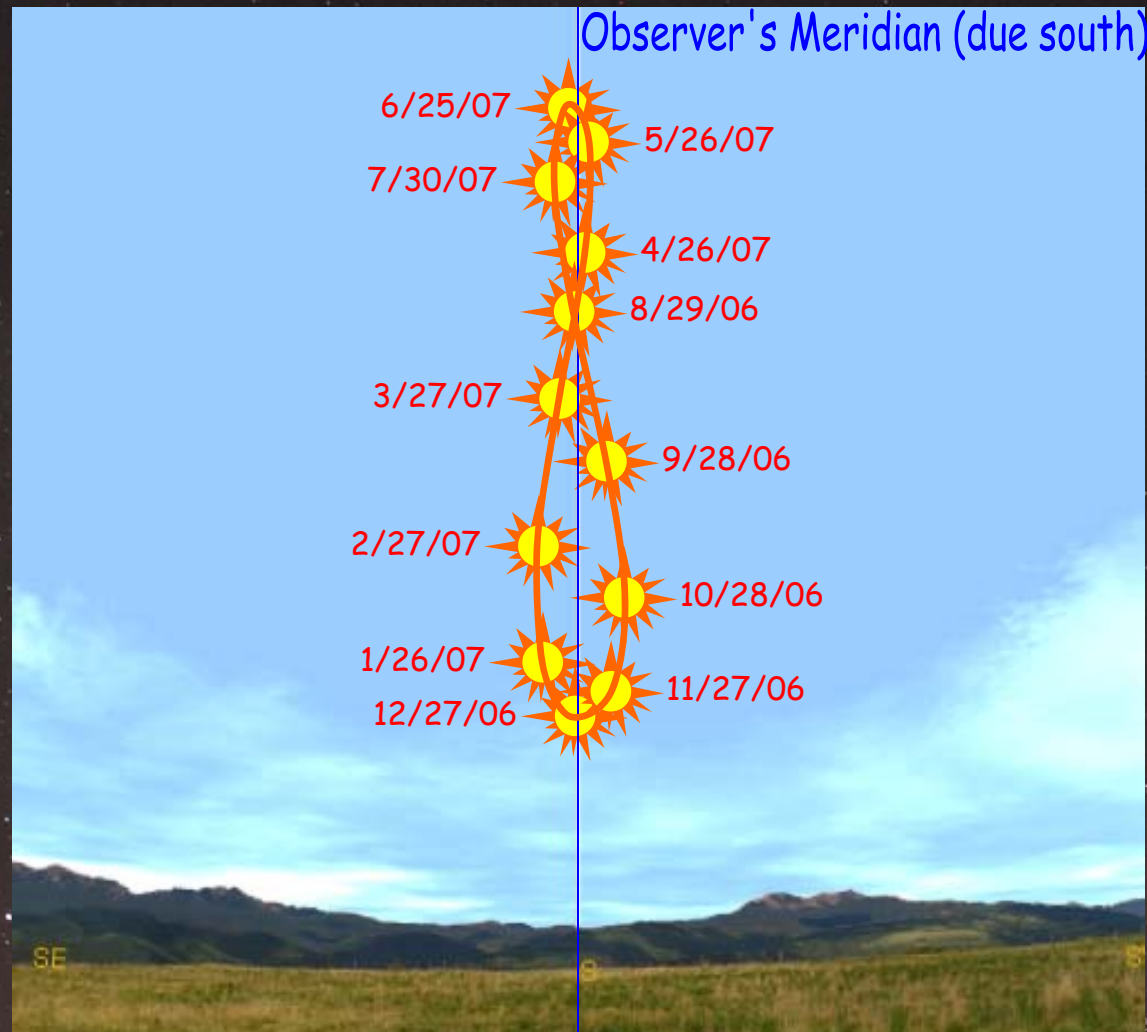
Solar Day:  $361^\circ$  rotation puts sun back on meridian



# The Sun at Noon

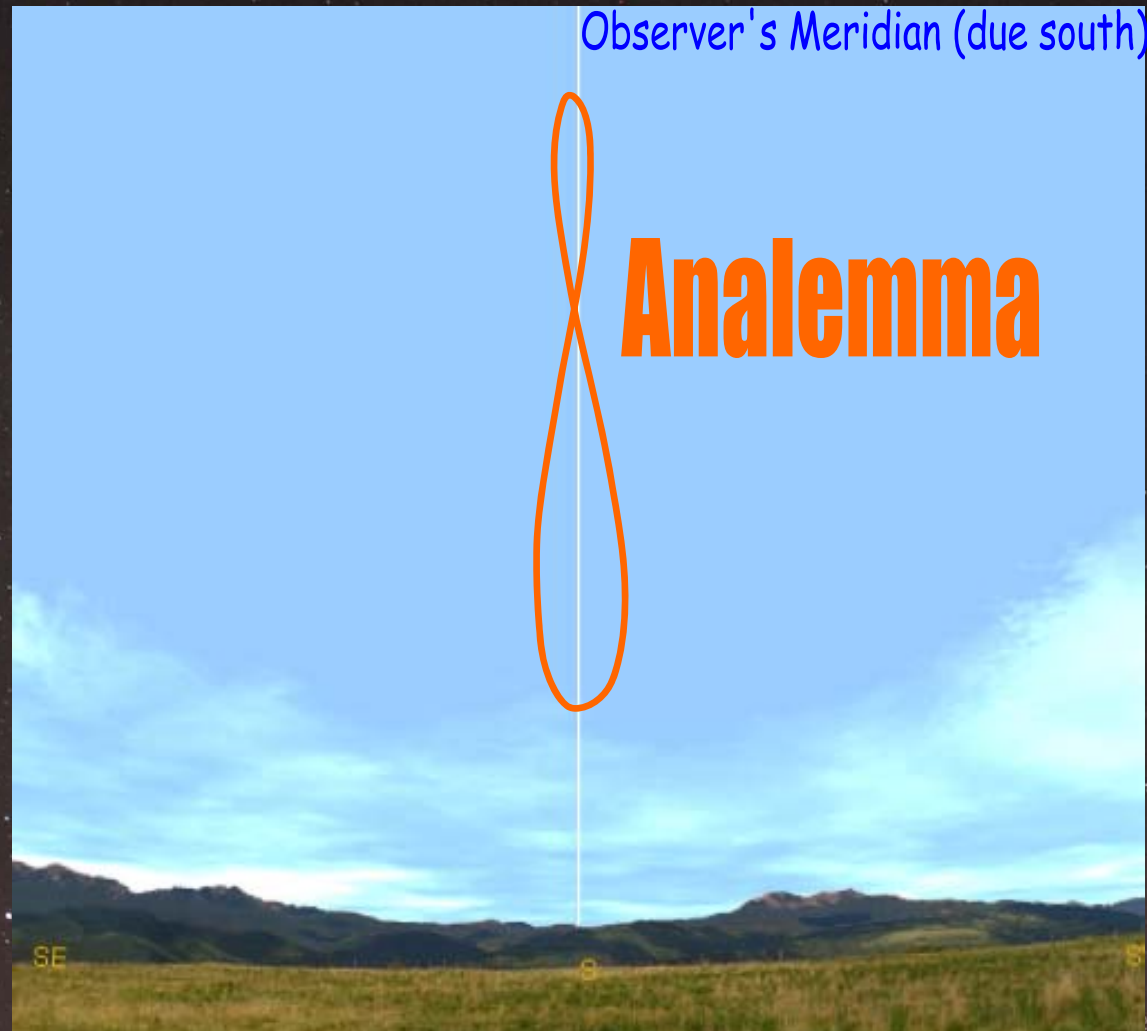
☆ Noon  $\Rightarrow$  Sun on meridian

☆ Sun's position varies: the Analemma



# The Sun at Noon

- ☆ Noon  $\Rightarrow$  Sun on meridian
- ☆ Sun's position varies: the Analemma



# The Analemma

## ☆ Position of true sun at clock noon

### 🌍 Clock Noon

› 12:00 pm in a  
24:00:00 day

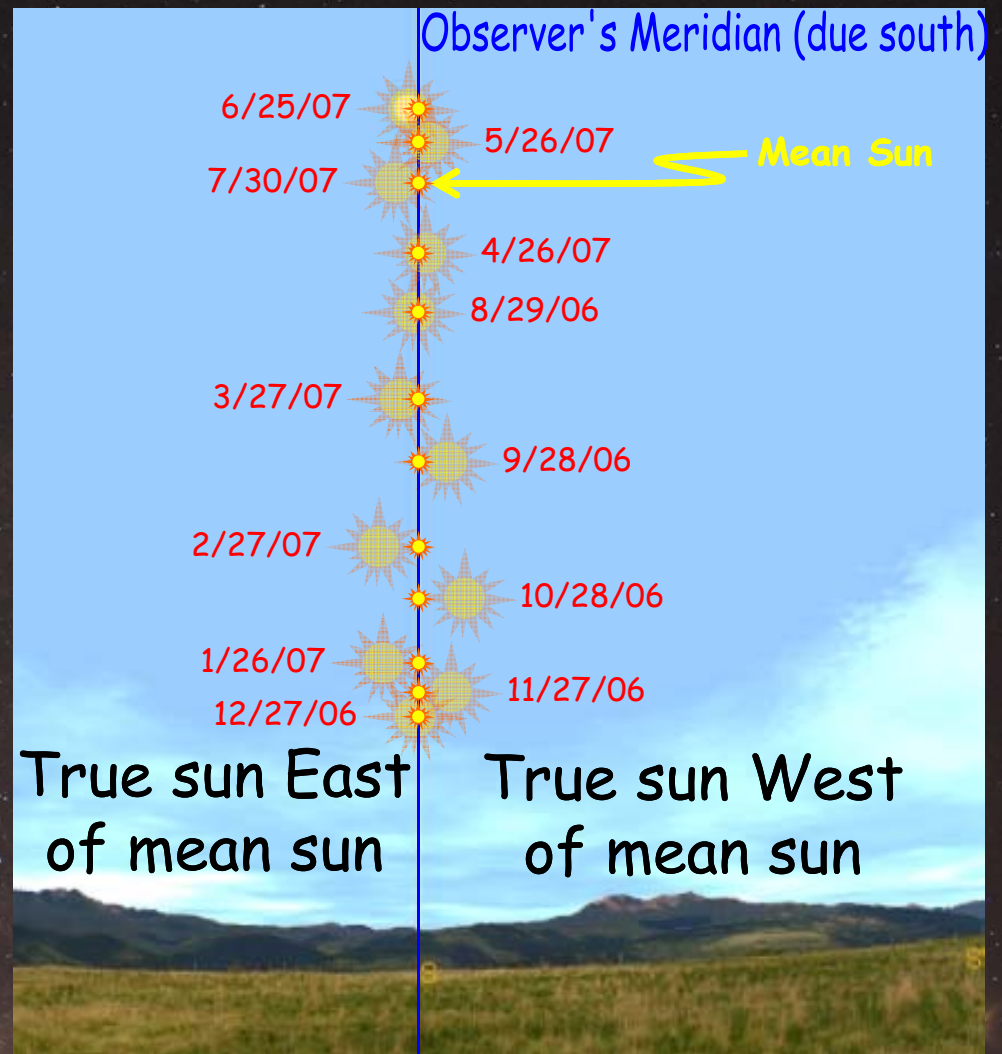
› Position of Mean Sun  
at noon

### 🌍 True Sun's Position

› varies due to Sun's  
speed along path

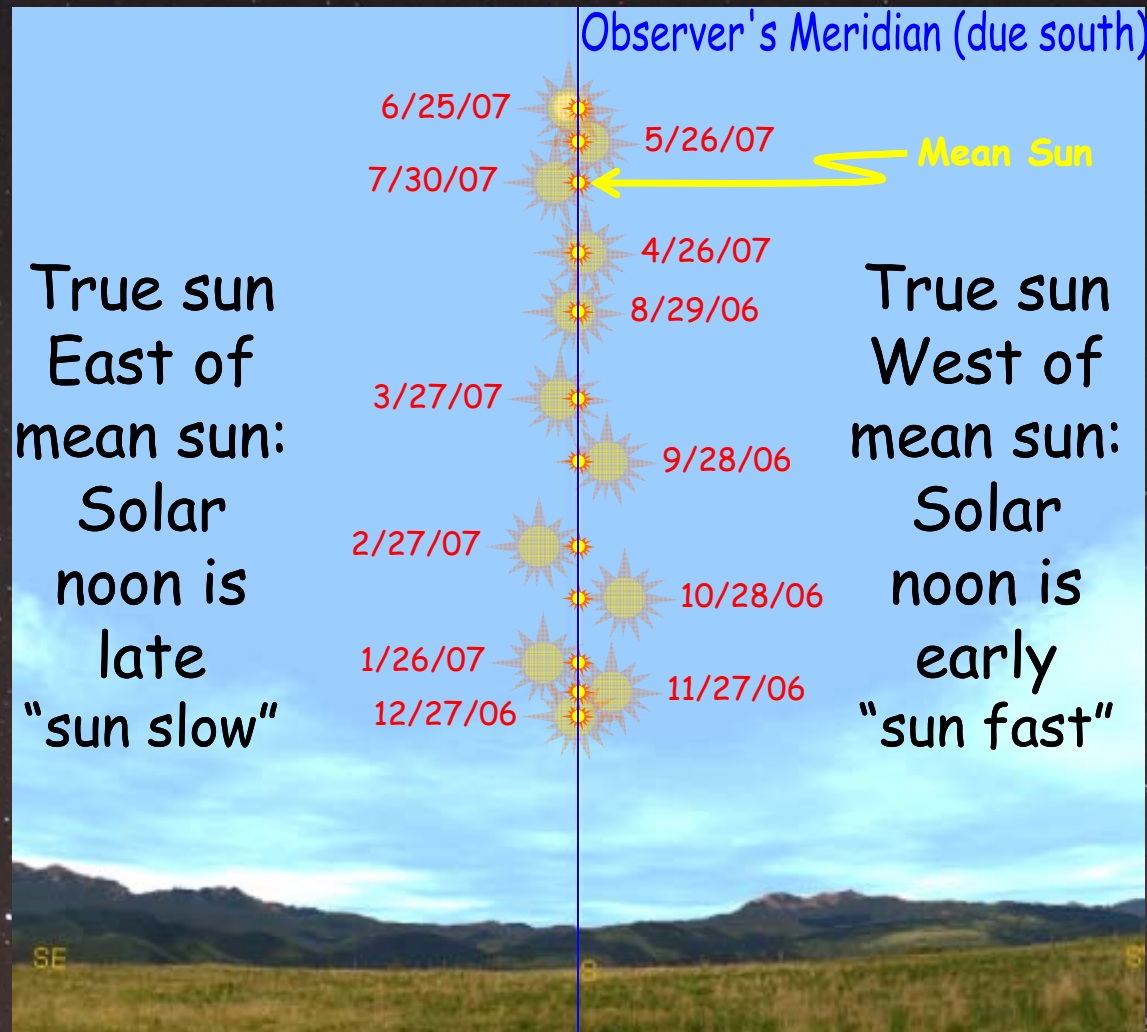
∩ varies due to elliptical  
path

∩ varies due to tilted  
path



# Mean Sun & True Sun

- ☆ Mean sun on meridian defines clock noon
- ☆ True sun on meridian defines solar noon



# Solar Noon Today (9/12/17)

## ☆ Potsdam ( $44^{\circ} 40' \text{ N}$ , $75^{\circ} 00' \text{ W}$ )

🌍 Standard time of solar noon = 11:56:13 am

🌍 Daylight time of solar noon = 12:56:13

## ☆ Canton ( $44^{\circ} 36' \text{ N}$ , $75^{\circ} 10' \text{ W}$ )

🌍 Standard time of solar noon = 11:56:53 am

🌍 Daylight time of solar noon = 12:56:53

🌍 40 seconds later than Potsdam

› Earth turns  $1^{\circ}$  in 4 minutes

⇒ Earth turns  $15'$  in 1 minute

⇒ Earth turns  $10'$  in 40 seconds!!

⇒ Celestial events in Canton

40 seconds later than in Potsdam!!

# Doing the Math

## ☆ Mean Sun

🌍 Projection of sun onto Celestial Equator

› moves  $360^\circ$  in one year (365.242191 days)

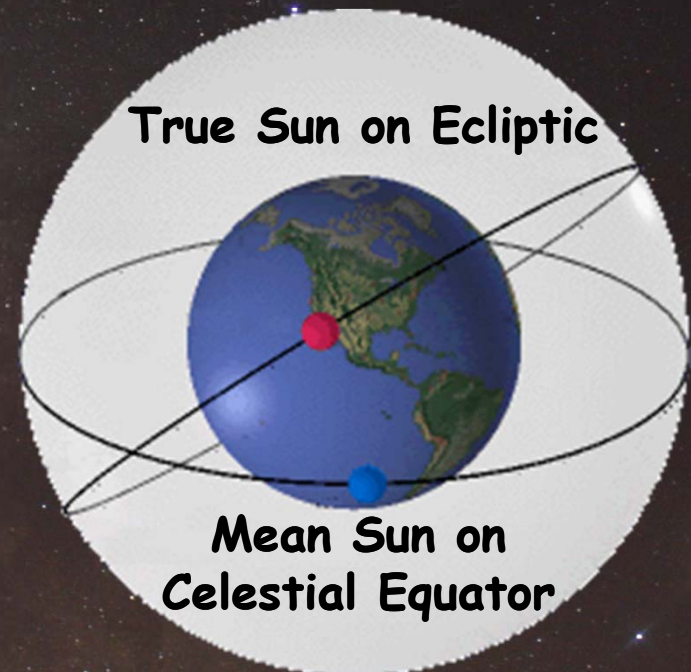
$$V_{\text{Mean Sun}} = \frac{360^\circ}{365.242191 \text{ days}} = 0.985647356^\circ/\text{day}$$

## ☆ True Sun

🌍 speed varies due to

› Sun's changing Declination

› Elliptical orbit



# Position of Sunrise & Sunset

- ☆ Azimuth of rising depends on  $\delta$

$$A_{\text{rise}} = \cos^{-1} \left( \frac{\sin \delta}{\cos \lambda} \right) \text{ degrees}$$

- ☆ Sunrise appears to move along horizon

🌍 original calendar!

eg. Stonehenge, Machu Pichu, Woodhenge (Illinois)



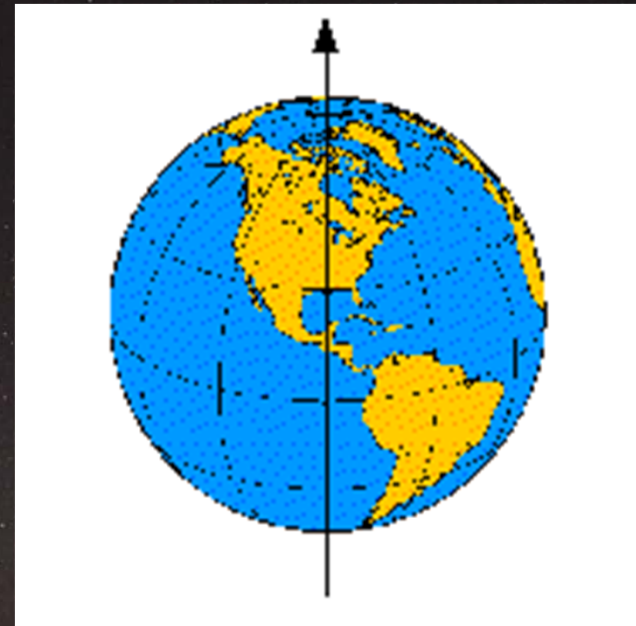
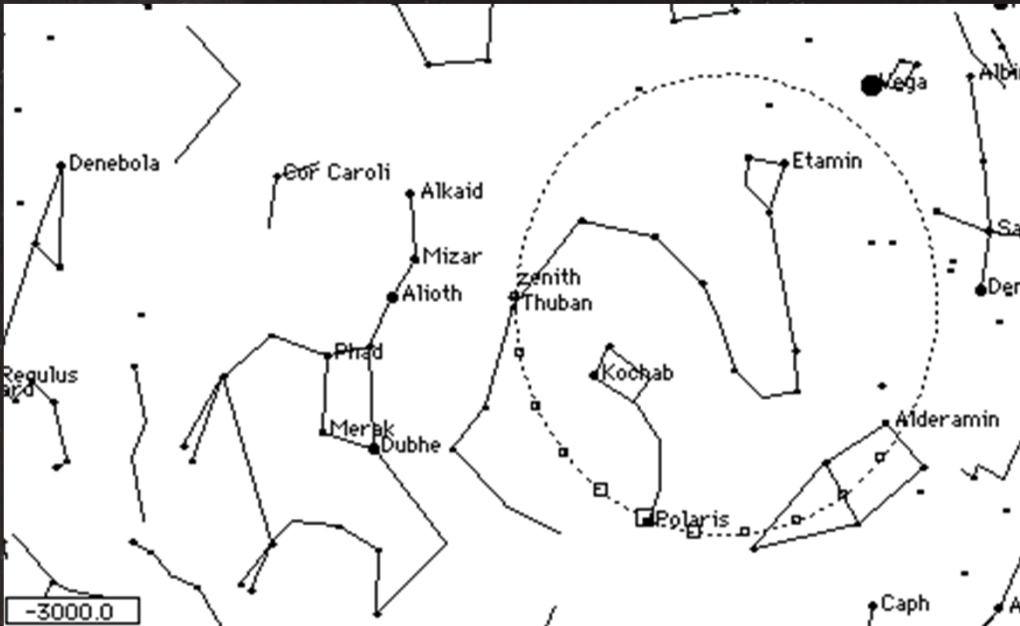
# Position of Sunset

12/9/9 3:40 pm EST  
40 minutes before  
sunset



# Precession

☆ Earth's axis wobbles over 26,000 years

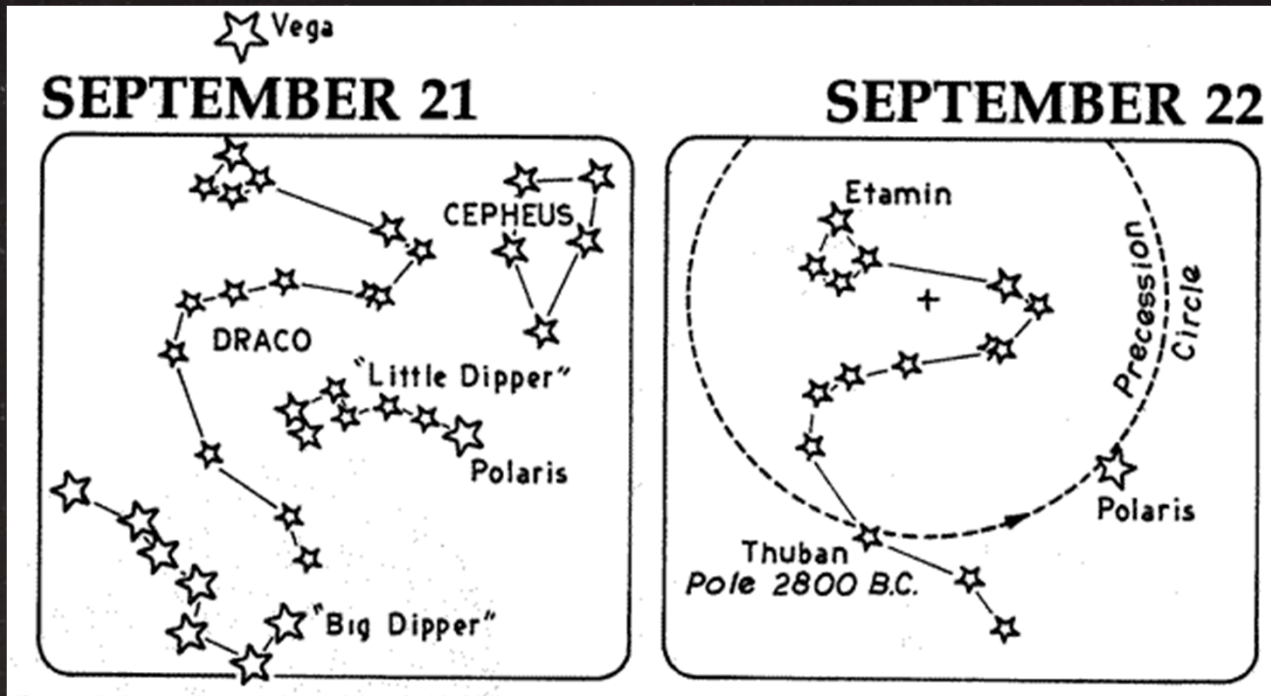


RA and Dec grid wobbles with pole,  
ecliptic does not wobble so solstices  
& equinoxes change position

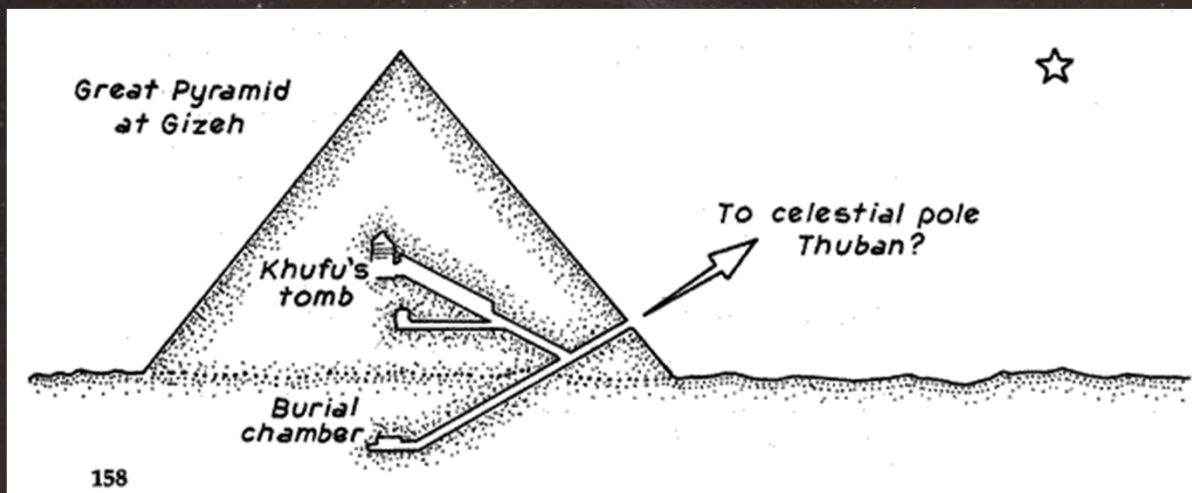
©1996-2001 Scott R. Anderson

[http://www.opencourse.info/astronomy/introduction/03\\_motion\\_earth/](http://www.opencourse.info/astronomy/introduction/03_motion_earth/)

# Raymo's 365 Starry Nights



Precession  
Circle

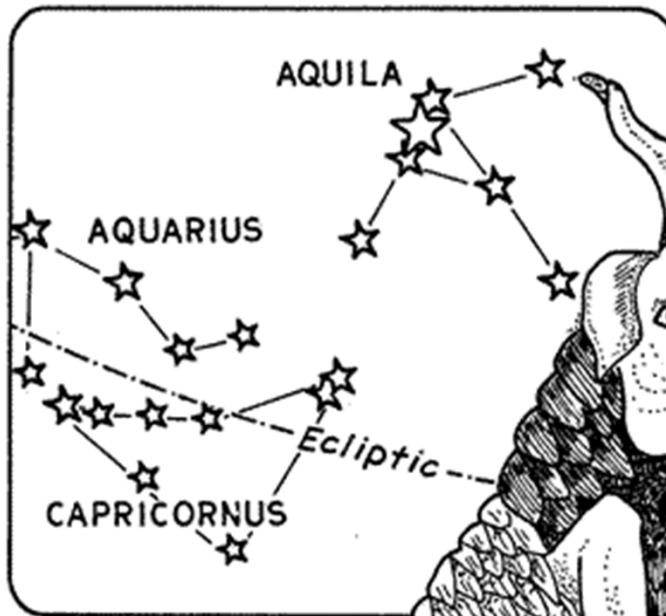


View from  
the  
Pyramids

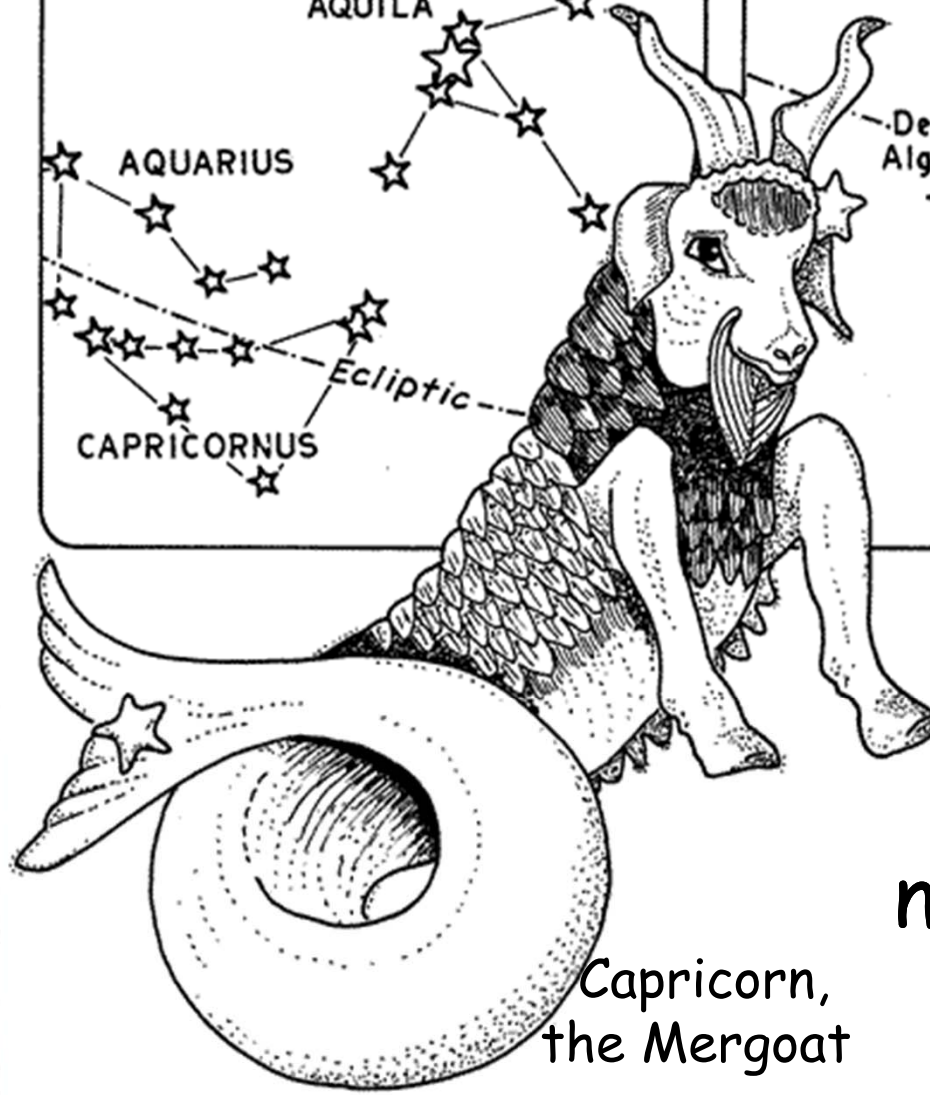
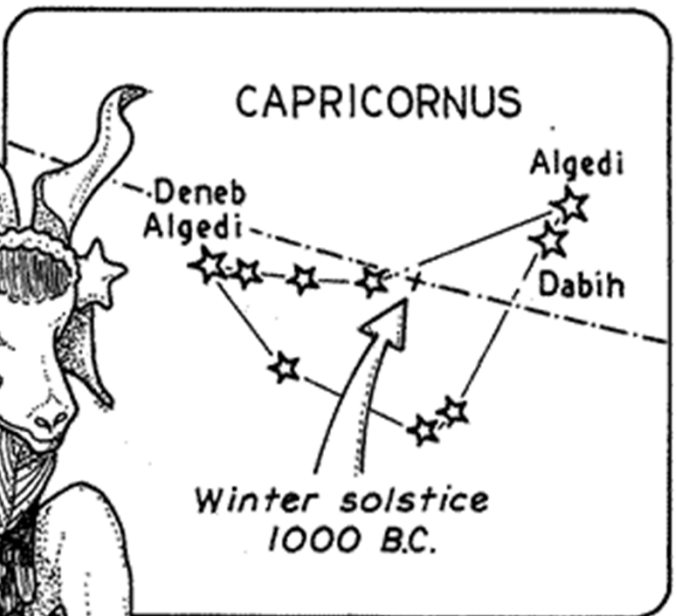
# Raymo's 365 Starry Nights

Position  
of the  
winter  
solstice  
in 1000  
BCE

SEPTEMBER 23



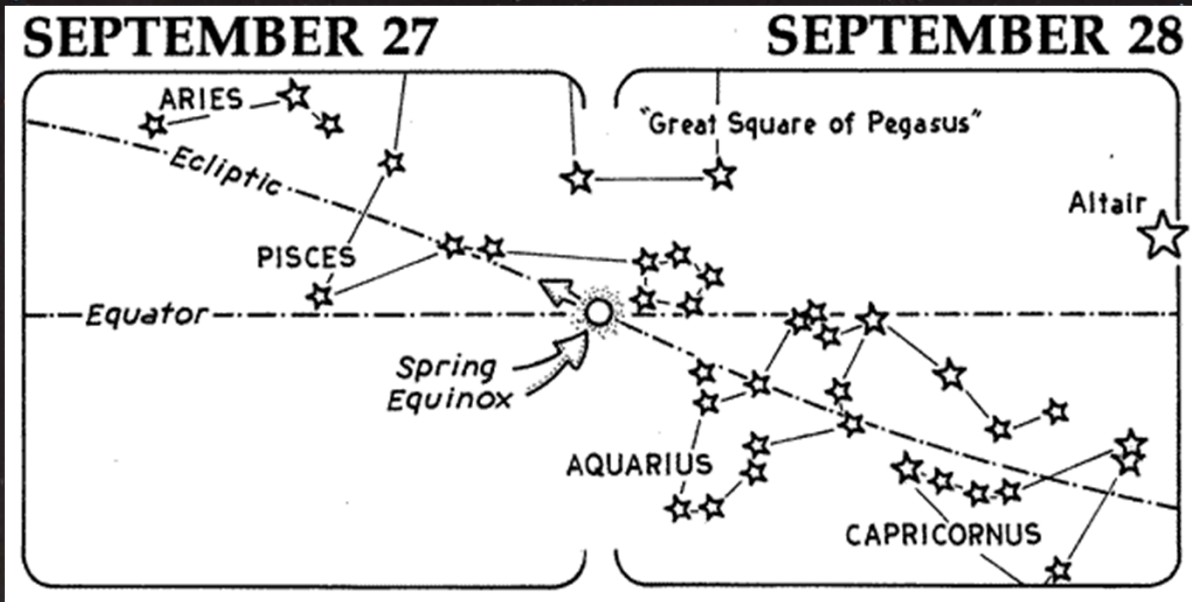
SEPTEMBER 24



Tropic of  
Capricorn  
name origin

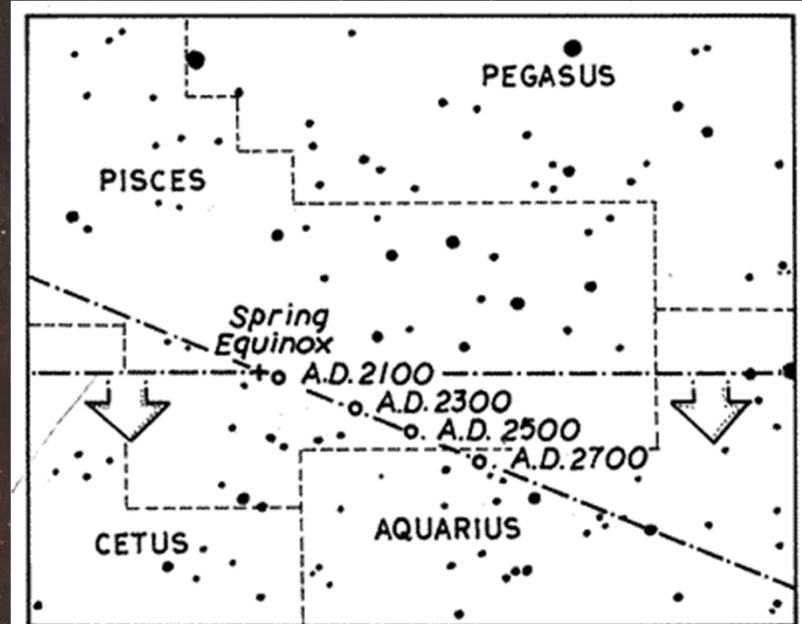
Capricorn,  
the Mergoat

# Raymo's 365 Starry Nights



Position of  
the Vernal  
Equinox now

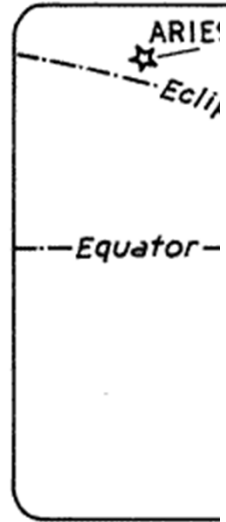
Motion of the Vernal  
Equinox to the  
"Age of Aquarius"



# Raymo's 365 Starry Nights

SEPTEMBER 27

SEPTEMBER 28



When the moon is in the Seventh House  
And Jupiter aligns with Mars  
Then peace will guide the planets  
And love will steer the stars

This is the dawning of the Age of Aquarius  
Aquarius! Aquarius!

Harmony and understanding  
Sympathy and trust abounding  
No more falsehoods or derisions  
Golden living dreams of visions  
Mystic crystal revelation  
And the mind's true liberation  
Aquarius! Aquarius!



of  
nal  
now

