

SOAR: The Sky in Motion

The Year

Aileen A. O'Donoghue
Henry Priest Professor of Physics

The Tilted Teacup Ride

☆ Coordinates and the Day: 9/11/25

🌐 Celestial Navigation

☆ The Year: 9/18/25

🌐 The Age of Aquarius

☆ The Month and Moon Phases: 9/25/25

🌐 The Harvest Moon

☆ The Day in All its Glory: 10/2/25

🌐 The Analemma

The Tilted Teacup Ride

☆ Coordinates and the Day: 9/6/22

🌐 Celestial Navigation

☆ The Year: 9/13/22

🌐 The Age of Aquarius

☆ The Month and Moon Phases: 9/20/22

🌐 The Harvest Moon

☆ The Day in All its Glory: 9/27/22

🌐 The Analemma

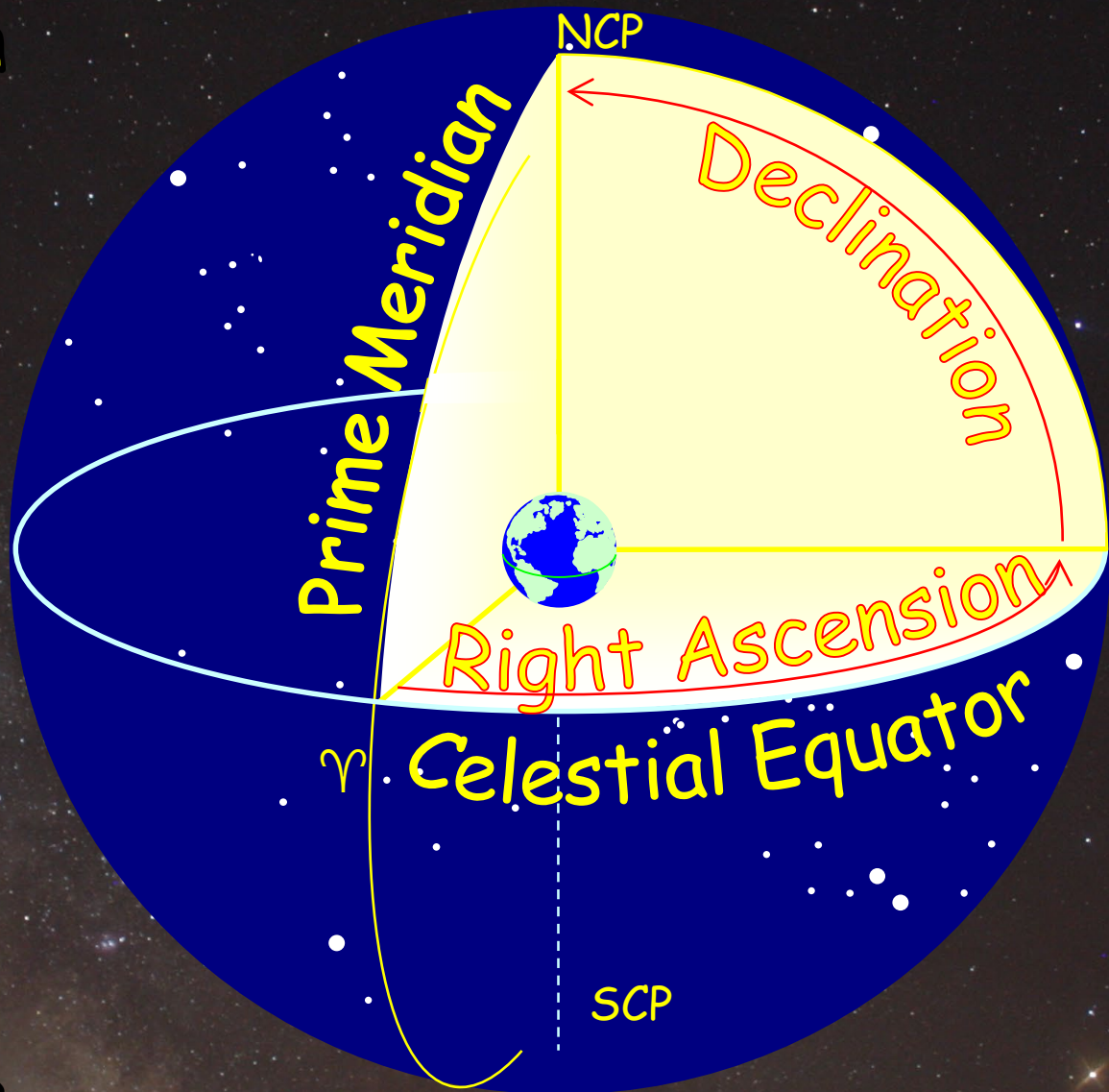
Celestial Coordinates

☆ Right Ascension

- 🌐 RA or α
- 🌐 From prime meridian (0^h) to $23^h59^m59^s$ Eastward

☆ Declination

- 🌐 Dec or δ
- 🌐 From celestial equator (0°) to poles N & S 90°

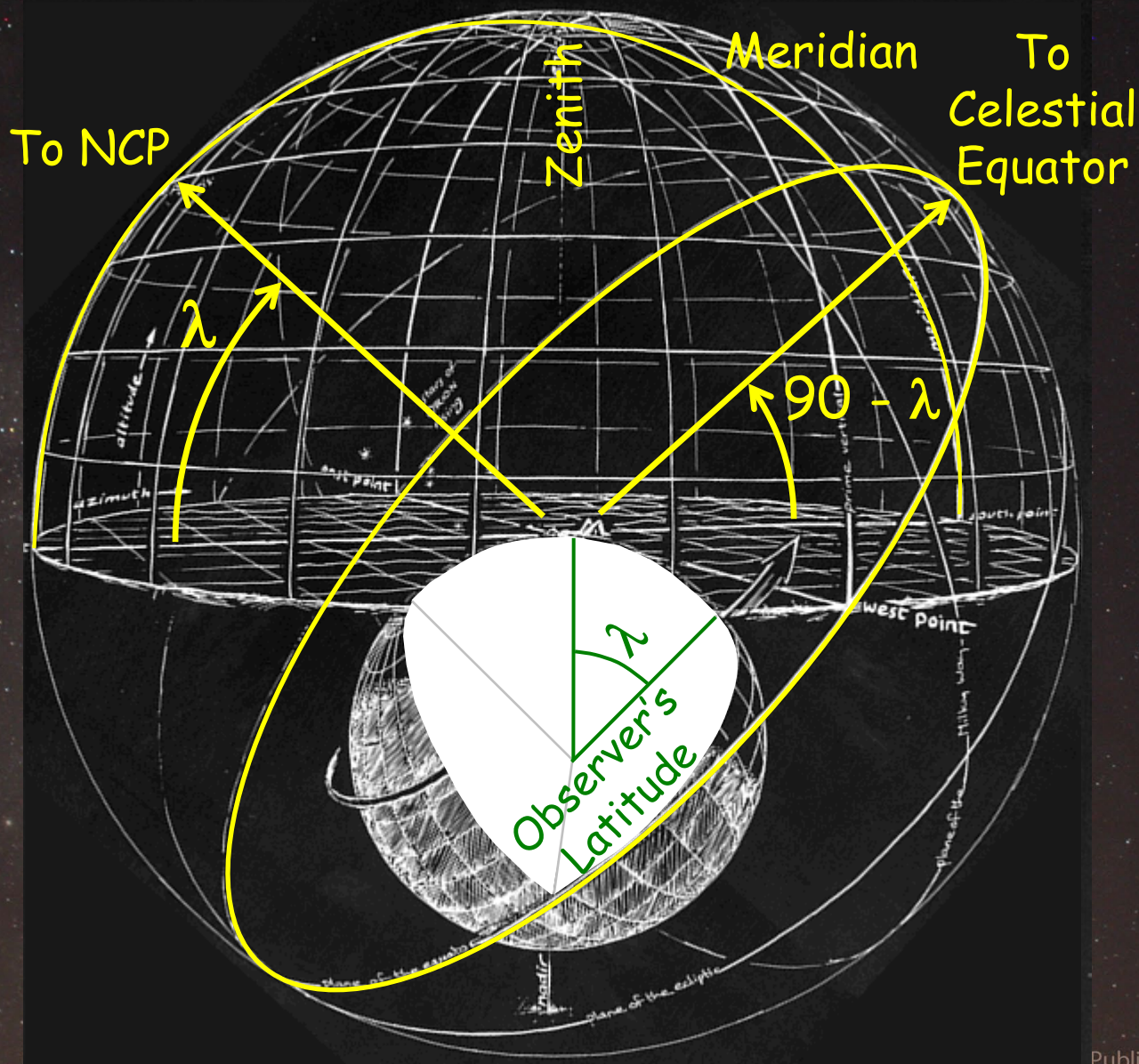


Tilted Sky

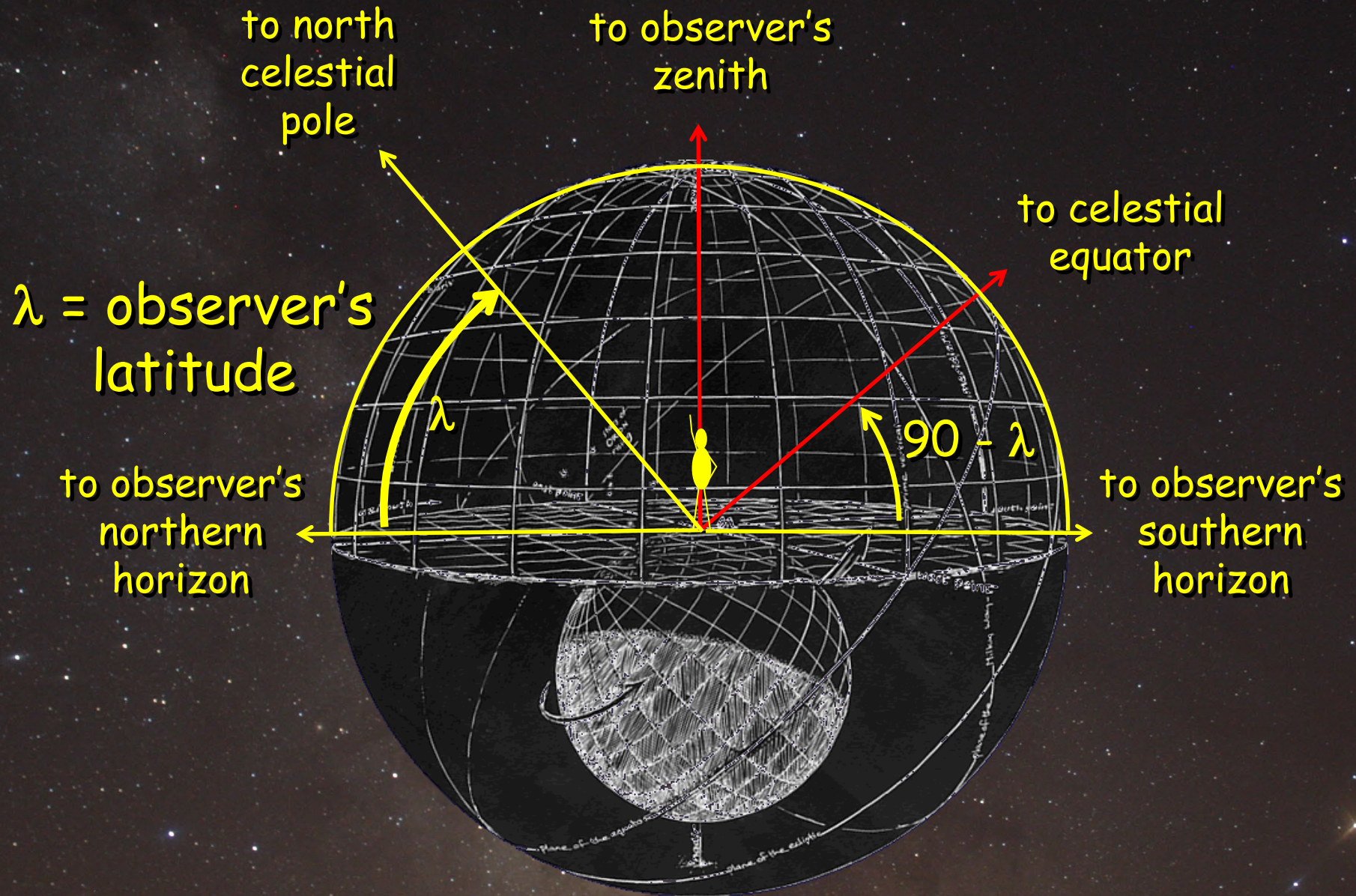
☆ Observers see sky "tilted" due to latitude

We see ourselves "on top" of the Earth, beneath the sky.

So we see sky motions tilted



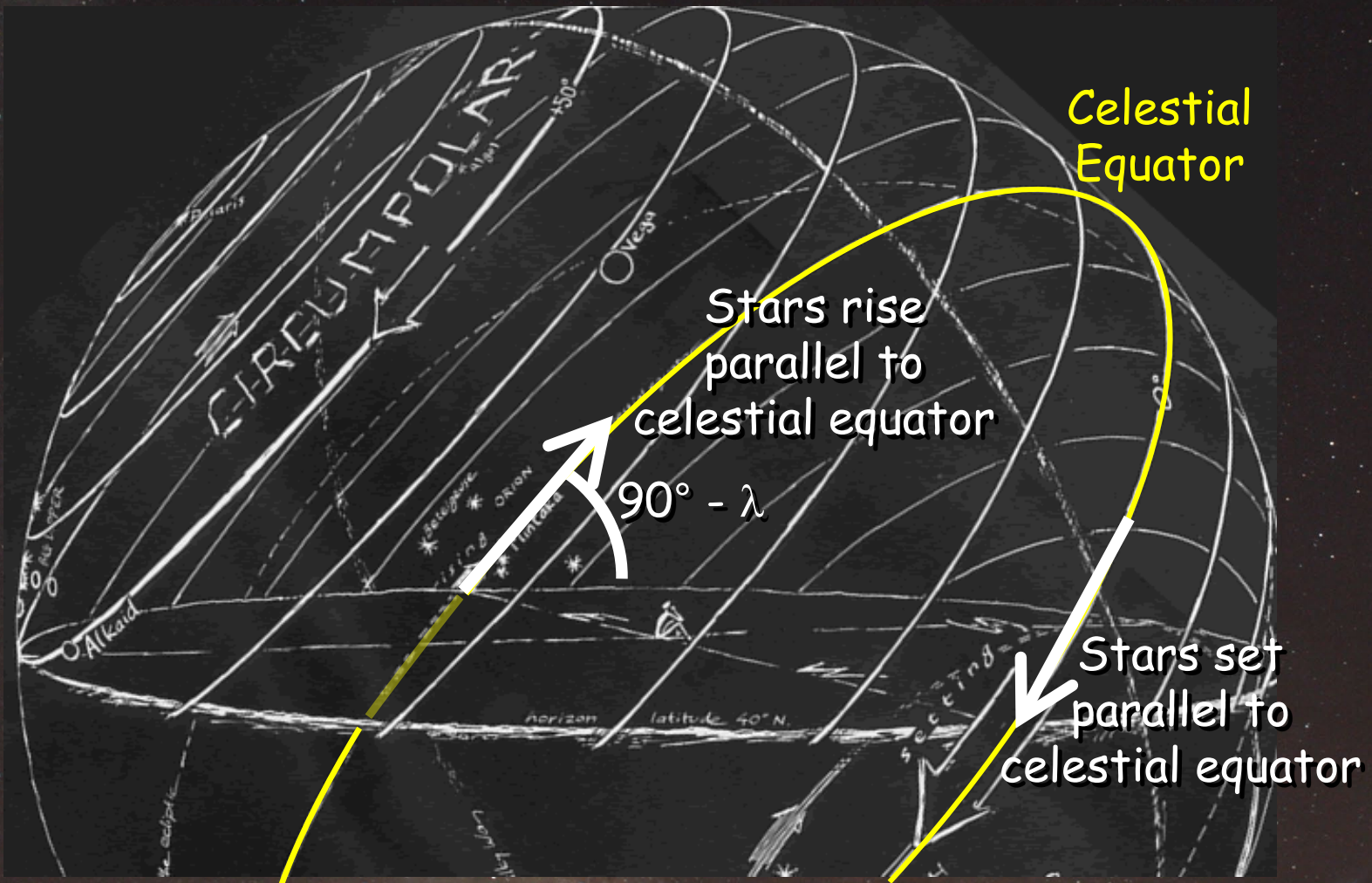
Horizon Coordinate System



View of Observers

☆ Diurnal circles are parallel to CE

🌍 Stars rise and set at CE's angle from horizon



Sunrise, Sunset ...

☆ Everything in the sky (sun, moon, stars, etc.)

🌍 Rises in the east

🌍 Sets in the west

each day

Measuring Circles:

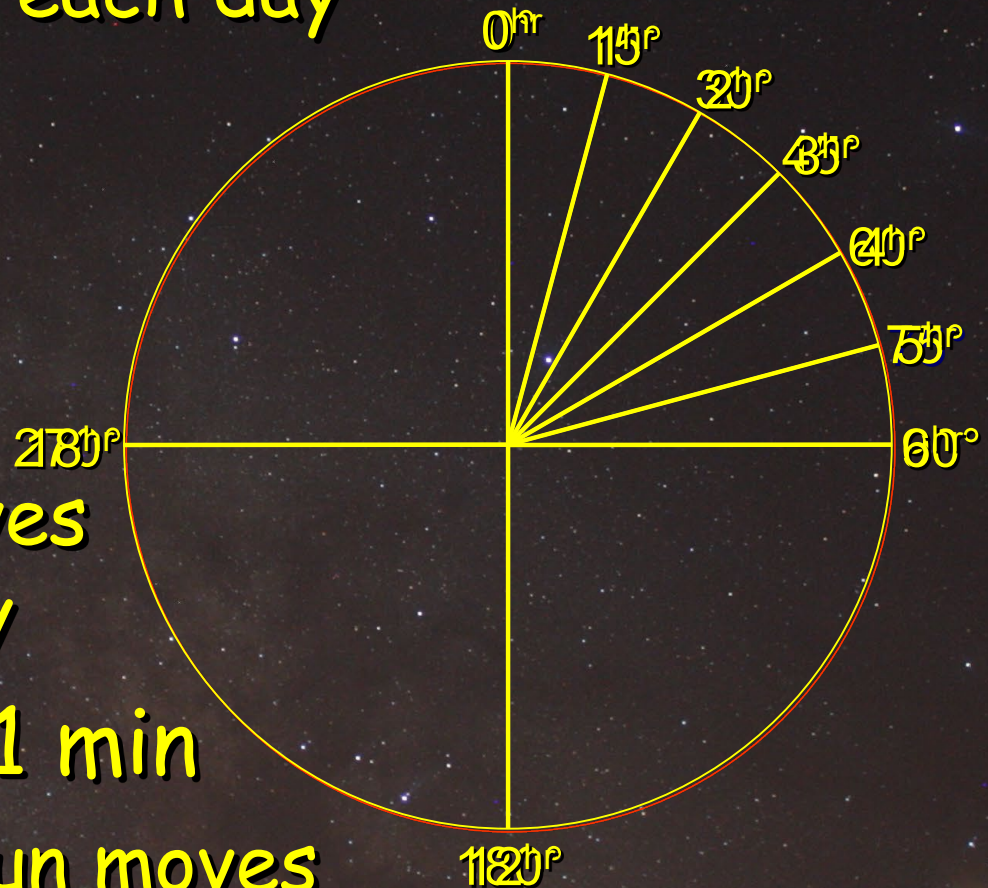
$360^\circ = 24 \text{ hr}$

$15^\circ = 1 \text{ hr}$

Each hour, the sun moves
15 degrees in the sky

$1^\circ = 4 \text{ min}$ or $15' = 1 \text{ min}$

Every 4 minutes, the sun moves
1 degree = $60'$ in the sky



Clock Time = Position of Sol

☆ Observers move through times

It's 6 pm
(sunset).

It's 3 pm.

It's
noon.

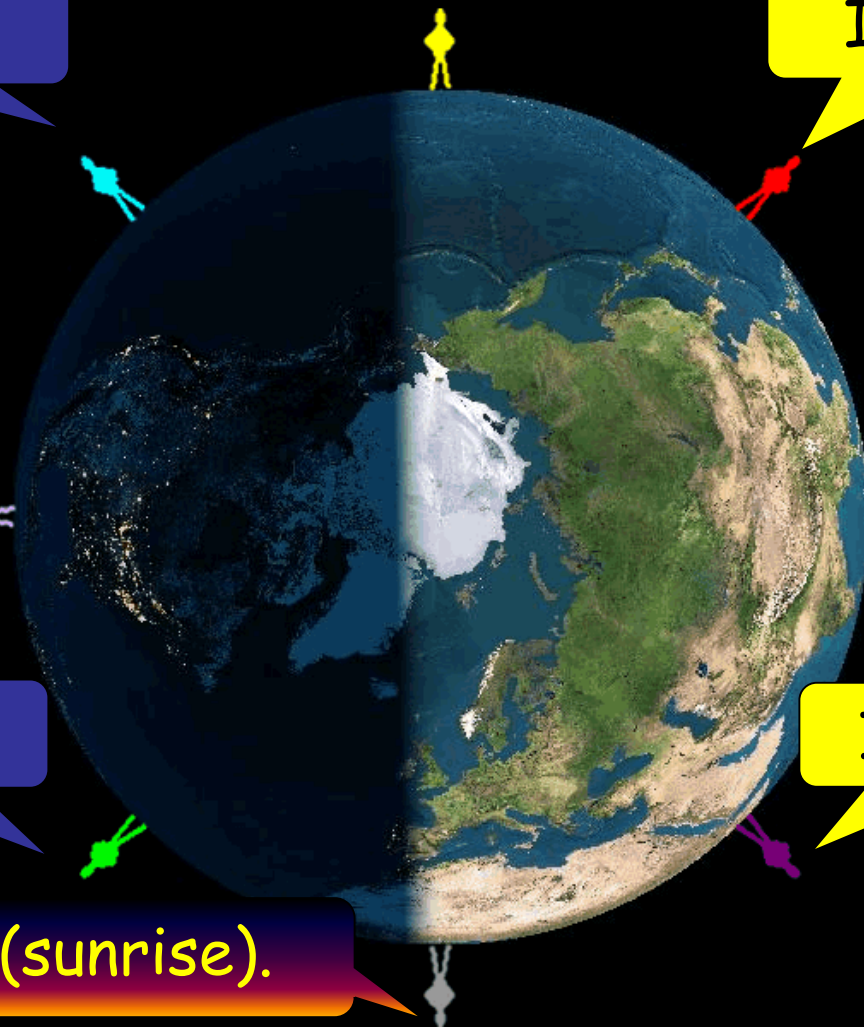
It's 9 am.

It's 9 pm.

It's
midnight.

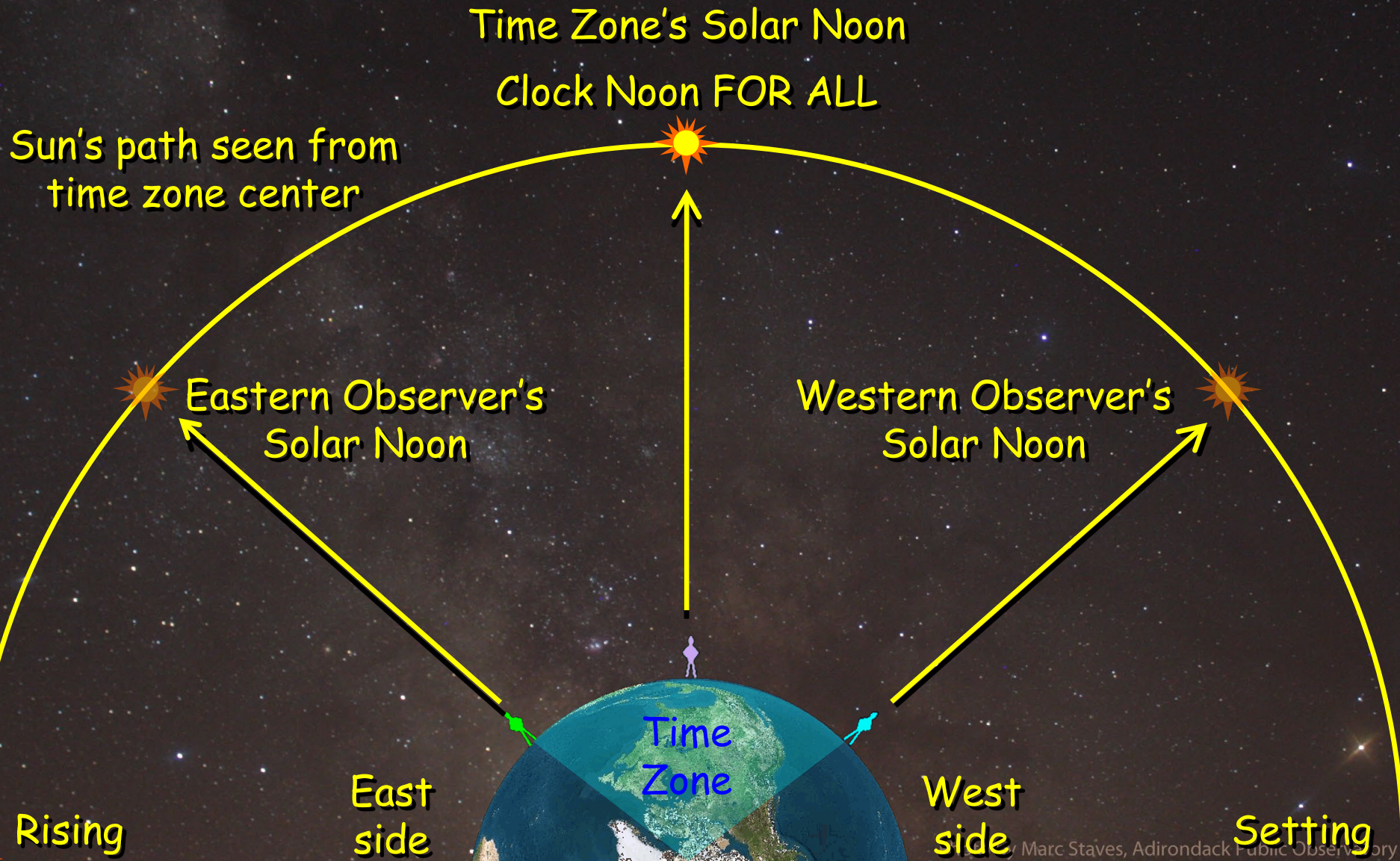
It's 3 am.

It's 6 am (sunrise).



Solar Time vs. Clock Time

☆ Solar time varies across time zones

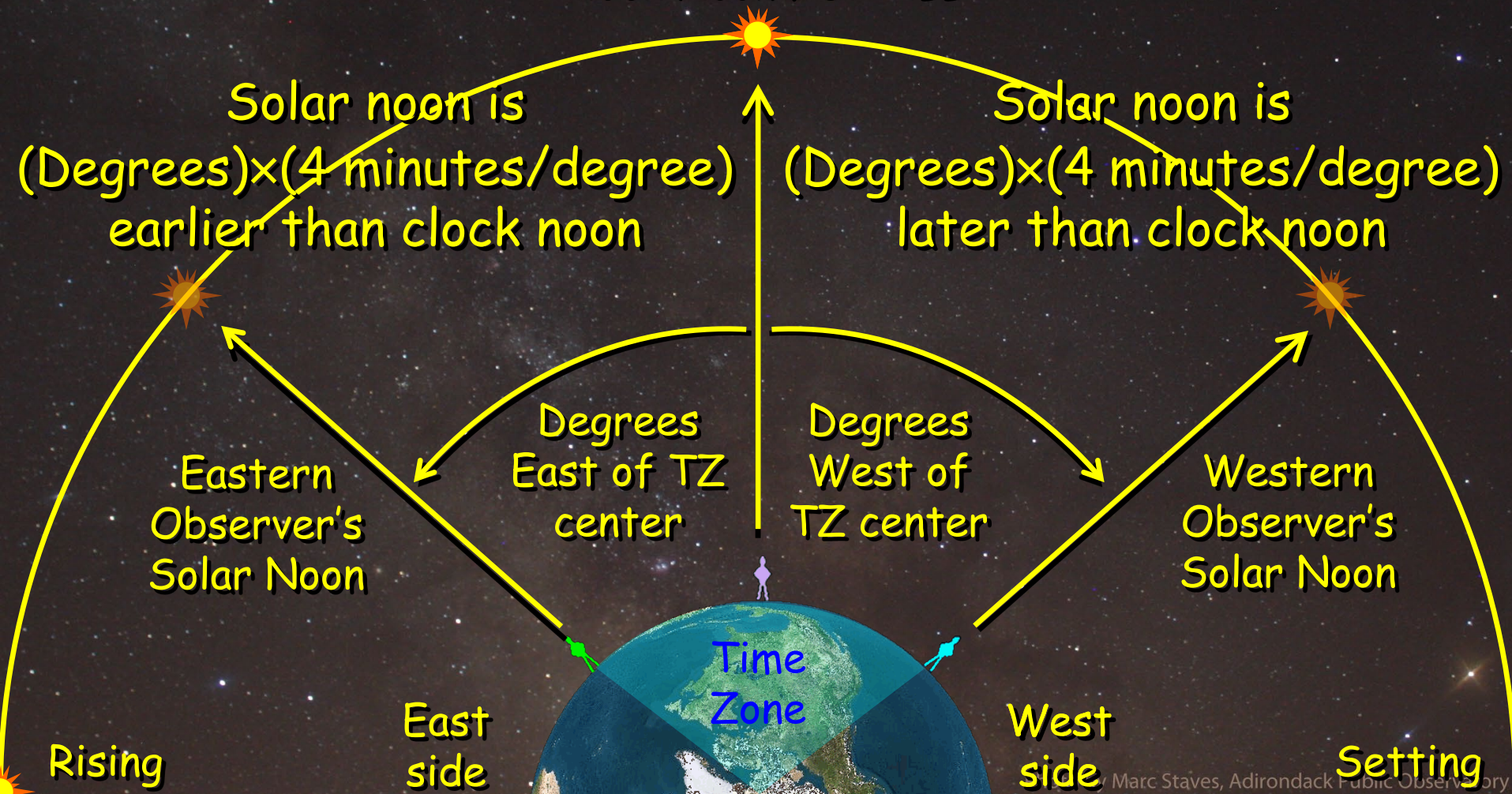


Solar Time vs. Clock Time

☆ Solar time varies across time zones

Time Zone's Solar Noon

Clock Noon FOR ALL



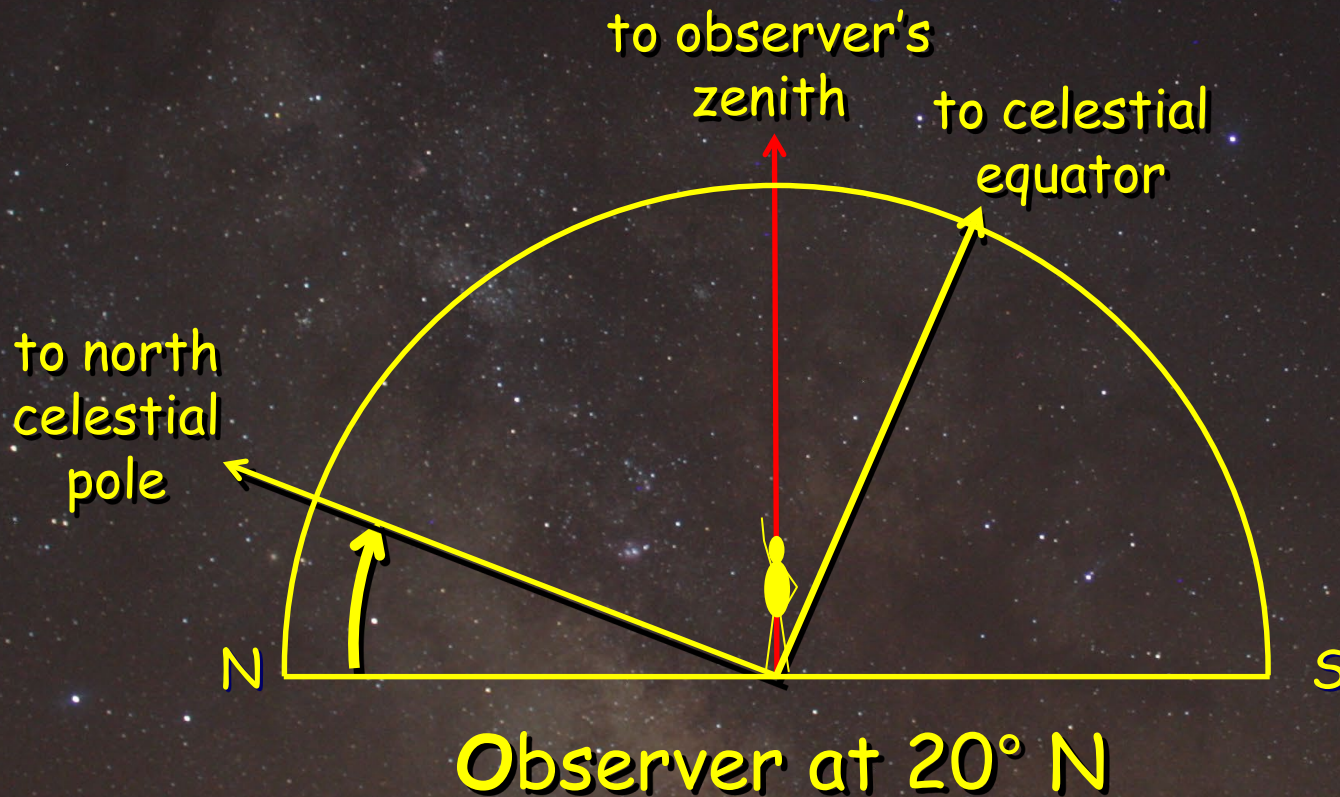
Celestial Navigation

☆ Finding Latitude & Longitude from

① Altitude of Polaris (NCP)

② Transit time of star

› Looked up in an ephemeris (eg. Field Guide)

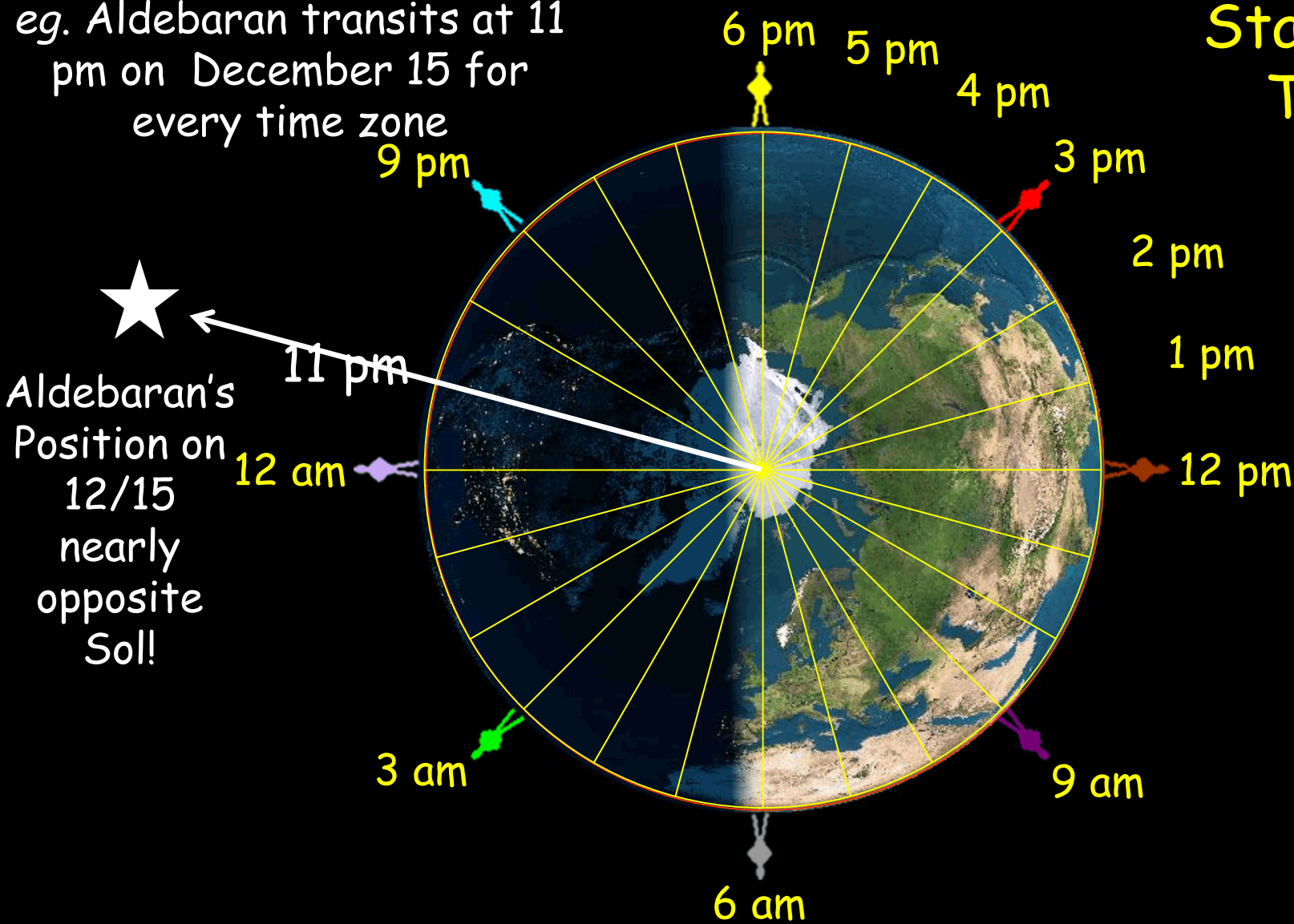


Star Transit Time

Gives position of star with respect to the sun

eg. Aldebaran transits at 11 pm on December 15 for every time zone

Standard Time



Clicker Question

☆ What's your longitude if you see Altair transit at 1 am on September first and your watch is set for Pacific time?

On 9/1 Altair transits at 10 pm PDT

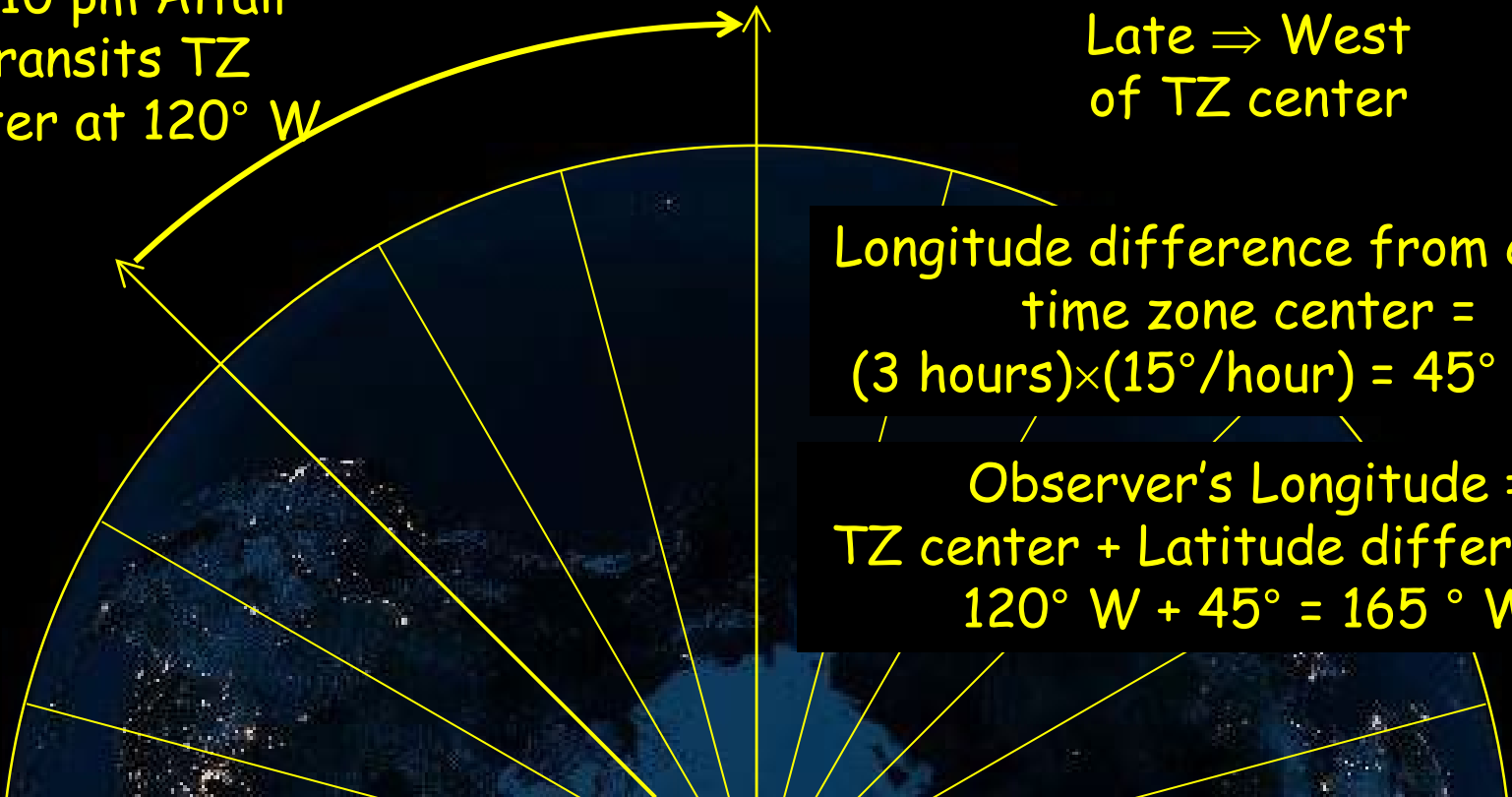
At 10 pm Altair transits TZ center at 120° W

Observer sees Altair transit at 1 am PDT

Late \Rightarrow West of TZ center

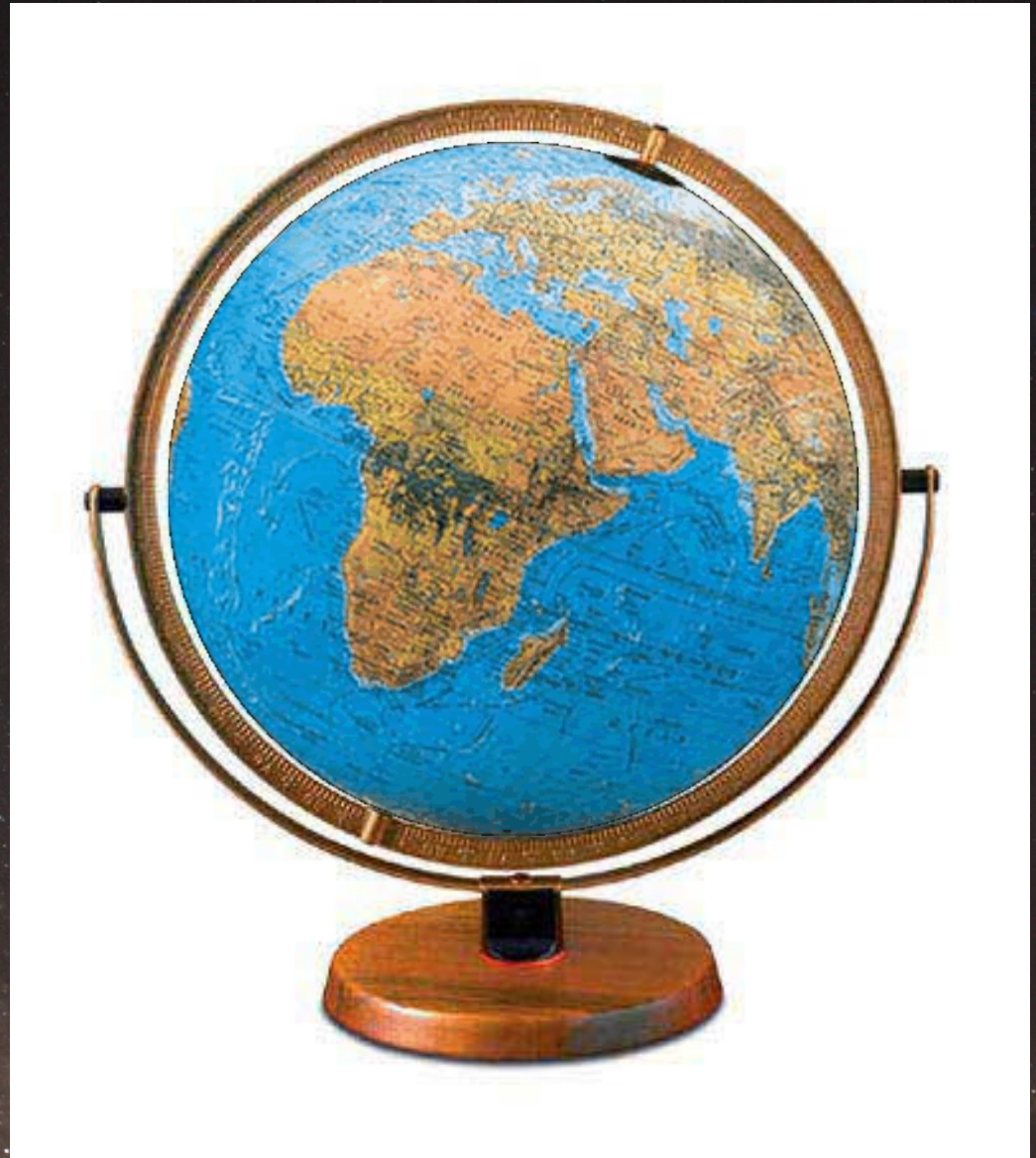
Longitude difference from clock's time zone center =
 $(3 \text{ hours}) \times (15^\circ/\text{hour}) = 45^\circ$ West

Observer's Longitude =
TZ center + Longitude difference =
 $120^\circ \text{ W} + 45^\circ = 165^\circ \text{ W}$

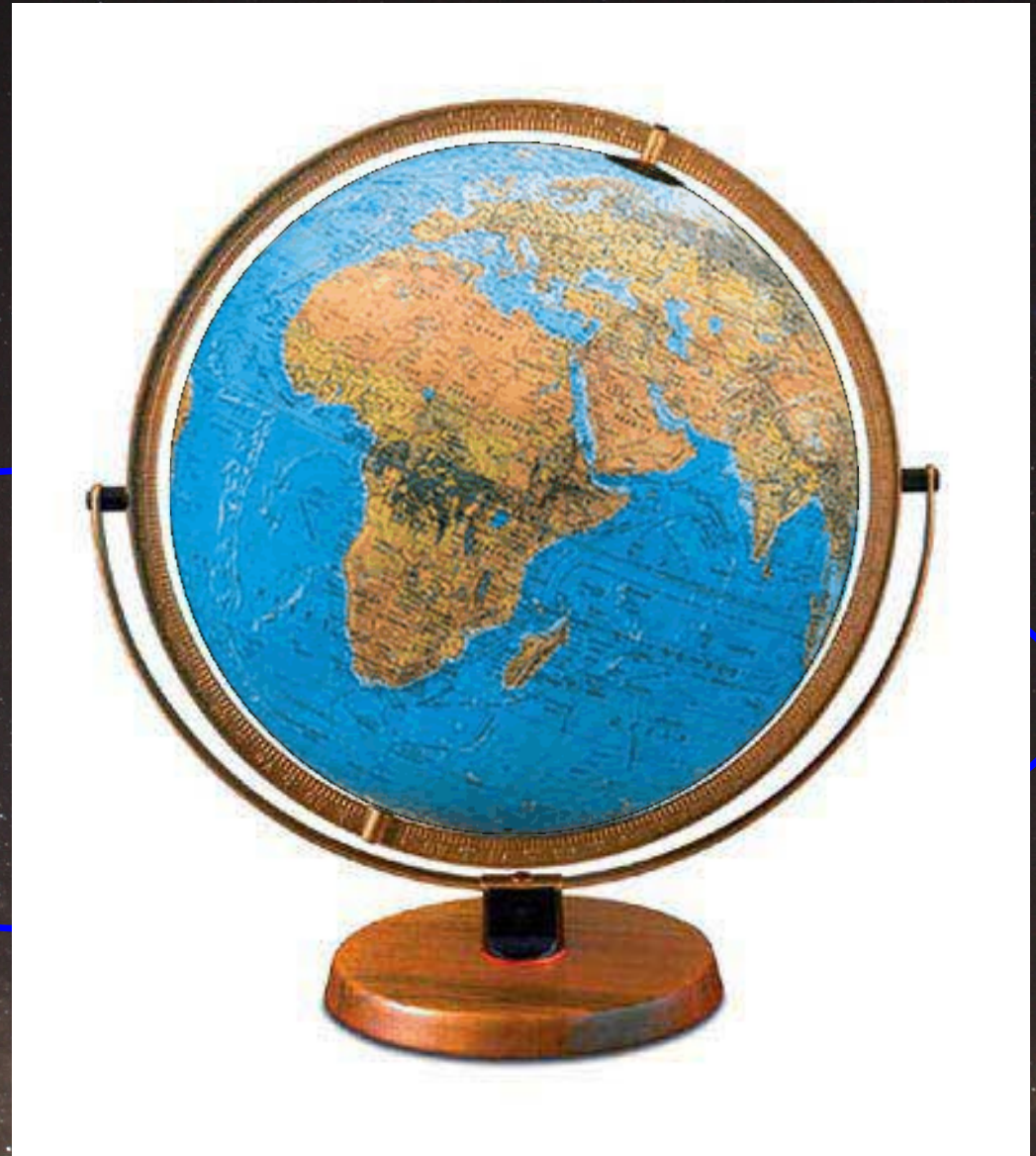


Models of Earth

Why are
globes
tilted?



Earth's Orbit



licker Question

☆ Why is it warmer in the summer?

a) Earth is closer to the Sun

b) The Sun is higher in the sky

c) Because it's summer!

Earth's Orbit

☆ Ellipse with Sun at one focus

🌍 perihelion - closest to sun

› January 3, 2026 at 12:15 pm EST

› Earth moving fastest ... Feb is short!

🌍 aphelion - farthest from sun

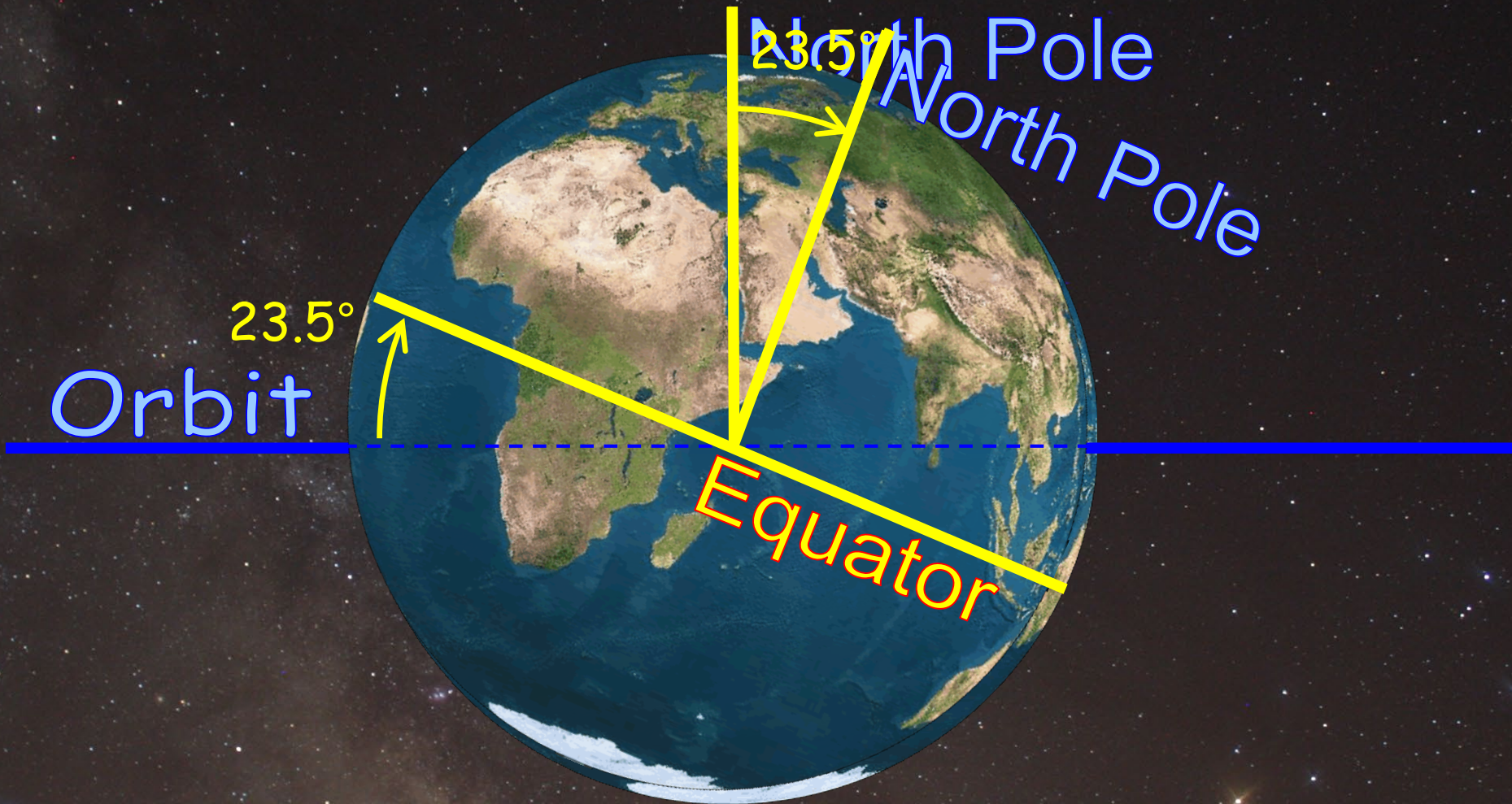
› July 6, 2026 at 1:30 pm EDT

☆ N Pole toward Polaris



Earth's Orbit

☆ Rotation Axis tilted 23.5° from \perp



The Home World

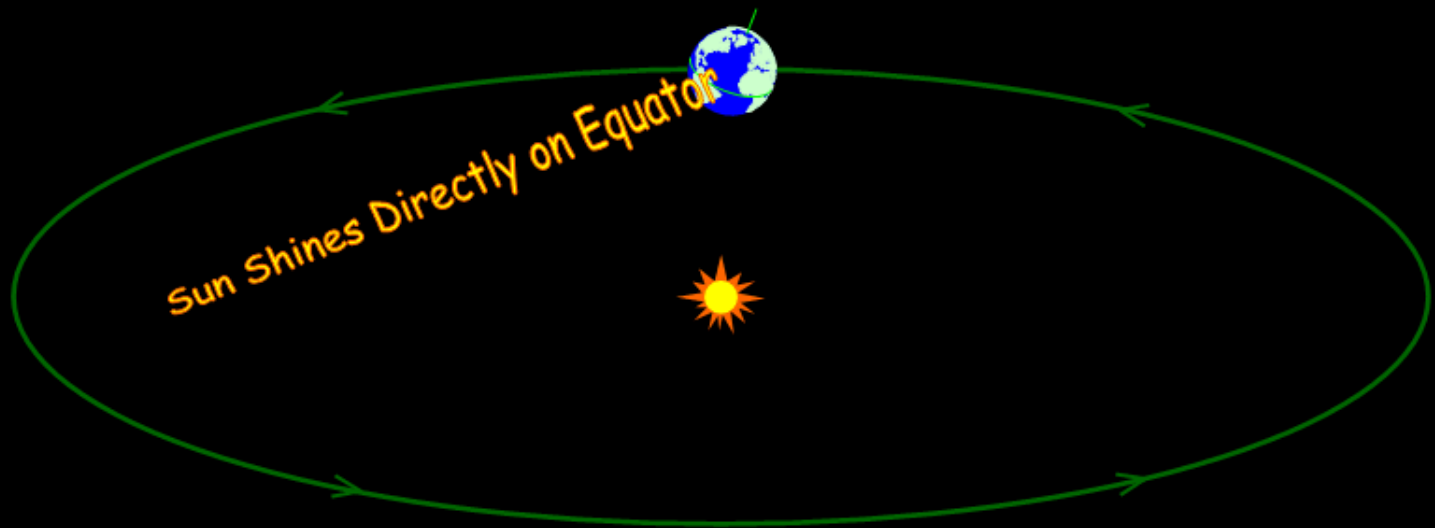
☆ The Earth in space: Axis points at Polaris

🌍 360° in 365 days $\Rightarrow \sim 1^\circ/\text{day}$

🌍 Rotation axis tilted 23.5° from orbit axis

\Rightarrow Declination of sun varies through year

\Rightarrow subsolar latitude varies through year



Seasons

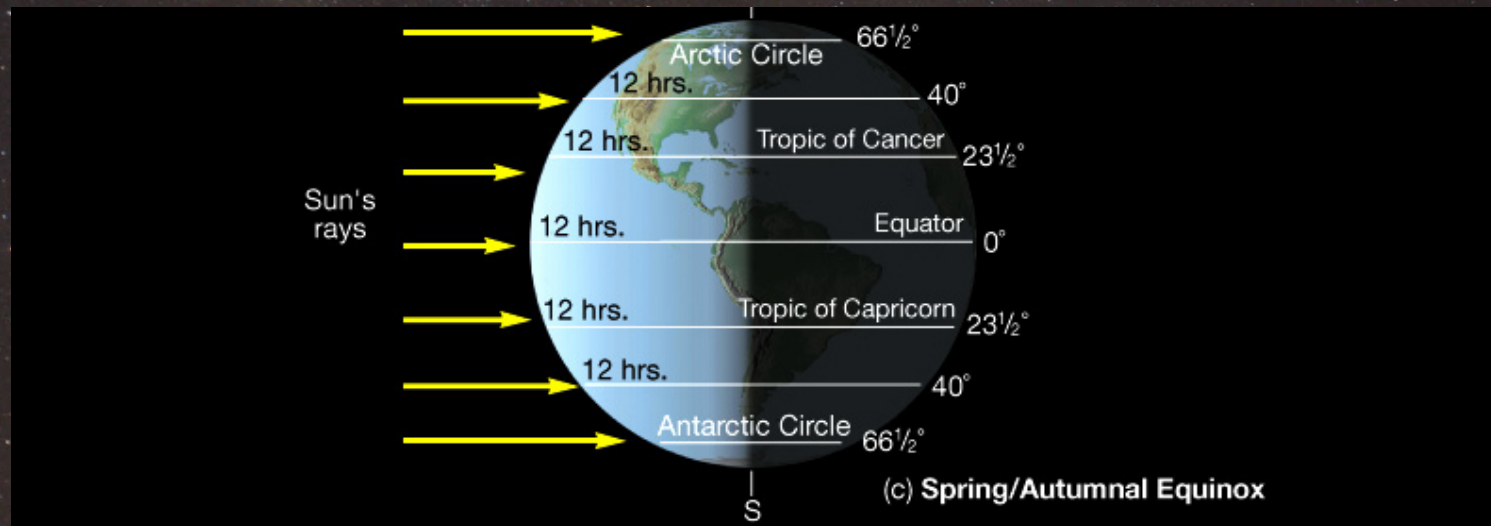
☆ Equinox - Sun on Celestial Equator

☉ Vernal (spring): $\delta = 0^\circ$, $\alpha = 0^h$

› Sun crossing equator moving north

☉ Autumnal (fall): $\delta = 0^\circ$, $\alpha = 12^h$

› Sun crossing equator moving south

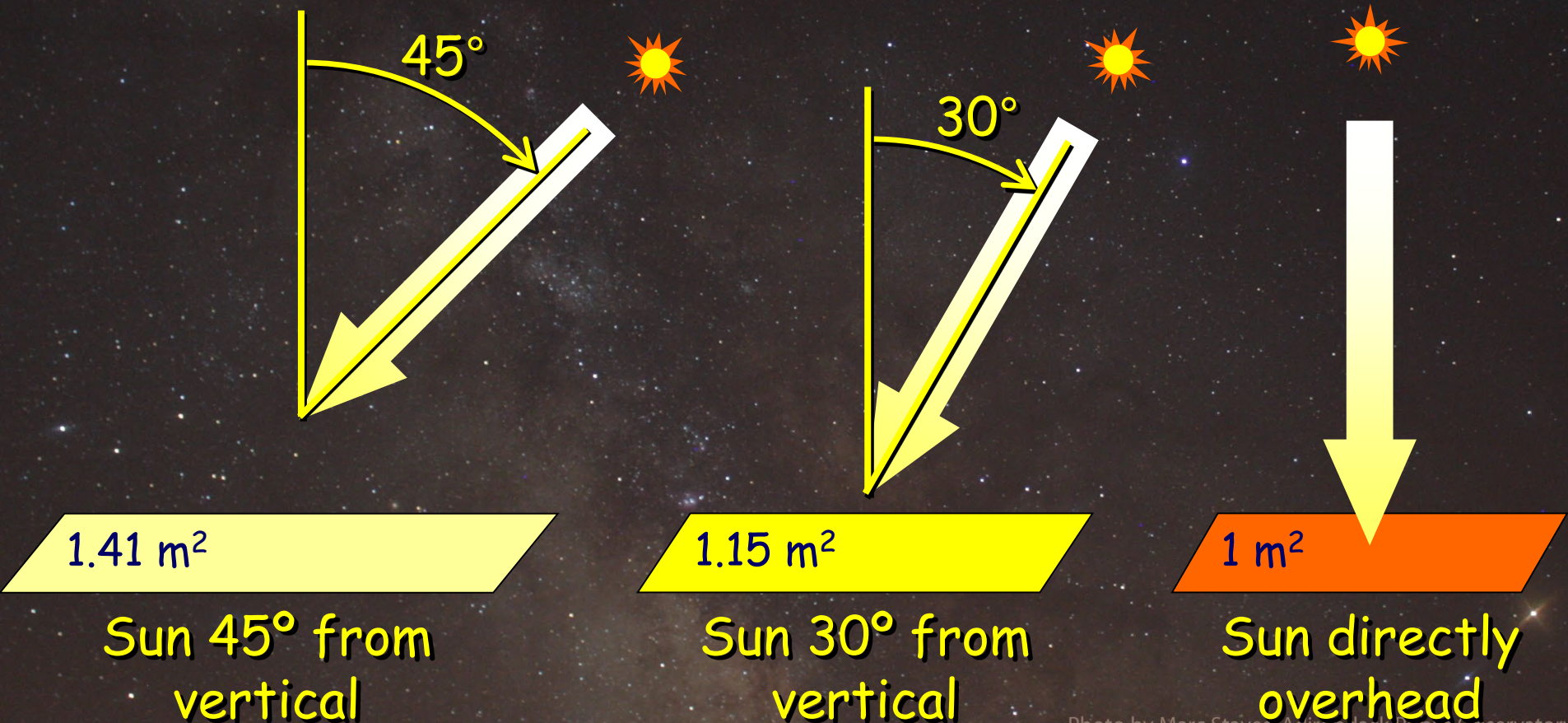


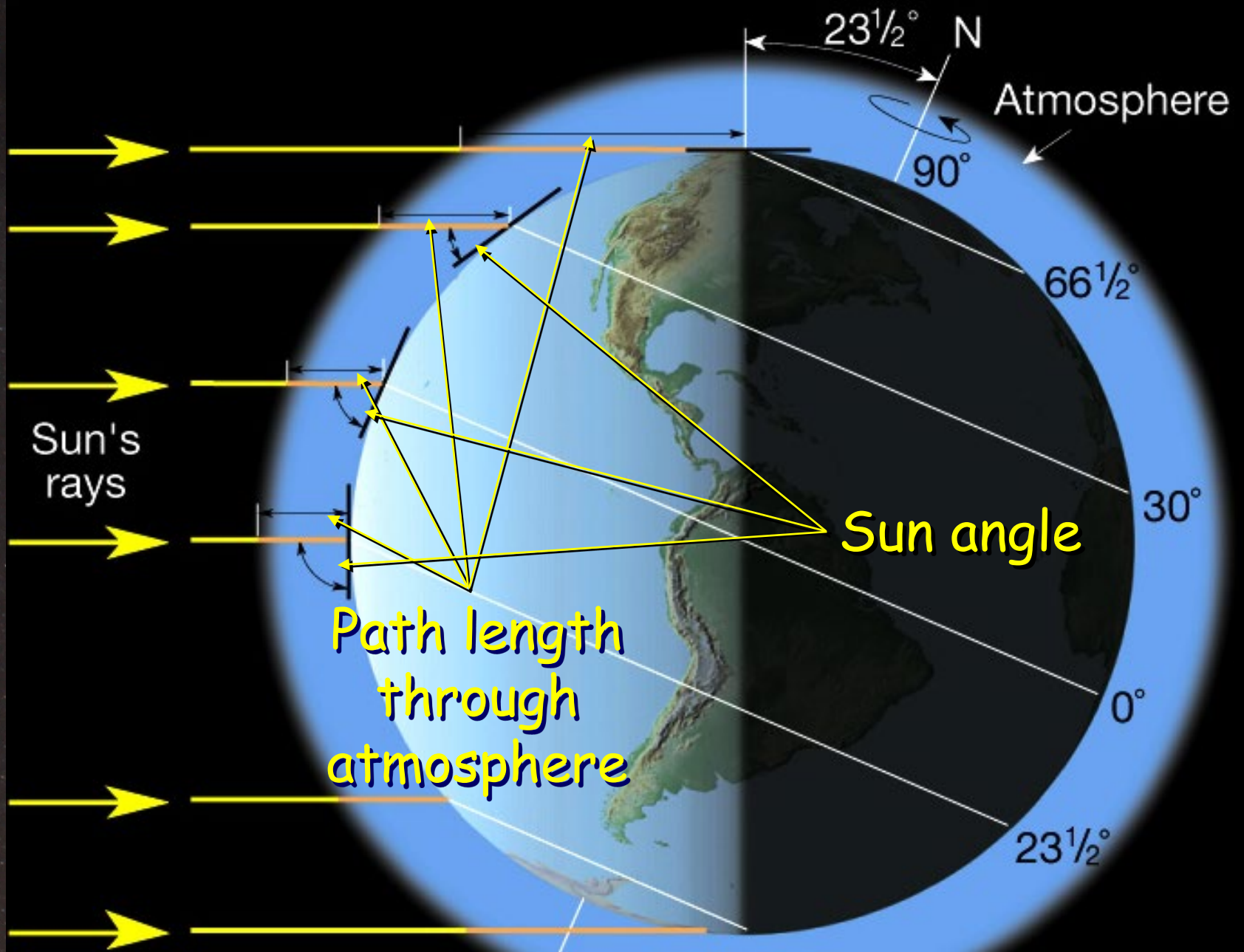
Seasons

☆ Due to changing angle of sunlight

🌍 At low angles, sunlight spreads out

› less energy falls on any piece of ground



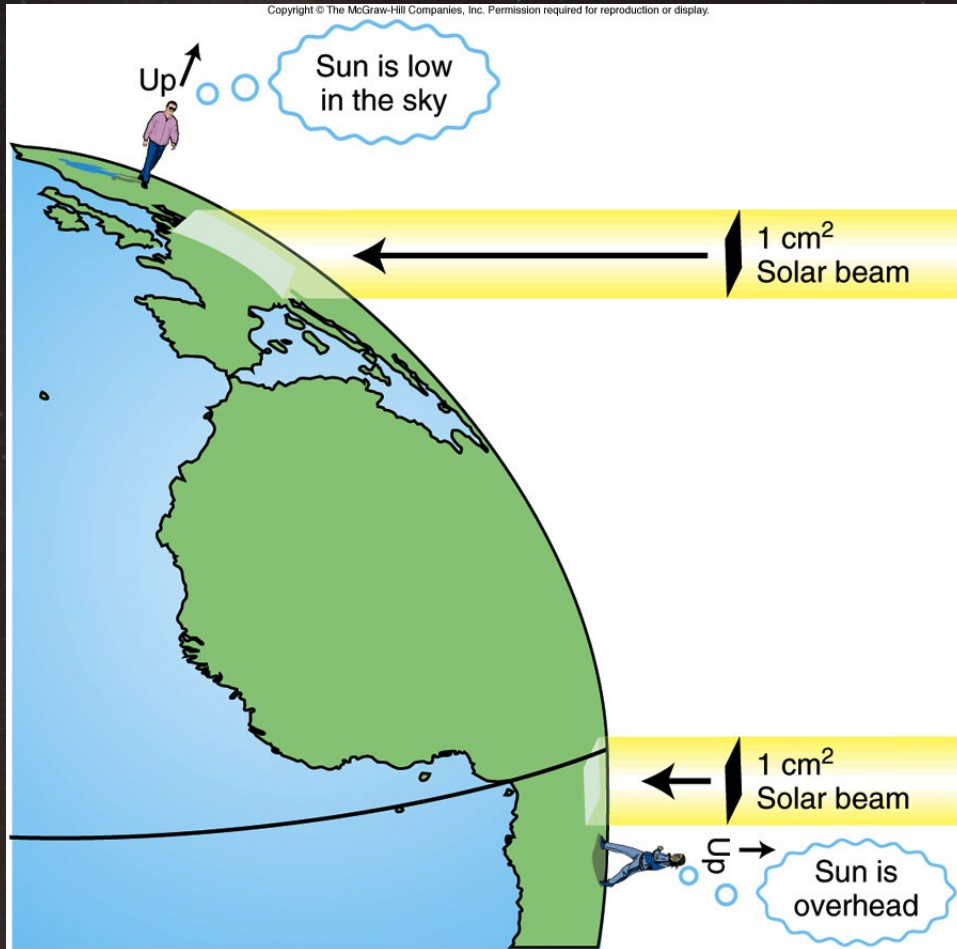


Seasons: Due to changing insolation.

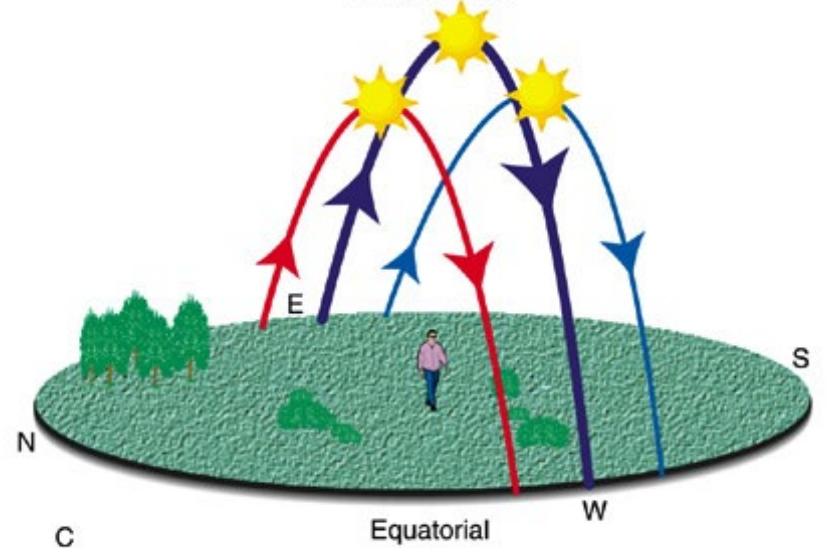
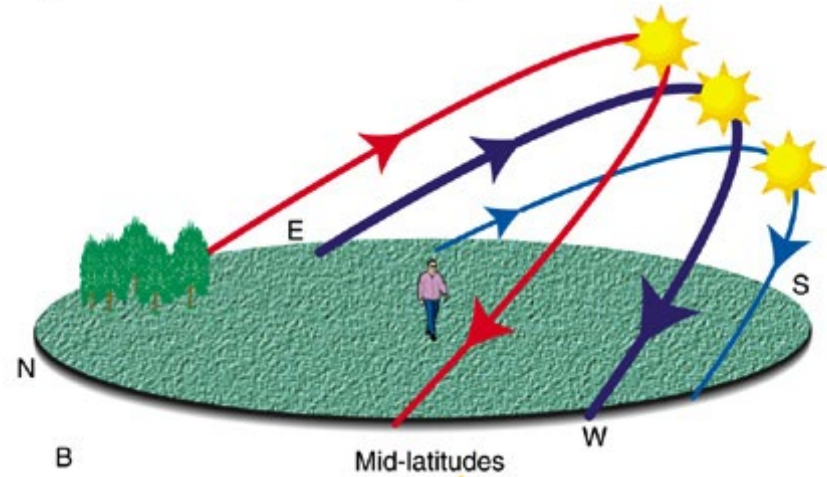
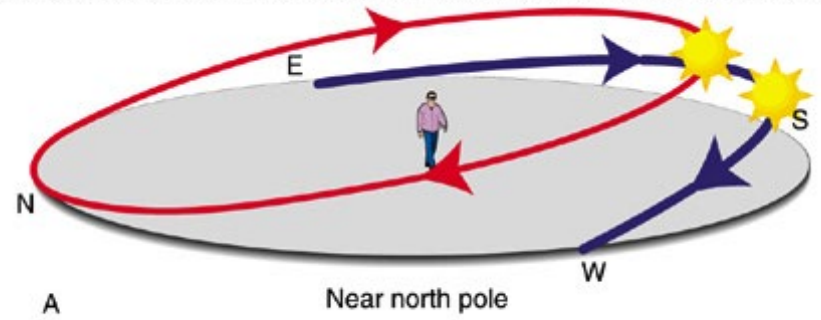
Seasons

☆ Vary with latitude

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— June — September, March — December

Seasons

☆ Equinox - sun on Celestial Equator

🌍 Vernal (spring) $0^{\text{h}} 0^{\circ}$

10:46 am, March 20, 2026

› Sun crosses CE moving north

🌍 Autumnal (fall) $12^{\text{h}} 0^{\circ}$

8:05 pm, September 22, 2026

› Sun crosses CE moving south

☆ Solstice - sun farthest north or south

🌍 Northern Summer $6^{\text{h}} +23.5^{\circ}$

› Sun northernmost ($+23.5^{\circ}$)

4:24 am, June 21, 2026

🌍 Southern Summer $18^{\text{h}} -23.5^{\circ}$

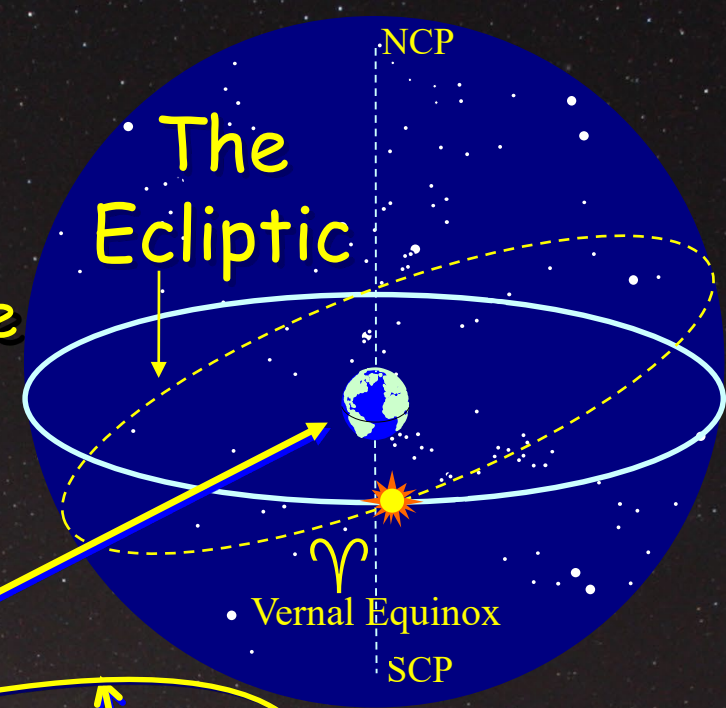
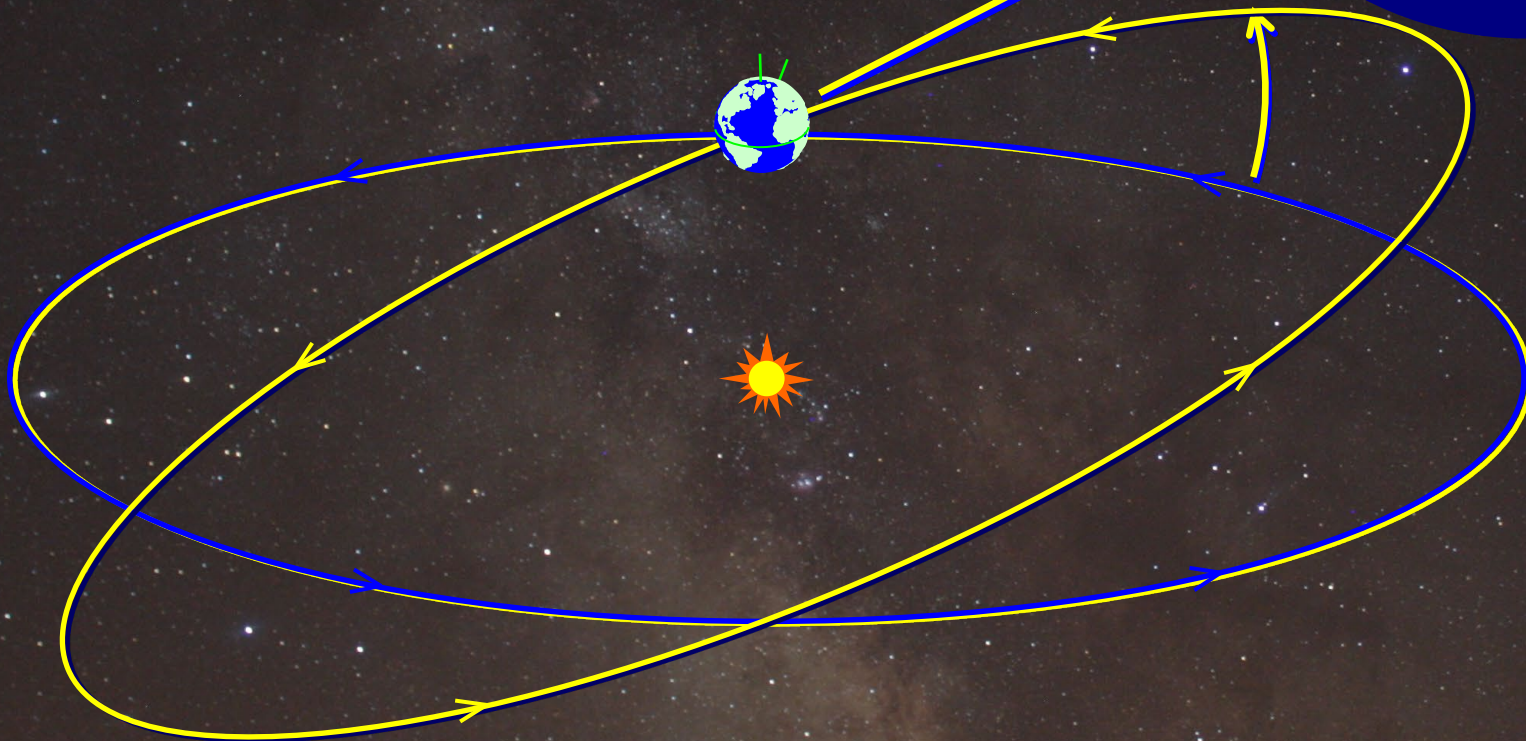
› Sun southernmost (-23.5°)

10:03 am, December 21, 2026

Sun in the sky

☆ View from Earth

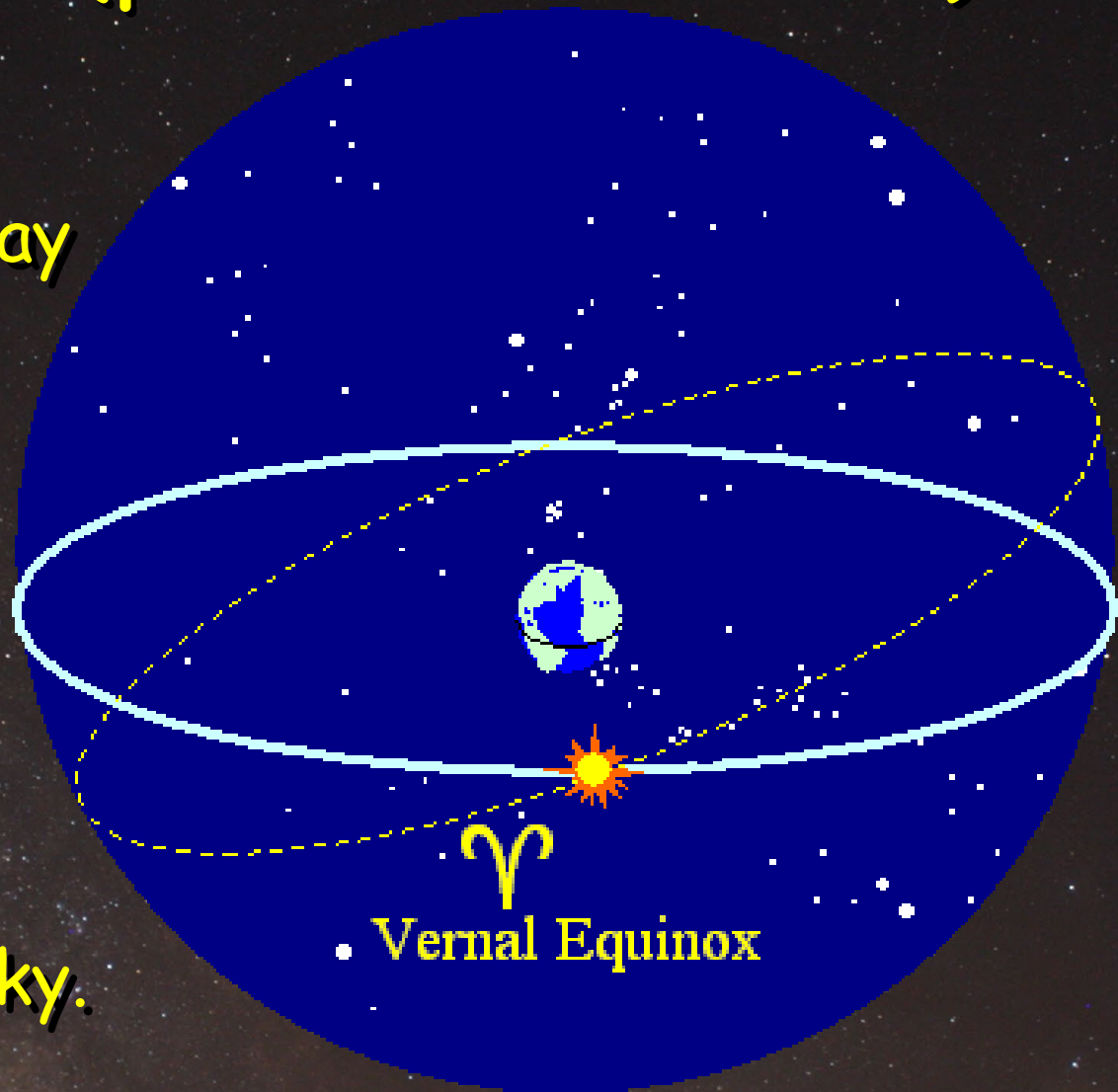
- 🌍 Rotate to Earth's equatorial plane
- 🌍 Center on Earth
- 🌍 Project sun onto sky



The Ecliptic (path of the sun)

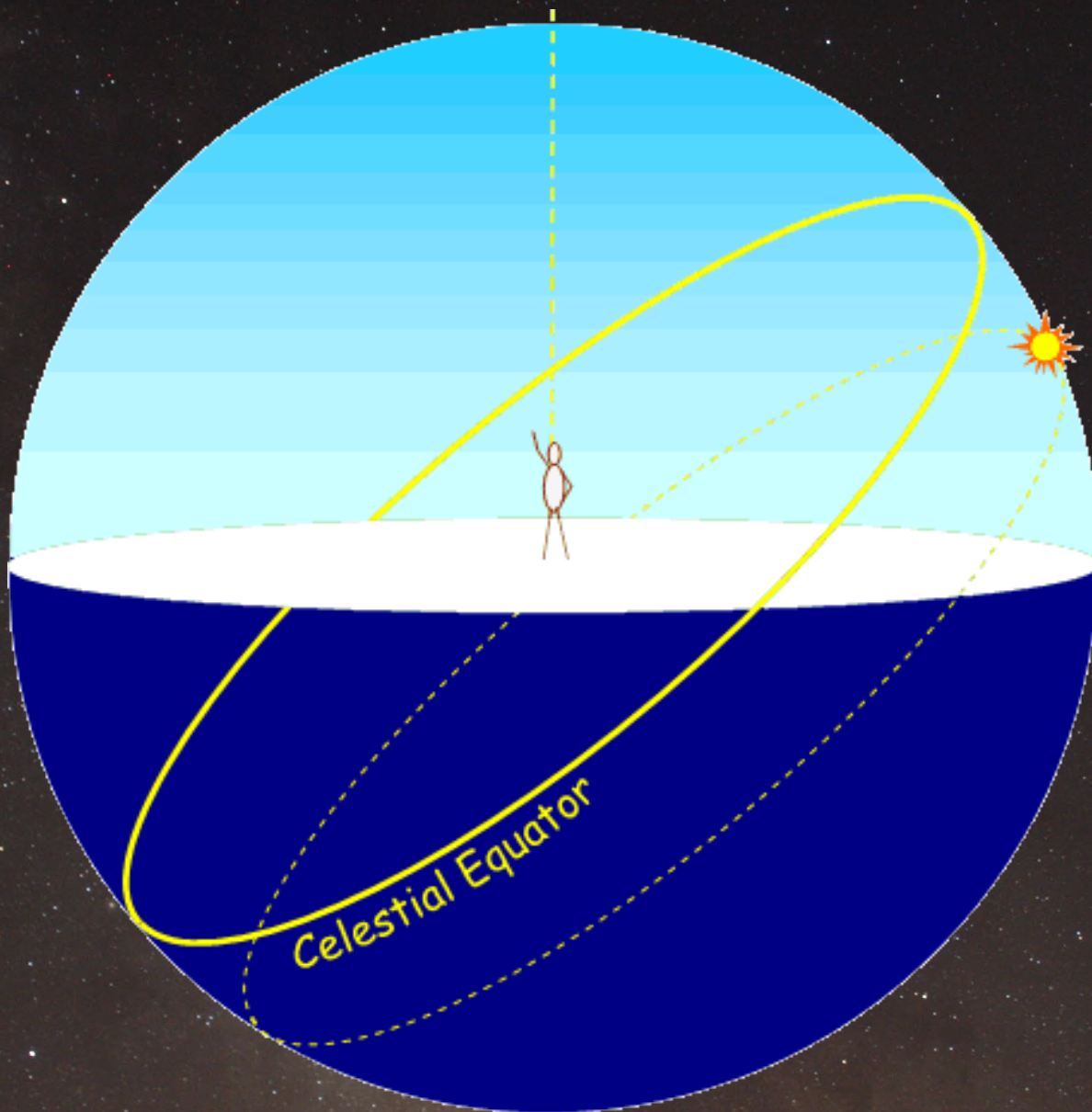
☆ View from Earth

- ☉ Sun moves $\sim 1^\circ$ /day eastward across stars
- ☉ Sun moves north and south in declination
- ☉ Solstices & Equinoxes are positions in the sky.

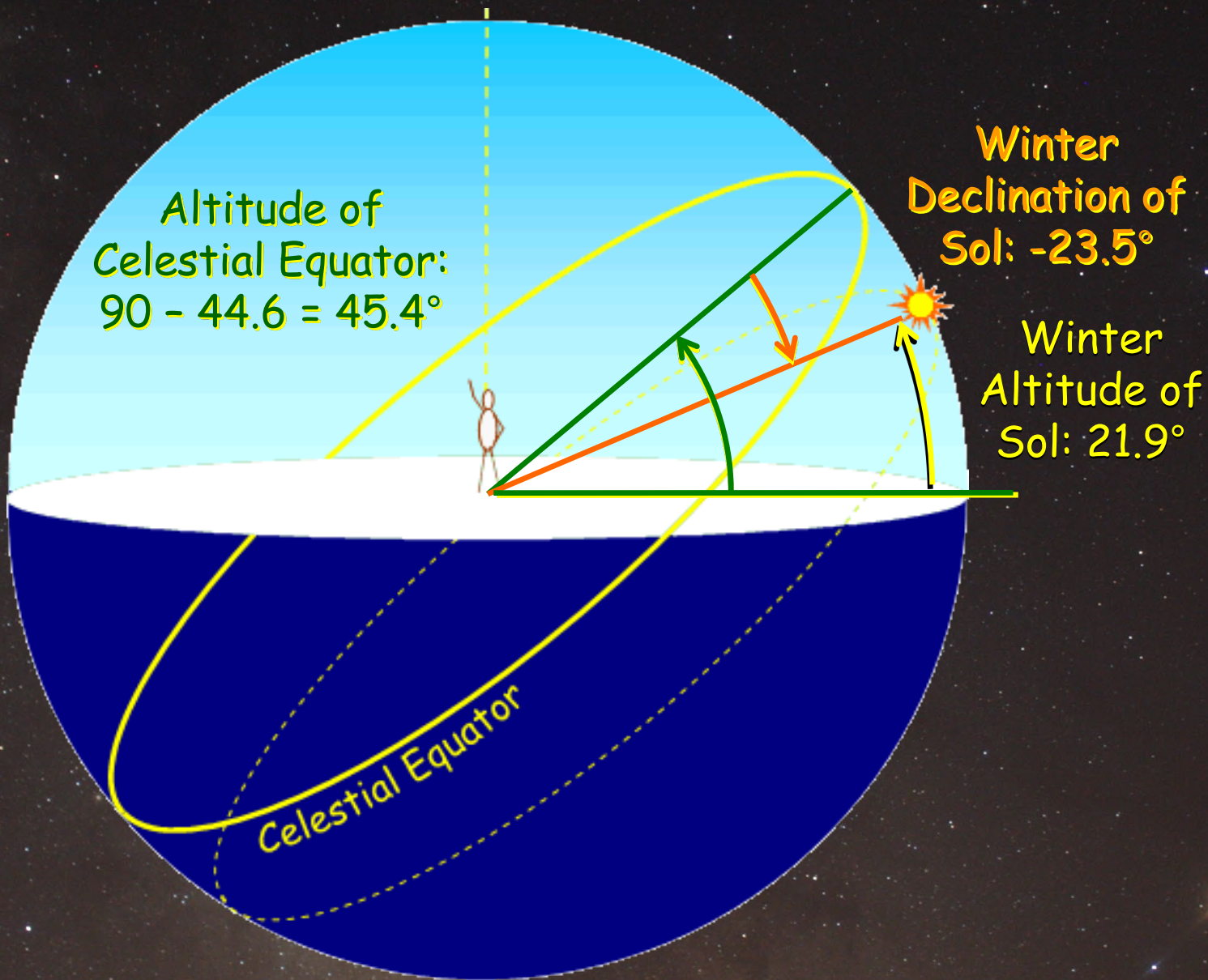


This motion is
through the YEAR!

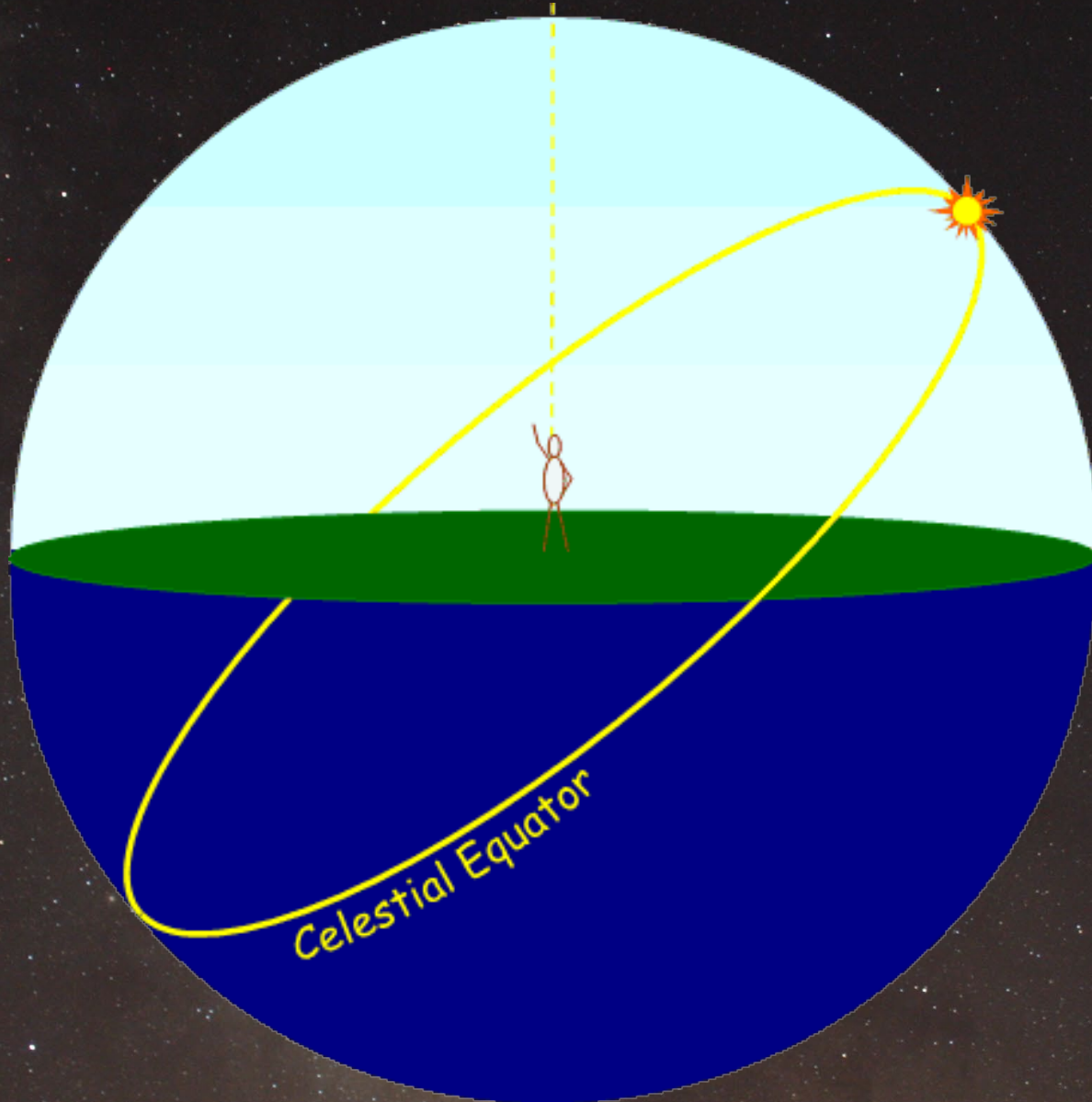
Sun's path on a winter day



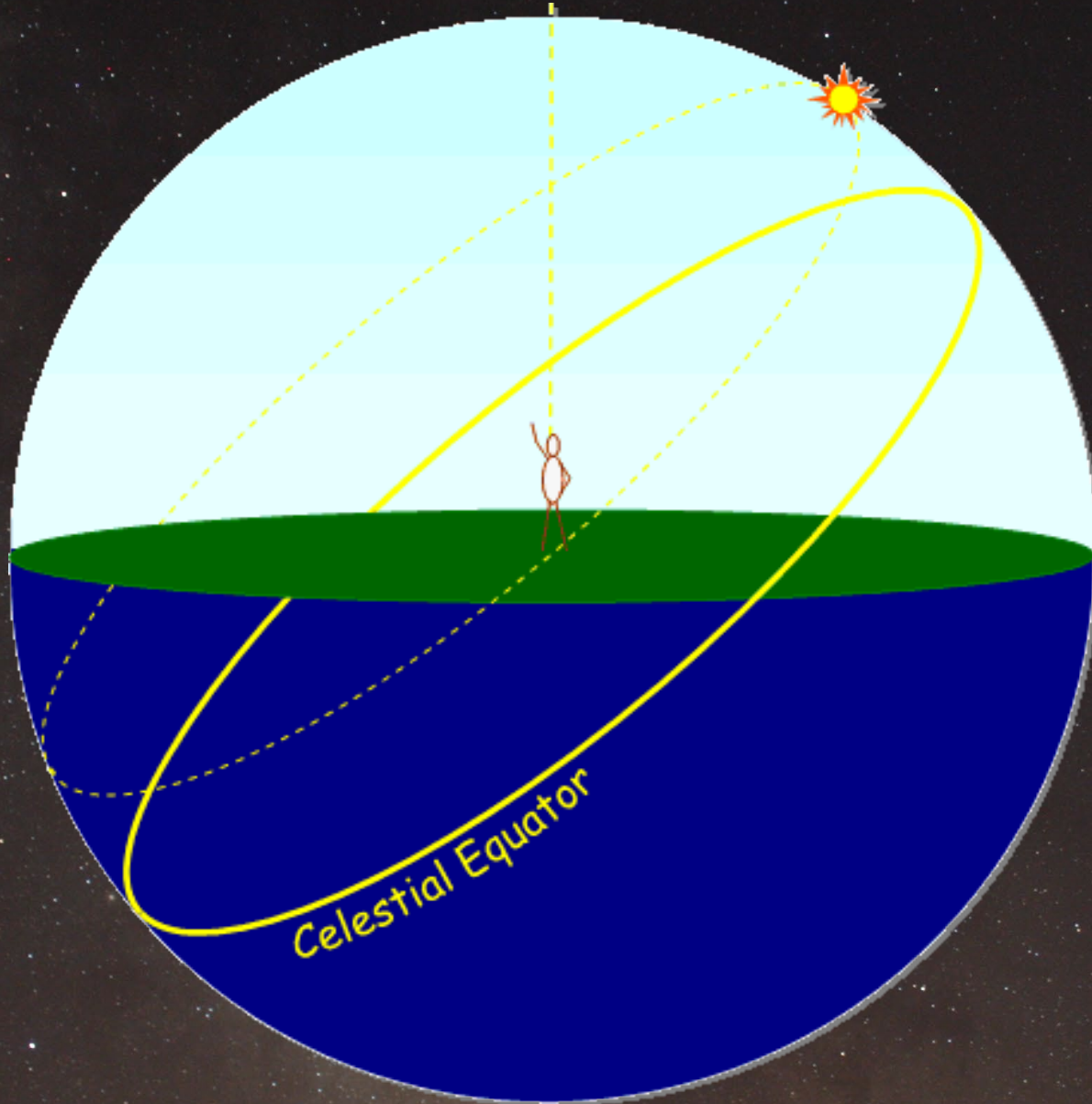
Sun's path on a winter day



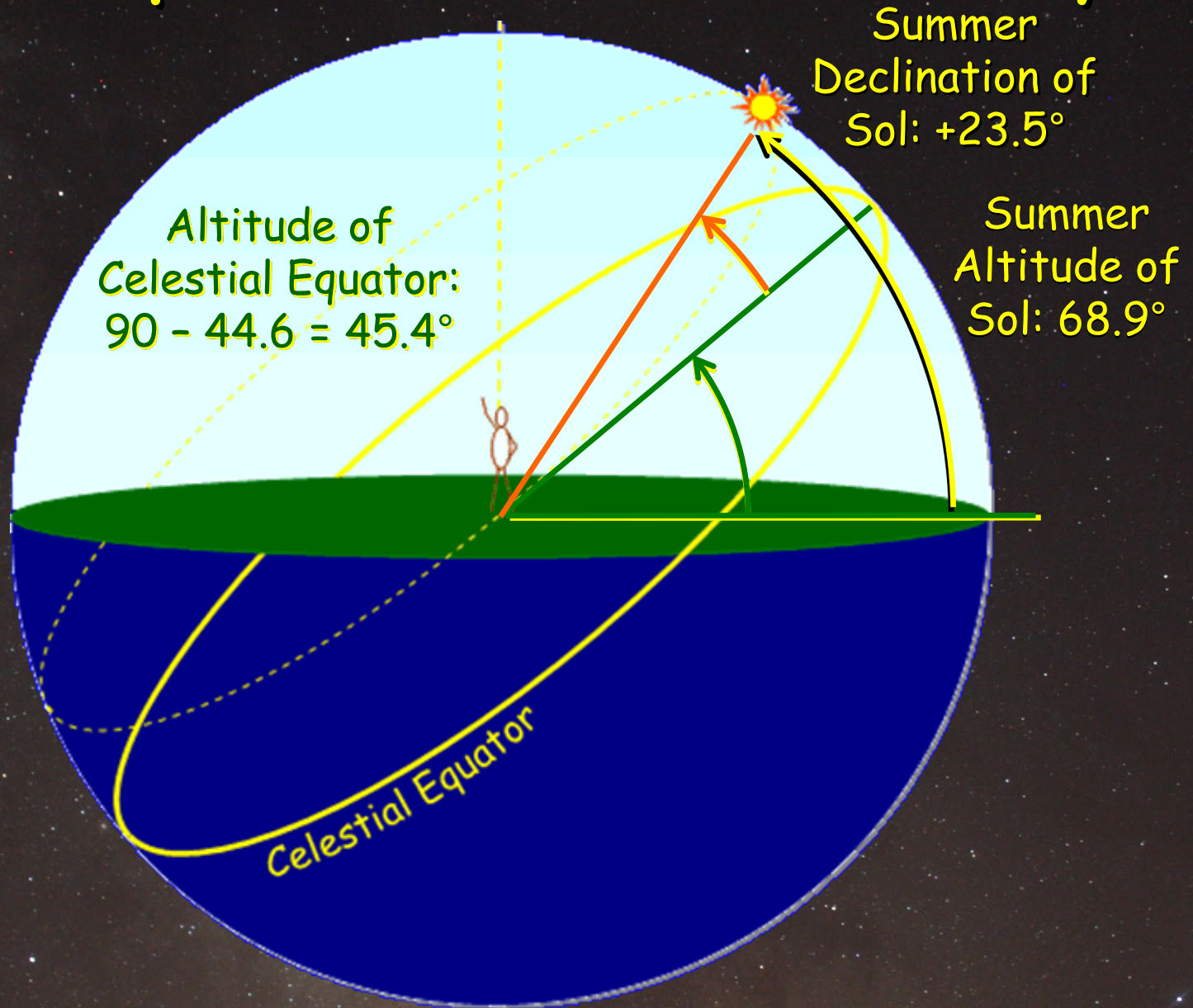
Sun's path on a fall/spring day



Sun's path on a summer day



Sun's path on a summer day



Clicker Question

At noon on the summer solstice, the sun's maximum altitude in Key West (24.6°N) is

A. 41.9°

B. 65.4°

C. 88.9°

Hint:

$$90^\circ - 24.6^\circ = 65.4^\circ$$

Hint: What is
 $65.4^\circ + 23.5^\circ$?



Time

☆ Clock Time

- 🌍 the position of the mean sun at TZ center
 - › eg. 12 pm = transit of mean sun (avg. of analemma)
- 🌍 Mean Solar Day = 24:00:00 (hours:min:sec of time)

☆ Solar Time

- 🌍 the position of the sun wrt the observer
 - eg. Noon = sun transits
- 🌍 Solar Day varies as shown by analemma

☆ Sidereal Time

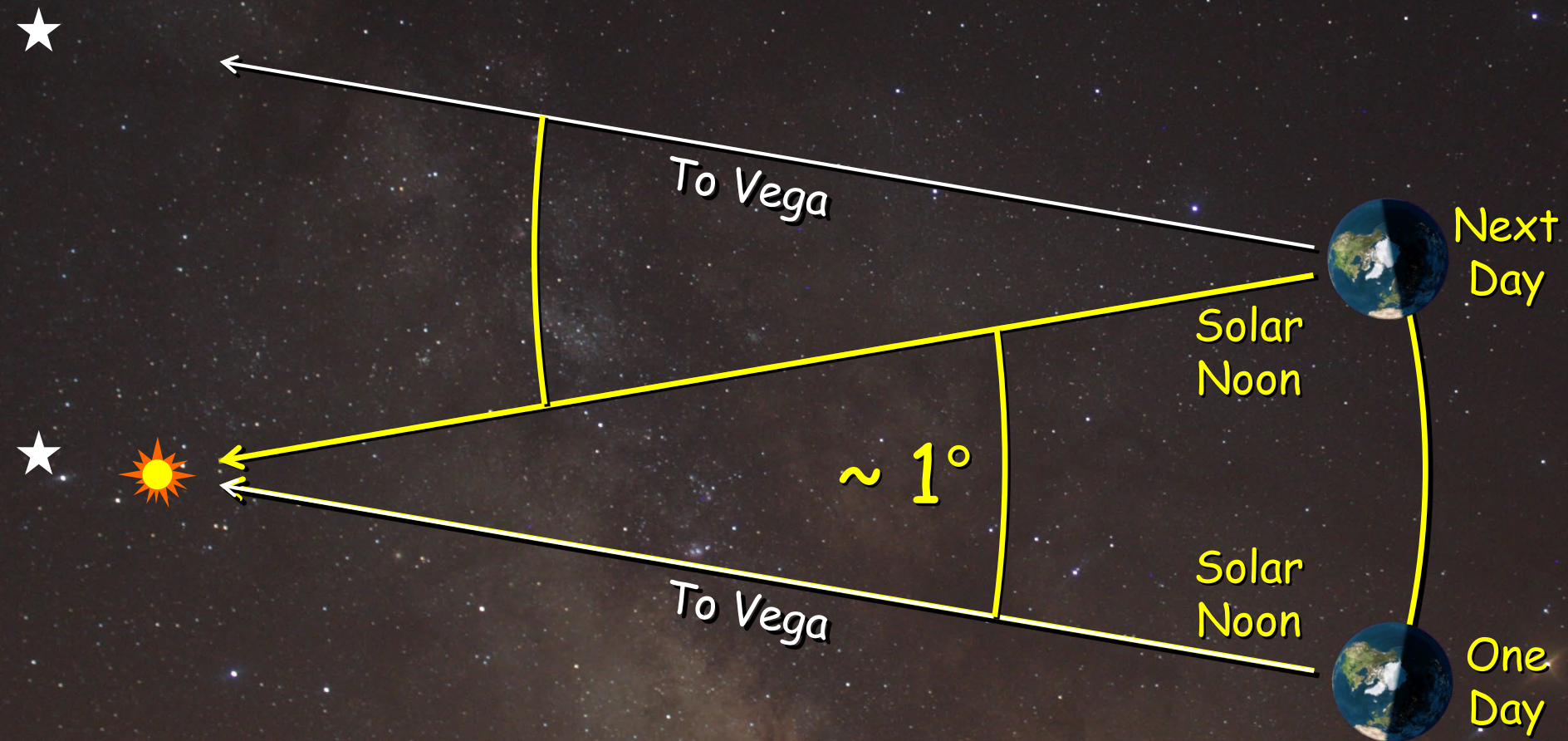
- 🌍 the position of Υ wrt the observer
 - › eg. 0^h Local Sidereal Time (LST) = Υ transits
 - › Sidereal time = R.A. on the meridian
- 🌍 Sidereal Day = 23:56:00

The Sidereal Day

🌍 Earth turns 360° with respect to stars

) eg. Vega transit to Vega Transit

🌍 23:56:00

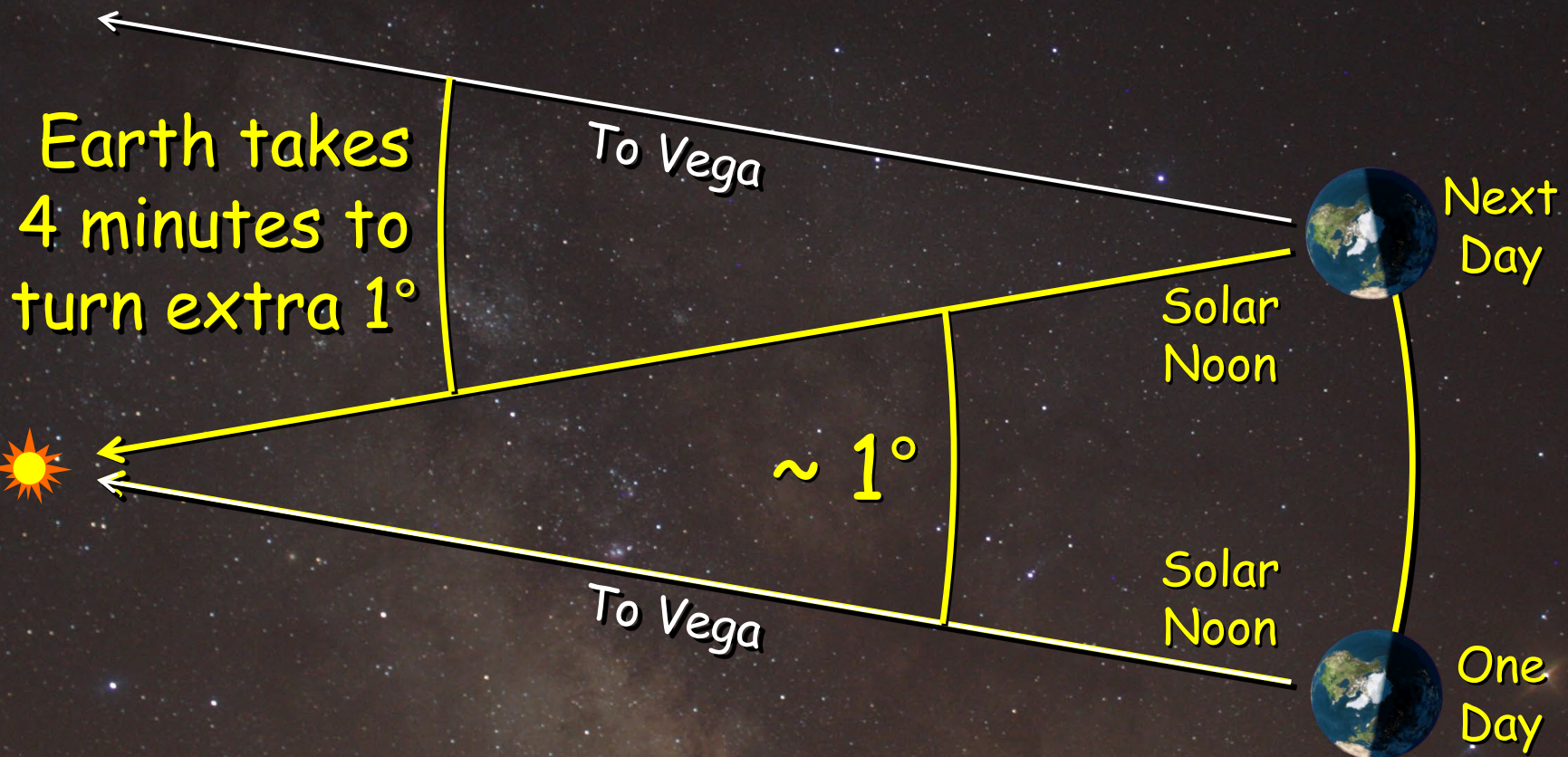


The Sidereal Day

🌍 Earth turns 360° with respect to stars

) eg. Vega transit to Vega Transit

🌍 23:56:00

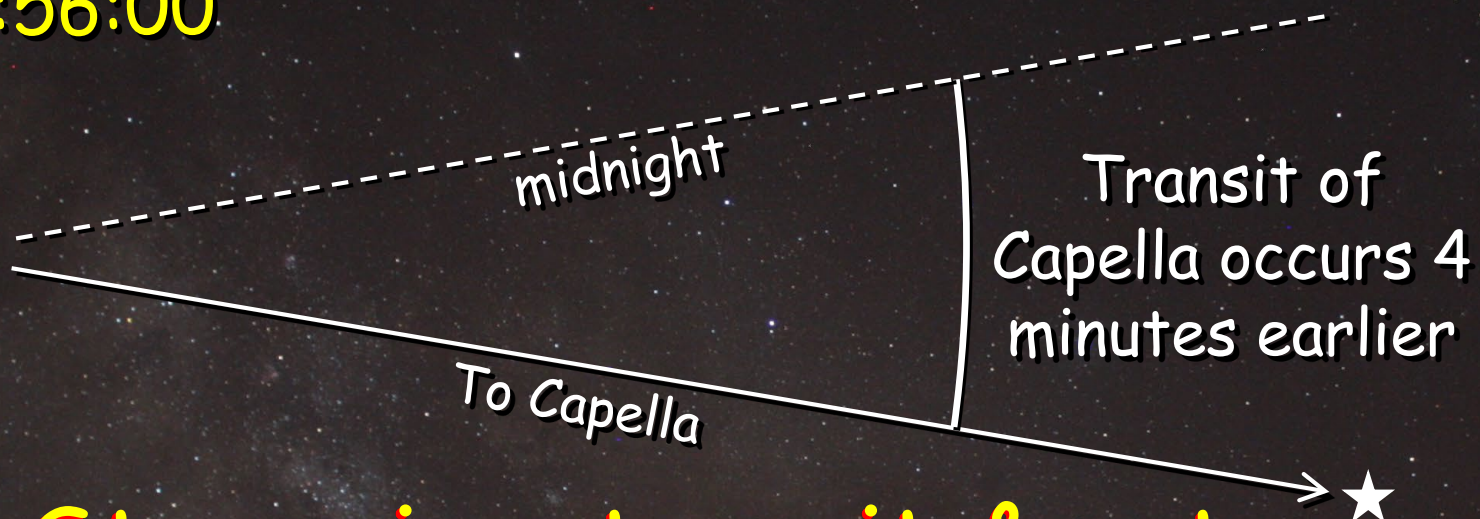


The Sidereal Day

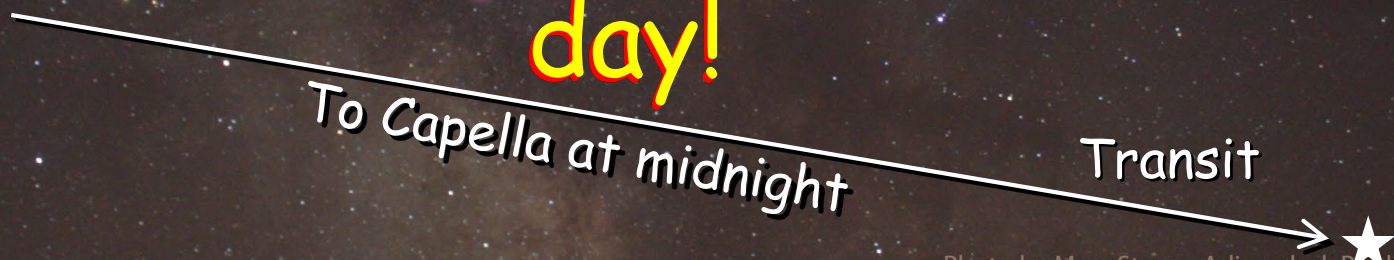
🌍 Earth turns 360° with respect to stars

) eg. Capella transit to Capella Transit

🌍 23:56:00



Stars rise, transit & set
four minutes earlier each
day!



The Sidereal Day

Sidereal Day: 360° rotation puts star back on meridian

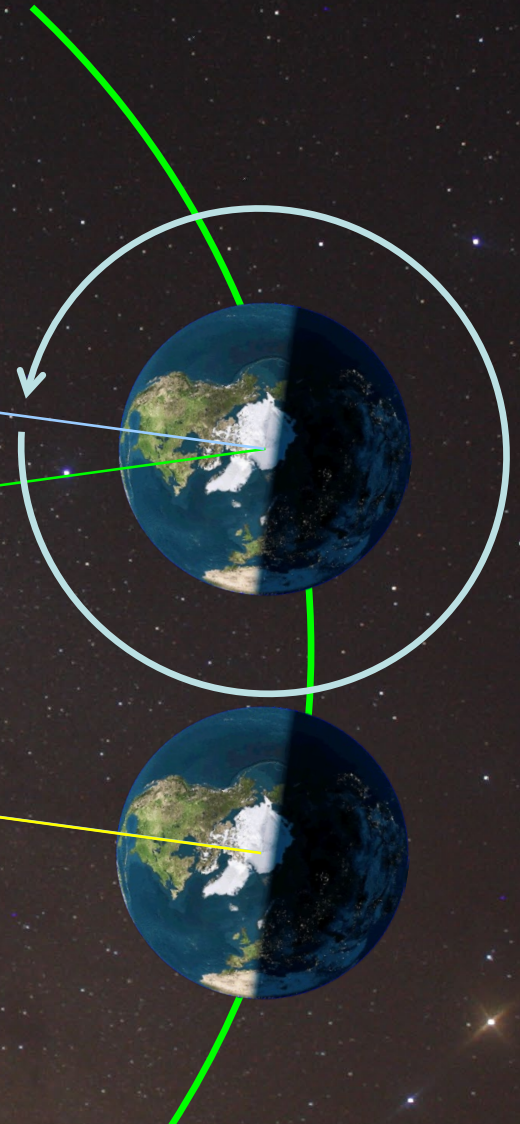
to distant star



~1° along orbit

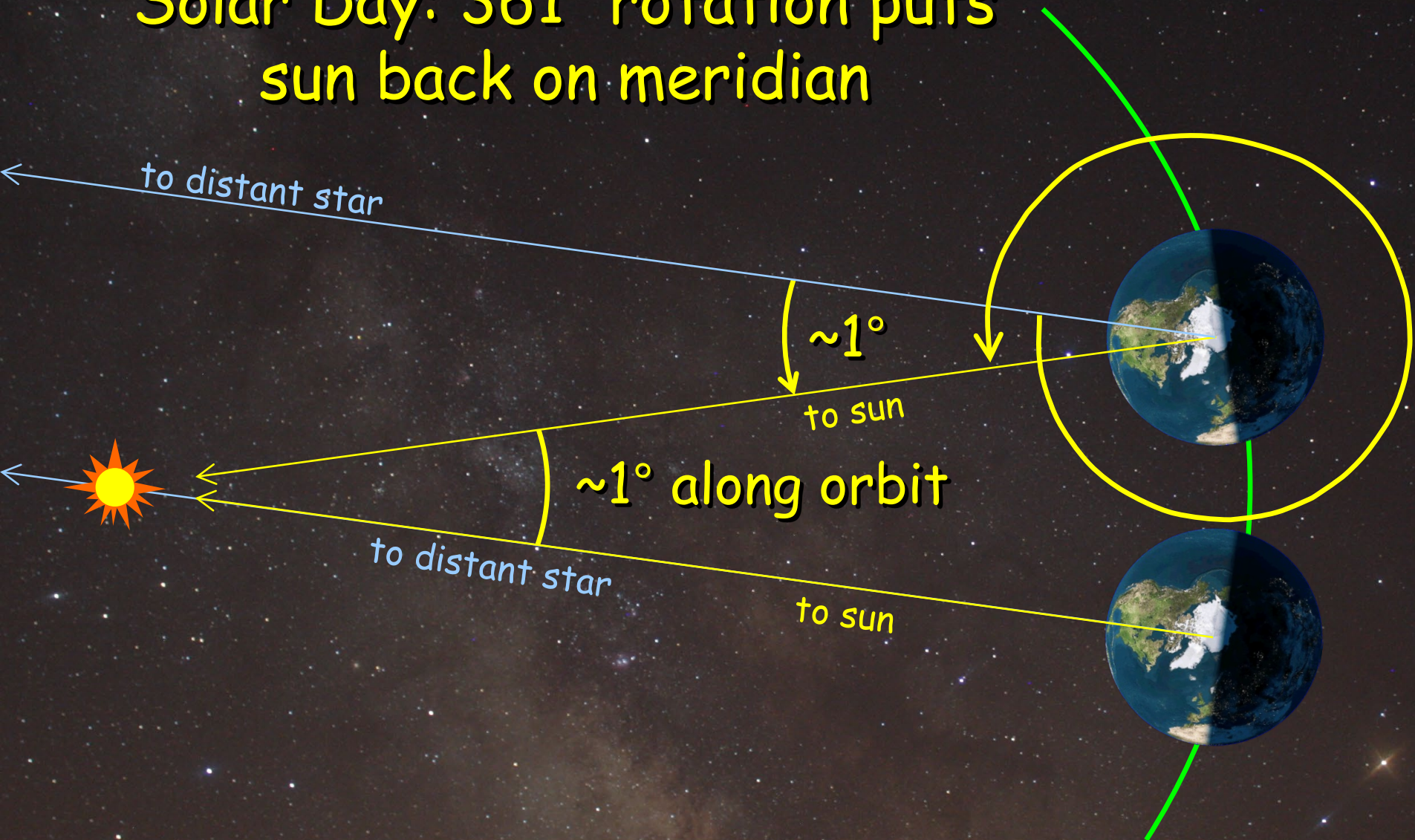
to distant star

to sun



The Solar Day

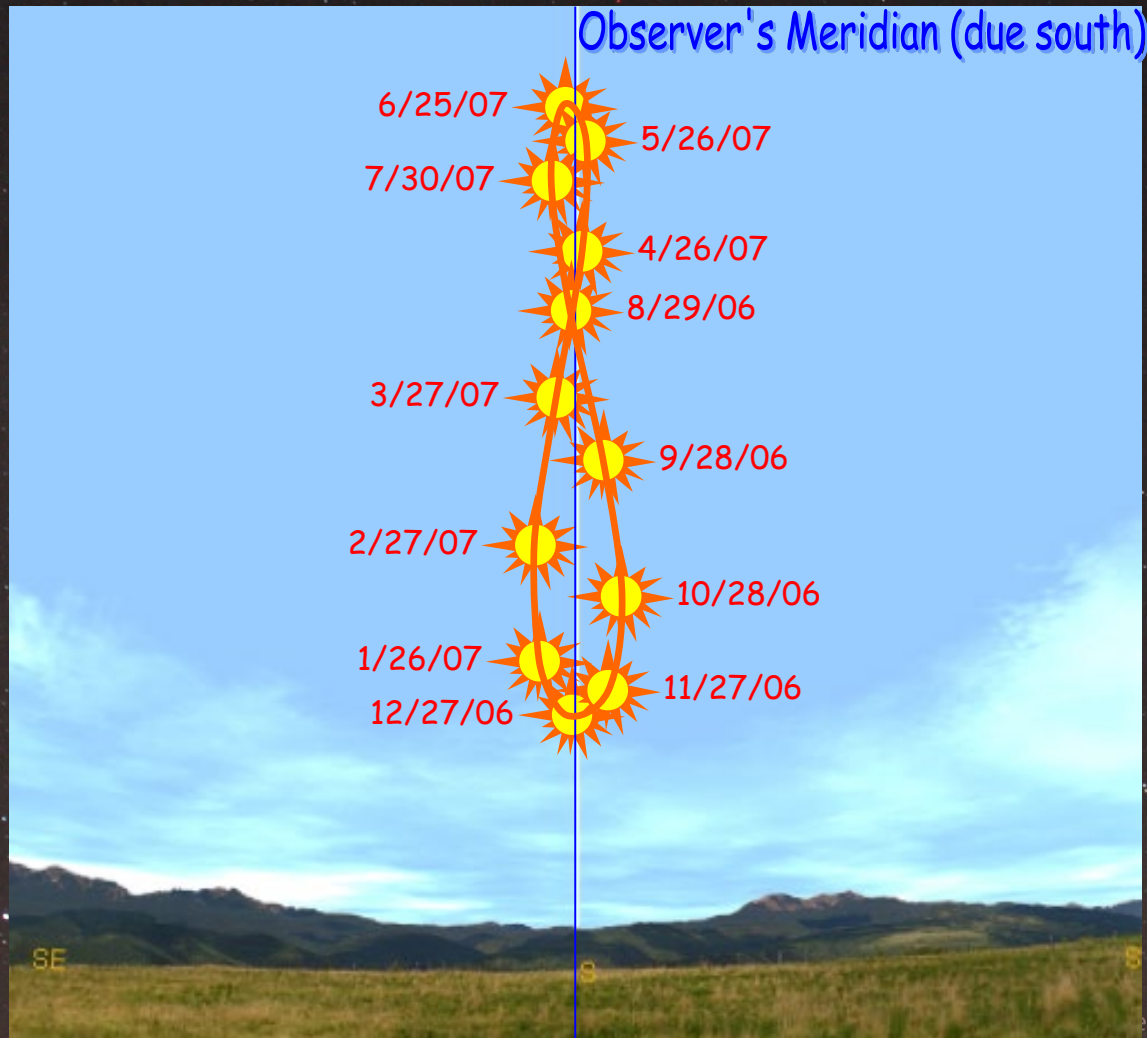
Solar Day: 361° rotation puts sun back on meridian



The Sun at Noon

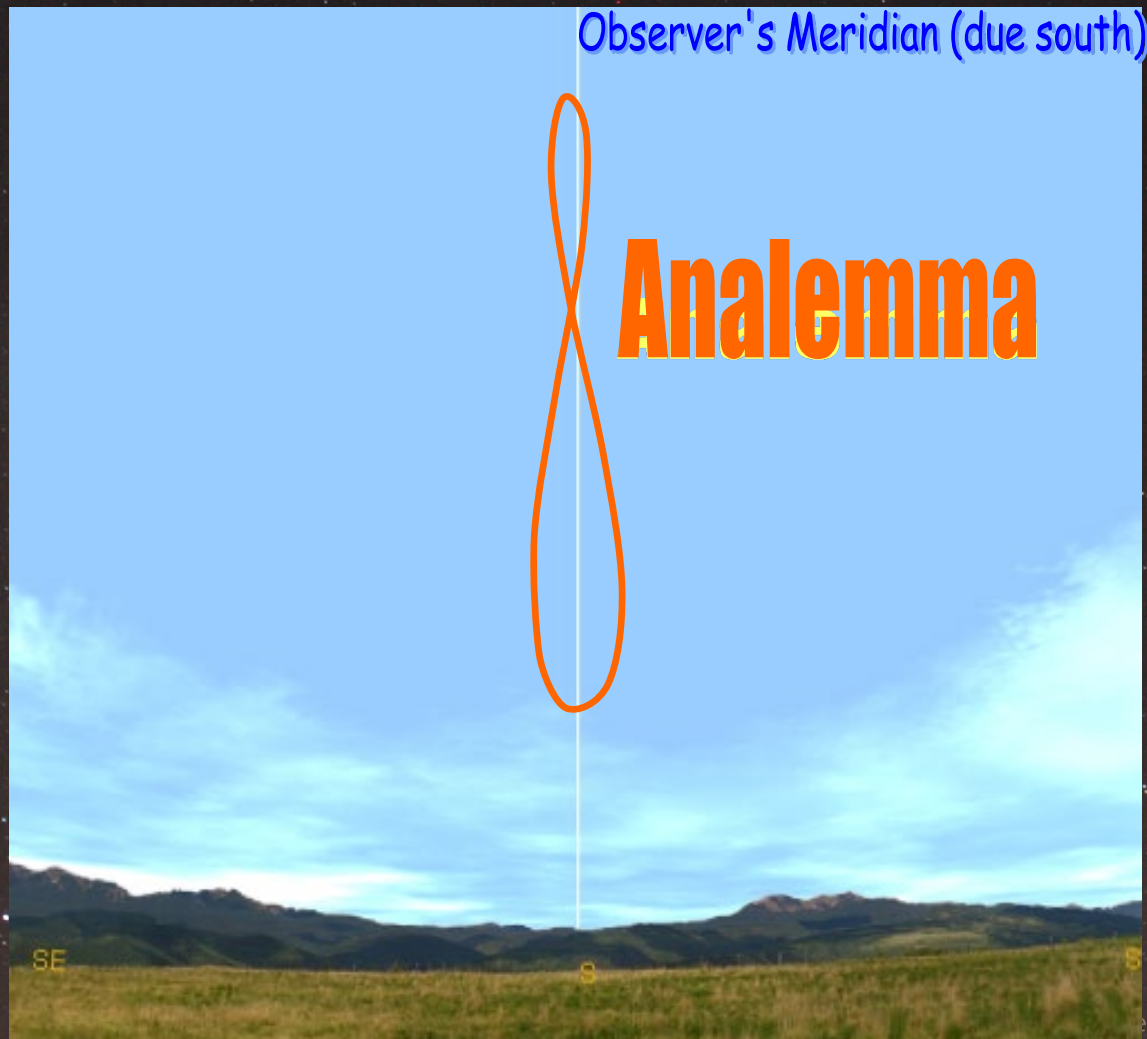
☆ Noon \Rightarrow Sun on meridian

☆ Sun's position varies: the Analemma



The Sun at Noon

- ☆ Noon \Rightarrow Sun on meridian
- ☆ Sun's position varies: the Analemma



The Analemma

☆ Position of true sun at clock noon

🌍 Clock Noon

- › 12:00 pm in a 24:00:00 day
- › Position of Mean Sun at noon

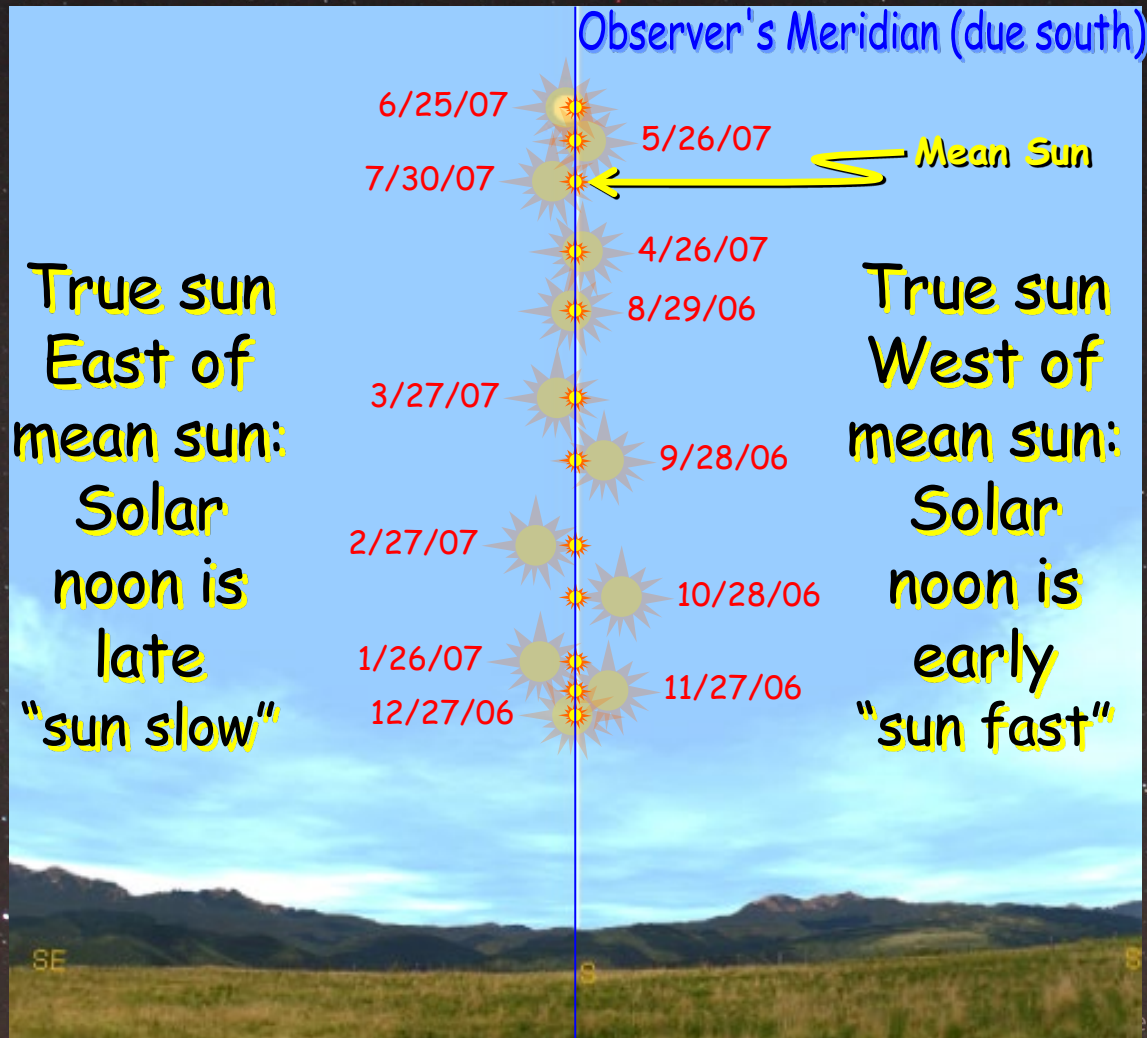
🌍 True Sun's Position

- › varies due to Sun's speed along path
 - ∩ varies due to elliptical path
 - ∩ varies due to tilted path



Mean Sun & True Sun

- ☆ Mean sun on meridian defines clock noon
- ☆ True sun on meridian defines solar noon



Solar Noon Today (9/13/22)

☆ Potsdam ($44^{\circ} 40' \text{ N}$, $75^{\circ} 00' \text{ W}$)

🌍 Standard time of solar noon = 11:54:04 am

🌍 Daylight time of solar noon = 12:54:04 pm

☆ Canton ($44^{\circ} 36' \text{ N}$, $75^{\circ} 10' \text{ W}$)

🌍 Standard time of solar noon = 11:54:44 am

🌍 Daylight time of solar noon = 12:54:44 pm

🌍 40 seconds later than Potsdam

» Earth turns 1° in 4 minutes

⇒ Earth turns $15'$ in 1 minute

⇒ Earth turns $10'$ in 40 seconds!!

⇒ Celestial events in Canton

40 seconds later than in Potsdam!!

Solar Noon Today (9/18/25)

☆ www.spot-on-sundials.co.uk/calculator.html

Print Your Solar Noon Calendar

Our [latitude and longitude](#) page will help you to find the input data you need for our unique Solar Noon Calculator

The time of solar noon depends on the Equation of Time and on the difference in longitude between your location and the standard meridian of the time zone you are in. It is slightly different for every day of the year. Our unique Solar Noon Calculator will provide you with a table showing the exact time of solar noon for your location for each day of the year. If you prefer, you can print out the values of the Equation of Time, which gives you the difference between solar time and clock time for each day of the year.

Note that our calculator requires that your latitude and longitude be in decimal format. If your co-ordinates are in Degrees, Minutes, Seconds please click [here](#).

	Example	Your Details	Comments
Location	Epsom England	<input type="text"/>	<i>this information is displayed across the top of your calendar, it is not included in any calculations</i>
Latitude	51.33250 N	<input type="text"/> <input type="text"/>	<i>optional - enter your latitude if you want your latitude/longitude co-ordinates to be displayed on your calendar</i>
Longitude	0.26722 W	<input type="text"/> W	<i>required - Longitude is used in the calculations</i>
Time Zone	US Eastern Montreal, New York, Columbia, Peru	<input type="text"/>	<i>required - select your time zone from the drop-down list</i>
Type of Calendar	Solar Noon <input checked="" type="radio"/> Equation of Time <input type="radio"/>		Solar Noon displays the exact time of solar noon each day. Equation of Time displays the difference between solar time and the standard time where you are.

If your area has daylight saving time in the summer, we recommend that you highlight or draw a box round the relevant time, and write "Add one hour for daylight saving time" at the foot of the relevant months.

Note: The values given by the Calculator are averages for the full leap year cycle of four years (1,461 days) and change slightly from year to year. The range of variation for the 1st day of each month is shown below:

Jan - 21 secs	May - 5 secs	Sept - 6 secs
Feb - 6 secs	June - 7 secs	Oct - 15 secs
Mar - 9 secs	July - 9 secs	Nov - 1 sec
Apr - 14 secs	Aug - 2 secs	Dec - 17 secs

Solar Noon Today (9/19/25)

Solar Noon Calendar for Potsdam, NY at 44.7N : 75.0W

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
1	12:03:32	12:13:32	12:12:13	12:03:44	11:57:06	11:57:57	12:04:01	12:06:23	12:00:03	11:49:35	11:43:31	11:49:06
2	12:04:00	12:13:39	12:12:01	12:03:27	11:56:59	11:58:07	12:04:12	12:06:19	11:59:38	11:49:16	11:43:30	11:49:29
3	12:04:28	12:13:46	12:11:58	12:03:10	11:56:53	11:58:17	12:04:23	12:06:14	11:59:18	11:48:57	11:43:30	11:49:53
4	12:04:55	12:13:52	12:11:33	12:02:53	11:56:48	11:58:28	12:04:34	12:06:08	11:58:58	11:48:38	11:43:30	11:50:17
5	12:05:22	12:13:57	12:11:22	12:02:37	11:56:44	11:58:38	12:04:45	12:06:02	11:58:38	11:48:20	11:43:32	11:50:42
6	12:05:48	12:14:01	12:11:04	12:02:18	11:56:38	11:58:49	12:04:55	12:05:55	11:58:18	11:48:02	11:43:34	11:51:07
7	12:06:14	12:14:05	12:10:53	12:02:01	11:56:35	11:59:01	12:05:04	12:05:48	11:57:57	11:47:44	11:43:38	11:51:33
8	12:06:39	12:14:07	12:10:40	12:01:45	11:56:32	11:59:12	12:05:11	12:05:40	11:57:37	11:47:27	11:43:42	11:51:59
9	12:07:04	12:14:09	12:10:27	12:01:29	11:56:29	11:59:24	12:05:18	12:05:12	11:57:16	11:47:11	11:43:47	11:52:26
10	12:07:29	12:14:10	12:10:08	12:01:13	11:56:27	11:59:36	12:05:24	12:05:23	11:56:55	11:46:55	11:43:53	11:52:53
11	12:07:53	12:14:11	12:09:52	12:00:57	11:56:25	11:59:48	12:05:29	12:05:13	11:56:34	11:46:39	11:43:59	11:53:21
12	12:08:16	12:14:10	12:09:36	12:00:42	11:56:24	12:00:00	12:05:16	12:05:03	11:56:13	11:46:24	11:44:07	11:53:48
13	12:08:38	12:14:09	12:09:21	12:00:27	11:56:24	12:00:13	12:05:03	12:04:52	11:55:51	11:46:09	11:44:15	11:54:17
14	12:09:00	12:14:07	12:09:03	12:00:12	11:56:24	12:00:26	12:06:00	12:04:44	11:55:30	11:45:55	11:44:25	11:54:45
15	12:09:22	12:14:04	12:08:46	11:59:58	11:56:25	12:00:39	12:06:06	12:04:29	11:55:09	11:45:41	11:44:35	11:55:14
16	12:09:43	12:14:01	12:08:29	11:59:44	11:56:26	12:00:52	12:06:11	12:04:16	11:54:47	11:45:28	11:44:46	11:55:43
17	12:10:03	12:13:56	12:08:12	11:59:30	11:56:28	12:01:05	12:06:17	12:04:03	11:54:26	11:45:16	11:44:58	11:56:12
18	12:10:22	12:13:52	12:07:55	11:59:17	11:56:30	12:01:18	12:06:21	12:03:50	11:54:04	11:45:04	11:45:10	11:56:42
19	12:10:40	12:13:46	12:07:37	11:59:04	11:56:33	12:01:31	12:06:25	12:03:36	11:53:43	11:44:53	11:45:24	11:57:11

Canton is 10' west of Potsdam
 Potsdam 11:54:04 am



Location

Epsom
England

this information is displayed across the top of your calendar, it is not included in any calculations.

Solar Noon Calendar for Canton, NY at 44.6N : 75.167W

	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
1	12:04:12	12:14:12	12:12:53	12:04:24	11:57:46	11:58:37	12:04:41	12:07:03	12:00:43	11:50:15	11:44:11	11:49:46
2	12:04:40	12:14:19	12:12:41	12:04:07	11:57:39	11:58:47	12:04:52	12:06:59	12:00:18	11:49:56	11:44:10	11:50:09
3	12:05:08	12:14:26	12:12:28	12:03:49	11:57:33	11:58:57	12:05:03	12:06:54	11:59:53	11:49:37	11:44:10	11:50:33
4	12:05:35	12:14:32	12:12:15	12:03:32	11:57:27	11:59:10	12:05:14	12:06:43	11:59:33	11:49:18	11:44:10	11:50:57
5	12:06:02	12:14:37	12:12:02	12:03:15	11:57:23	11:59:18	12:05:25	12:06:42	11:59:18	11:49:00	11:44:12	11:51:22
6	12:06:28	12:14:41	12:11:44	12:02:58	11:57:18	11:59:29	12:05:35	12:06:42	11:58:58	11:48:42	11:44:14	11:51:47
7	12:06:54	12:14:45	12:11:33	12:02:41	11:57:14	11:59:41	12:05:44	12:06:28	11:58:33	11:48:24	11:44:18	11:52:13
8	12:07:19	12:14:47	12:11:21	12:02:24	11:57:11	11:59:52	12:05:53	12:06:20	11:58:11	11:48:07	11:44:22	11:52:39
9	12:07:44	12:14:49	12:11:03	12:02:08	11:57:09	12:00:04	12:06:02	12:06:12	11:57:56	11:47:51	11:44:27	11:53:06
10	12:08:09	12:14:50	12:10:48	12:01:53	11:57:07	12:00:16	12:06:11	12:06:03	11:57:35	11:47:35	11:44:33	11:53:33
11	12:08:33	12:14:51	12:10:32	12:01:37	11:57:05	12:00:28	12:06:19	12:05:53	11:57:14	11:47:19	11:44:39	11:54:01
12	12:08:56	12:14:50	12:10:16	12:01:22	11:57:04	12:00:40	12:06:26	12:05:43	11:56:53	11:47:04	11:44:47	11:54:28
13	12:09:18	12:14:48	12:10:00	12:01:07	11:57:04	12:00:55	12:06:33	12:05:32	11:56:31	11:46:49	11:44:55	11:54:57
14	12:09:40	12:14:47	12:09:43	12:00:52	11:57:04	12:01:06	12:06:40	12:05:21	11:56:10	11:46:35	11:45:05	11:55:25
15	12:10:02	12:14:44	12:09:26	12:00:38	11:57:05	12:01:19	12:06:46	12:05:09	11:55:49	11:46:21	11:45:15	11:55:54
16	12:10:23	12:14:41	12:09:09	12:00:24	11:57:06	12:01:32	12:06:51	12:04:56	11:55:27	11:46:08	11:45:26	11:56:23
17	12:10:43	12:14:36	12:08:52	12:00:10	11:57:08	12:01:45	12:06:57	12:04:43	11:55:06	11:45:56	11:45:38	11:56:52
18	12:11:02	12:14:32	12:08:35	11:59:57	11:57:10	12:01:58	12:07:01	12:04:30	11:54:44	11:45:44	11:45:50	11:57:22
19	12:11:20	12:14:26	12:08:17	11:59:44	11:57:13	12:02:11	12:07:05	12:04:16	11:54:23	11:45:33	11:46:04	11:57:51
20	12:11:38	12:14:20	12:08:00	11:59:34	11:57:17	12:02:24	12:07:08	12:04:02	11:54:04	11:45:22	11:46:18	11:58:24

Solar noon in Canton is 40 sec later than Potsdam
 Canton 11:54:44 am

Doing the Math

☆ Mean Sun

🌍 Projection of sun onto Celestial Equator

› moves 360° in one year (365.242191 days)

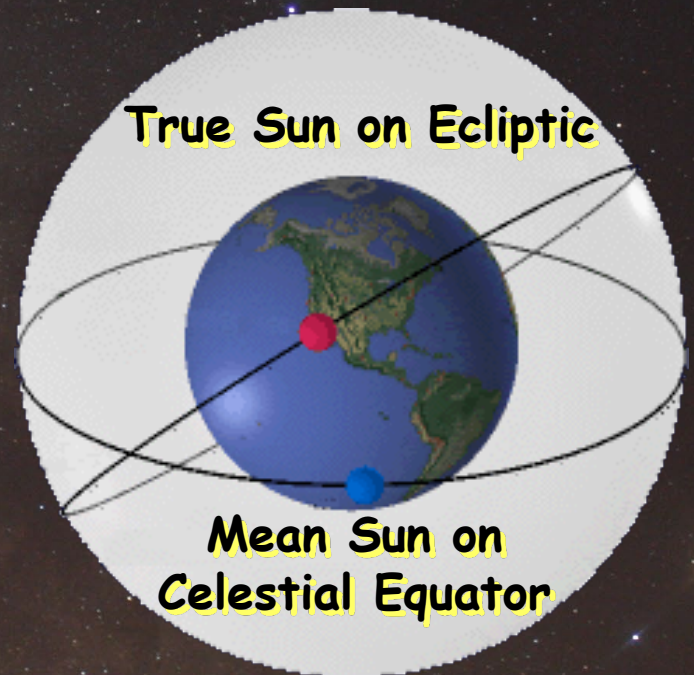
$$V_{\text{Mean Sun}} = \frac{360^\circ}{365.242191 \text{ days}} = 0.985647356^\circ/\text{day}$$

☆ True Sun

🌍 speed varies due to

› Sun's changing Declination

› Elliptical orbit



The Calendar

☆ Solar Calendars (Tropical Year = 365.2421897d)

🌍 Attempt to keep dates aligned with seasons

🌍 e.g. Vernal Equinox near March 21 { First Council of Nicaea, 325 CE

☆ Julian Calendar

🌍 Instituted by Julius Caesar in 46 BCE

› Rounded Tropical Year to 365.25 d

› Added one day every 4 years ($\frac{1}{4} = 0.25$ day/year)

∩ Added too much time!

(10.153 days in 1300 years)

∩ $365.25 - 365.2421897 = 0.00781$ extra days/year

∩ After 1300 years, Vernal Equinox occurred on March 31!

∩ Messed up date of Easter!!

∩ Easter = first Sunday after first full moon after ∩

The Calendar

☆ **Gregorian Calendar** (Year = 365.2421897d)

🌐 **Instituted by Pope Gregory XIII, 1582**

› **Dropped 10 days**

‣ **Thursday, Oct. 4 1582 followed by Friday Oct. 15**

‣ **British Empire & American Colonies:**

Wed. Sep. 2, 1752 followed by Thu. Sep. 14

The Calendar

☆ **Gregorian Calendar** (Year = 365.2421897d)

🌐 **Instituted by Pope Gregory XIII, 1582** **Close!**

› **Dropped 10 days**

∩ Thursday, Oct. 4 1582 followed by Friday Oct. 15

∩ **British Empire & American Colonies:**

Wed. Sep. 2, 1752 followed by Thu. Sep. 14

› **Century Years not divisible by 400 not leap years**

∩ Leap years 97 in 400 ($\frac{97}{400} = 0.24219$)

∩ $365.2425 - 365.24219 = 0.00031$ extra days/year

∩ 1600 = leap year for everyone

(0.403 days in 1300 years)

∩ 1700 = leap year only for those on Julian Calendar (Brits)

‣ British Empire had to drop 11 days, not 10!

‣ George Washington's Birthday

Julian: Feb. 11, 1731

Gregorian: Feb. 22, 1731

Cross Quarter Days

- ☆ Days $\frac{1}{2}$ way between solstices & equinoxes
- ☆ 1st days of seasons on some calendars (Celt)

🌍 Beltane ~ May 1

› $\frac{1}{2}$ way from Vernal Equinox to Summer Solstice

🌍 Lughnasa ~ August 2

› $\frac{1}{2}$ way from Summer Solstice to Autumnal Equinox

🌍 All Hallows (Samhain) ~ November 1

› $\frac{1}{2}$ way from Autumnal Equinox to Winter Solstice

🌍 Candlemas (Imbolc) ~ February 2

› $\frac{1}{2}$ way from Winter Solstice to Vernal Equinox

If Candlemas Day be fair and bright,
Winter will have another flight

If Candlemas Day be damp & black,
It will carry cold winter away on its back.

Position of Sunrise & Sunset

- ☆ Azimuth of rising depends on δ

$$A_{\text{rise}} = \cos^{-1} \left(\frac{\sin \delta}{\cos \lambda} \right) \text{ degrees}$$

- ☆ Sunrise appears to move along horizon

🌐 original calendar!

eg. Stonehenge, Machu Pichu, Woodhenge (Illinois)



Position of Sunset

12/9/9 3:40 pm EST
40 minutes before
sunset

SW

W



TRADUCCIONES CONTINUAS