

9.14) a) VERIFY THAT THE UNITS OF μ_B ARE $\text{Amp} \cdot \text{m}^2$.

b) VERIFY THAT $\text{A} \cdot \text{m}^2 = \frac{\text{J}}{\text{T}}$ USING $\vec{F} = q\vec{v} \times \vec{B}$

$$a) \mu_B = \frac{e\hbar}{2m_e} \sim \frac{C \cdot (\text{J} \cdot \text{s})}{\text{kg}} \sim \frac{C \cdot \text{s}}{\text{kg}} (\text{N} \cdot \text{m}) \sim \frac{C \cdot \text{s} \cdot \text{m}}{\text{kg}} \left(\frac{\text{kg} \cdot \text{m}}{\text{s}^2} \right)$$

$$\mu_B \sim \frac{C \cdot \text{m}^2}{\text{s}} \sim \text{Amp} \cdot \text{m}^2 \quad \text{QED!}$$

- YES, THE BOHR MAGNETON IS IN $\text{A} \cdot \text{m}^2$!

b) VERIFY THAT $\text{A} \cdot \text{m}^2 = \frac{\text{J}}{\text{T}}$

FROM THE LORENTZ FORCE, $\vec{F} = q\vec{v} \times \vec{B}$,

$$\Rightarrow F \sim qvB \sim C \cdot \frac{\text{m}}{\text{s}} \cdot \text{T} \sim \frac{C}{\text{s}} \cdot \text{m} \cdot \text{T} \sim \text{Amp} \cdot \text{m} \cdot \text{T}$$

THE AMP IN TERMS OF TESLA IS

$$\text{N} \sim \text{A} \cdot \text{m} \cdot \text{T} \Rightarrow \text{A} \sim \frac{\text{N}}{\text{m} \cdot \text{T}}$$

THE UNITS OF MAGNETIC MOMENT ARE THEN

$$\mu \sim \text{A} \cdot \text{m}^2 \sim \left(\frac{\text{N}}{\text{m} \cdot \text{T}} \right) \text{m}^2 \sim \frac{\text{N} \cdot \text{m}}{\text{T}} \sim \frac{\text{J}}{\text{T}} \quad \text{QED!}$$

SO THE UNITS OF MAGNETIC MOMENT ARE $\text{A} \cdot \text{m}^2 = \frac{\text{J}}{\text{T}}$!