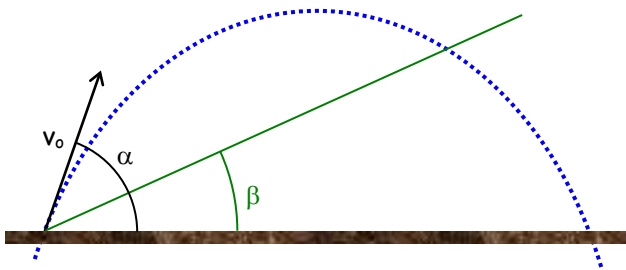


**HOMWORK SET 2: PROJECTILES**  
 Due Monday, September 5, 2022

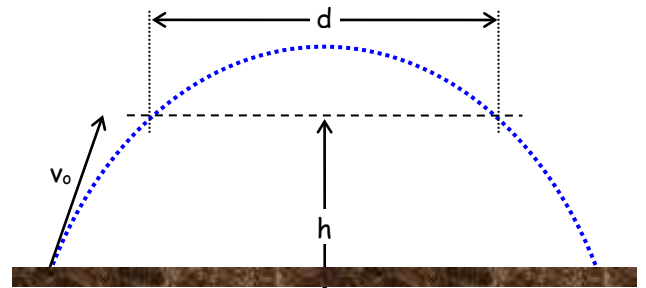


1) If a projectile is fired from the origin of the coordinate system with an initial velocity  $v_0$  and in a direction making an angle  $\alpha$  with the horizontal, show that the time required for the projectile to cross a line passing through the origin and making an angle  $\beta < \alpha$  with the horizontal is

$$t_0 = \frac{2v_0}{g} (\sin \alpha - \cos \alpha \tan \beta)$$

2) A projectile is fired with a velocity  $v_0$  such that it passes through two points both a distance  $h$  above the horizontal. Show that if the gun is adjusted for maximum range (derive what the angle is!), the separation of the points is

$$d = \frac{v_0}{g} \sqrt{v_0^2 - 4gh}$$



3) Two balls are thrown with equal speeds from the top of a cliff of height  $h$ . One is thrown at an angle  $\alpha$  above the horizontal. The other is thrown at an angle  $\beta$  below the horizontal. Show that each strikes the ground with the same speed and find the speed in terms of  $h$  and the initial speed  $v_0$ .

Remember, final speed is total speed,  $v = \sqrt{v_x^2 + v_y^2}$ , not just  $v_y$ !

