## Homework Set 8: Conservation Laws <br> Due Wednesday, September 27, 2023

1) The figure shows the result of a collision between two objects of unequal mass.
a) Find the speed $v_{2}$ of the larger mass after the collision and the angle $\theta_{2}$.
b) Show that the collision is elastic.

USE RATIOS FOR THE SINES \& COSINES INSTEAD OF FINDING THE ANGLES USING YOUR CALCULATOR.

2) A 6 kg projectile is launched at an angle of $30^{\circ}$ with the horizontal and an initial speed of $40 \mathrm{~m} / \mathrm{s}$. At the top of its flight, it explodes into two parts with masses of 2 and 4 kg . The fragments move horizontally just after the explosion, and the 2 kg piece lands back at the launch site.
a) Where does the 4 kg piece land? (MOMENTUM is CONSERVED IN THE EXPLOSION, KINEMATICS wILL TELL YOU THE SPEED OF THE 2 kg PIECE SO YOU CAN FIND vo FOR THE 4 kg PIECE.) $\quad x_{4}=212 \mathrm{~m}$
b) Compute the kinetic energy of the projectile just before the explosion and the total kinetic energy of the fragments just after the explosion to find the energy of the explosion. $\quad \Delta E=7.18 \mathrm{~kJ}$
3) A woman of mass $m$ stands at the edge of a rotating circular turntable. The turntable has a radius $R$, moment of inertia $I$, and rotates without friction. The angular velocity about the vertical axis through the center of the turntable is $\omega_{0}$. The woman walks radially inward. What is the final angular velocity of the system? Assume $m_{\text {woman }} R^{2}=3 I$ and that the woman has a moment of inertia of $I / 10$ when she is standing at the center (Hint: Use the parallel axis theorem to find her moment of inertia at the edge.).
$\omega_{f}=3.73 \omega_{0}$

4) A 16 g bullet is fired into the bob of a ballistic pendulum of mass 1.5 kg . When the bob is at its maximum height, the strings make an angle of $60^{\circ}$ with respect to the vertical. The length of the pendulum is 2.3 m . Find the initial speed of the bullet.
DON' T FORGET TO CONSERVE MOMENTUM!!
$v_{b}=449.8 \mathrm{~m} / \mathrm{s}$
5) A 2.0 kg block slides down a frictionless curved ramp from rest onto a rough horizontal surface (on to the brown surface) until it stops at $d$.
a) Write an expressions for the block's speed at the bottom of the ramp and the work done by friction in the horizontal slide.
b) For $h=2 \mathrm{~m}$ and $\mu_{\mathrm{k}}=0.25$, find the distance the block slides.


